Summary of Paper	Model and Results	Comments	RBC Model with Distribution Shocks

Discussion of "Hysteresis in Unemployment and Jobless Recoveries" by D. Plotnikov

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 $<sup>^1</sup>$ Any opinions expressed here do not necessarily reflect the views of the management of the Federal Reserve Bank of San Francisco or of the Board of Governors of the Federal Reserve System



## Summary:

- Agents either work or search for work: Don't care about leisure. Negative externality as firms search harder for workers.
- Model introduces a persistent "belief shock" to  $c_t/w_t$  ratio in place of labor-leisure tradeoff.
- Steady state does not pin down c<sub>t</sub> / w<sub>t</sub> ⇒ continuum of steady state employment rates.
- Persistent belief shock  $\Rightarrow$  persistent shift in  $c_t/w_t \Rightarrow$  persistent shift in employment.

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Basic setup of	model		

Standard part:

$$\frac{1}{c_t} = \beta E_t \left\{ \frac{1}{c_{t+1}} \left[ r_{t+1} + 1 - \delta \right] \right\}$$

$$c_t + \underbrace{k_{t+1} - (1 - \delta) k_t}_{i_t} = \underbrace{r_t k_t + w_t \ell_t}_{y_t}, \qquad \begin{aligned} r_t &= \frac{\partial y_t}{\partial k_t} \\ w_t &= \frac{\partial y_t}{\partial \ell_t} \end{aligned}$$

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12.

Non-standard part:

$$c_{t} = \phi \begin{bmatrix} \frac{y_{t}^{p}}{w_{t}} \end{bmatrix} w_{t}, \qquad (\phi \equiv c_{ss} / y_{ss})$$
$$\begin{bmatrix} \frac{y_{t}^{p}}{w_{t}} \end{bmatrix} = \begin{bmatrix} \frac{y_{t-1}^{p}}{w_{t-1}} \end{bmatrix}^{0.95} \begin{bmatrix} \frac{y_{t}}{w_{t}} \end{bmatrix}^{0.05} \exp\left(\varepsilon_{t}^{b}\right), \qquad \text{persistent belief shock}$$

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Hansen (1985):

$$c_t = \frac{1}{B} w_t$$
,  $B =$  marginal disutility of labor

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Plotnikov (2015)  $\simeq$  Hansen (1985) + Persistent shock to  $\frac{1}{B}$ .

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- Simulations compare a two-shock model (Plotnikov) to a one-shock model (Hansen). Also, productivity shock is mean-reverting rather than a unit root, so there are no permanent shocks in Hansen model.

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- Other types of fundamental shocks could account for sluggish employment recoveries, e.g., distribution shocks.



Capital share = 1 - employee compensation/gross value-added of corporate bus. sector.



Summary of Paper Simple Two-Shock RBC Model See Lansing (2015 AEJ-Macro, f.) and Lansing & Markiewicz (FRBSF WP 2012-23).

Capital Owners:

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \log \left(c_t^c\right), \quad c_t^c + k_{t+1} - \left(1 - \delta\right) k_t = r_t k_t$$

Workers:

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \log \left[ c_t^w - B \exp \left( \overline{z}_t \right) \ell_t^\gamma \right], \quad c_t^w = w_t \ell_t$$
$$\overline{z}_t = \overline{z}_t + \mu, \quad (\gamma - 1)^{-1} = 10.$$

Production:

$$y_t = Ak_t^{ heta_t} \left[ \exp\left(z_t\right) n \ell_t 
ight]^{1- heta_t}$$
,  $n = 4$ ,

 $z_t$  = productivity shock (choose to match  $y_t$  series in U.S. data).

 $\theta_t$  = distribution shock (take directly from U.S. data).

$$\ell_t = \left\{ \frac{A(1-\theta_t)}{B\gamma} \left[ \frac{k_t}{\exp(z_t)n} \right]^{\theta_t} \exp\left(z_t - \overline{z}_t\right) \right\}^{\frac{1}{\gamma+\theta_t-1}} \quad \text{(decision rule)}.$$

















