# Interest Rate Risk in Banking

Peter DeMarzo, *Stanford and NBER*, Arvind Krishnamurthy, *Stanford and NBER* Stefan Nagel, *Chicago and NBER* 

# Asset Value vs Franchise Value?

• JMPS (March 2023)



Correct! But incomplete ...

• DSS (March 2023)

How to value the deposit franchise Itamar Drechsler, Alexi Savov, and Philipp Schnabl

low rates, compared to their operating costs. So the change in the value of the deposit franchise is

 $\Delta DF = 1.7 - 0 = $1.7 trillion.$ 

Thus, banks have an unrealized gain of \$1.7 trillion on their deposit franchise. This number is very similar to the unrealized losses of \$1.75 trillion, especially compared to the value of bank capital, which was \$2.2 trillion. The implied net loss to equity is thus rather small.

Incorrect! ... and commonly misinterpreted ...

2

# Common "Intuition"... Sticky, low beta deposits $\Rightarrow$ Dur < 0

Silicon Valley Bank is not unusual in relying on the stability of its deposits. In an influential paper, Dreschler, Savoy, and Schnabl (2021) demonstrate that profits from the deposit spread have been a remarkably good hedge for interest-rate risk for US banks. Their analysis shows that deposit rates are quite inelastic to market interest rates, so that an increase in market rates leads to an increase in deposit *spreads.* Banks build their business plans around this relationship, using marketing, branch networks, and personal service to maximize the stability of their deposit base. We can think of the net present value of this deposit spread like an additional asset for banks, the "franchise value of deposits," but one that is never included in any formal balance sheets. When interest rates rise, the deposit spread increases and this franchise value goes up, but not even "mark-to-market" accounting will capture this change.

# Takeaways

- Sticky, low beta deposits do not hedge interest rate risk
- Bank franchise value arises from both deposits and loans... and has positive, not negative, duration
- In 2022-3, bank valuations fell due to
  - Securities Losses: -4.5% Assets
  - Franchise Losses: -1.5% Assets
- Sufficient franchise value remains to support the long-run solvency of most banks

# Conceptual Framework

1-70

T(X)= 11m (A 140

= 11m x2+2xh

= 11m 2x4+ 12 h=0 2x4+ h2

lim



Franchise Value = PV (Total Spread – Franchise Costs)

# Solvency and Run Risk

• Bank solvency as an ongoing concern:

Book Equity 
$$+ MTM_{Sec} + PV(S-C) > 0$$
  
 $+ Hedge?$ 

• Short-term run risk:

Multiple Equilibria when both hold

Book Equity 
$$+ MTM_{Sec} + MTM_{L} - \theta L < 0$$
  
Jiang et al.

# Deposit Spreads

• Suppose:  $r_t^D = -\alpha^D + \beta^D r_t^*$ fixed floating Spread  $\uparrow$ with r• Deposit spread:  $S_t^D = D(\alpha^D + (1 - \beta^D) r_t^*)$ 

- Floating value:  $PV(D(1-\beta^D)r_t^*) = D(1-\beta^D)$
- Floating rate ⇒ trades at par
- Zero duration
- :. Deposit Beta does not directly impact duration

# Deposit Franchise Value

- Deposit Franchise Costs:  $c^D$  per deposit
- Deposit Franchise Value:

$$PV\left(D\left(\alpha^{D}+\left(1-\beta^{D}\right)r_{t}^{*}-c^{D}\right)\right)=D\left(\frac{\alpha^{D}-c^{D}}{r_{t}^{\infty}}+\left(1-\beta^{D}\right)\right)$$

Duration +/- depending on whether fixed spread > franchise costs

# General Model: Term Deposits

• Fraction  $\lambda$  in ST accounts,  $1 - \lambda$  in *T*-period deposits, yield  $y^T$ 

$$r_t^D = -\alpha^D + \lambda \beta_1^D r_t^* + (1 - \lambda) \left[ \frac{1}{T} \sum_{j=1}^T \beta_T^D y_{t-j}^T \right]$$
$$= -\alpha^D + \left[ \lambda \beta_1^D + (1 - \lambda) \beta_T^D \right] r_t^* + (1 - \lambda) \beta_T^D \left[ \frac{1}{T} \sum_{j=1}^T \left( y_{t-j}^T - r_t^* \right) \right]$$
$$= -\alpha^D + \qquad \hat{\beta}_1^D r_t^* \qquad + \qquad (1 - \lambda) \beta_T^D \ell_t^T$$

## **Deposit Franchise Value: Implementation**

• Deposit Spread:  $S_t^D = D(r_t^* - r_t^D)$ 

• Let 
$$d = D/A$$
:  $s_t^D = \frac{S_t^D}{A_t} = \left[ \underbrace{d\alpha^D + d\left(1 - \hat{\beta}_1^D\right)}_{\phi_1^D} r_t^* \underbrace{-d\left(1 - \lambda\right)\beta_T^D}_{\phi_T^D} \ell_t^T \right]$ 

• Then Deposit Franchise Value =

$$A\left[\frac{\phi_0^D - c^D}{r_t^{\infty}} + \phi_1^D + \phi_T^D PV(\ell_t^T)\right]$$

# Total Franchise Value

• Loan rate modeled similarly: 
$$r_t^L = \alpha^L + \hat{\beta}_1^L r_t^* + (1 - \lambda) \beta_T^L \ell_t^T$$

• Value and sum with deposit franchise value:

$$PV(S-C) = A\left[\frac{\phi_0 - c}{r_t^{\infty}} + \phi_1 + \phi_T PV(\ell_t^T)\right] \approx \mathbf{0}$$

*c*)

where 
$$\phi = \phi^{D} + \phi^{L}$$
  
 $\approx \operatorname{sign}(\phi_{0} - c)$ 



# Data

- U.S. Call Reports. Data from 1984Q1 to 2021Q2
  - We exclude banks that have the majority of their deposit liabilities in foreign offices.
  - We also exclude banks that obtain more than 30% of their interest income from credit cards.
  - We exclude the bottom 1% by assets.
- For banks that are publicly traded, we match the Call Report bank data to equity prices obtained from CRSP.

# Deposit and Loan Spreads

• Deposits 
$$r^{D} = \frac{\text{Interest expense on deposits}}{D}$$
  
• Loans:  $r^{L} = \frac{\text{Interest income on loans}}{L} - \rho$   
where  $\rho = \frac{\text{Credit Loss Provisions}}{L} \times \frac{Q(Loss)}{P(Loss)}$  Berndt et al. (2018)

• Spreads: 
$$s^{D} = \frac{D}{A} \left( r^{*} - r^{D} \right)$$
 and  $s^{L} = \frac{L}{A} \left( r^{L} - r^{*} \right)$ 

# Franchise Cost

- Conceptually, measures net operating costs associated with running the lending and deposit-taking business.
  - Tangible Non-Interest Expense
    - salaries
    - expenses on premises
    - other non-interest expenses (tech, marketing)
  - Minus: Deposit service charges
- Adjustment 1: Exclude expenses from other business income (such as brokerage, etc.)\*
- Adjustment 2: Deduct fee income from credit cards

# Empirical Analysis

# Aggregate Spreads



18

# Aggregate Deposit Spread Fit



# Aggregate Lending Spread Fit



# Aggregate Spread Dynamics

	(1)	(2)	(3)	(4)	(5)
	Deposits	Deposits	Lending	Lending	Total
	Panel A: Regression in levels				
$r_t^*$	0.251	0.239	-0.069	-0.053	0.186
	(11.88)	(17.22)	(-3.03)	(-2.41)	(11.33)
$\ell_{\star}^2$		-0.195		0.159	-0.036
L		(-3.80)		(2.44)	(-0.60)
$\ell_{\star}^{5}$		-0.069		0.147	0.078
° L		(-1.73)		(2.61)	(1.40)
Intercent	0.001	0.000	0 000	0.004	0.006
mercept	-0.001	(1, 02)	( [ (0, 0) ] )	(2,00)	$(\Gamma, c_1)$
	(-1.34)	(1.83)	(5.69)	(3.09)	(5.01)
$R^2$	79.18	95.10	14.86	75.41	83.16
Obs.	147	147	147	147	147

Bankloval					
DATIK LEVET		(1)	(2)	(3)	(4)
Estimates		$\phi_0$ fixed	$\phi_1$ float	$\phi_2$ term	$\phi_{\mathtt{5}}$ term
$(2001_{2}020)$		Panel A	: Regressio	on in levels	
$(2001^{-}2020)$	Deposit spread				
	mean	0.0019	0.25	-0.23	-0.22
	p50	0.0023	0.25	-0.23	-0.22
	s.d.	0.0029	0.13	0.096	0.13
			Loan sprea	ad	
	mean	0.018	-0.10	0.090	0.28
	p50	0.018	-0.098	0.093	0.29
	s.d.	0.0089	0.18	0.20	0.22
				_	
	Total spread				
	mean	0.020	0.15	-0.14	0.068
	p50	0.020	0.15	-0.13	0.070
	s.d.	0.0089	0.22	0.20	0.22



		Total spread	
	(1)	(2)	(3)
$r_t^*$	$0.166^{***}$	0.268***	$0.168^{***}$
	(0.009)	(0.015)	(0.009)
$r_t^{*2}$		$-2.069^{***}$	
		(0.145)	
$\max(\Delta r_t^*, 0)$			$0.193^{***}$
			(0.018)
$\min(\Delta r_t^*, 0)$			0.068***
			(0.004)
$l_t^2$	$-0.132^{***}$	$-0.150^{***}$	$-0.094^{***}$
	(0.004)	(0.003)	(0.006)
$l_t^5$	0.077***	0.080***	0.056***
U C	(0.008)	(0.008)	(0.007)
Bank FE	Yes	Yes	Yes
Obs.	380,376	380,376	380,376
No. of banks	4,834	4,834	4,834
$\operatorname{Adj-}R^2$	0.8873	0.8874	0.8873

# Nonlinearities:

# Bank Franchise Value Estimates (2021)



# Comparison to Market Values (2021)



Asset  $M / B = 1 + \frac{(1 - \tau)(MTM_{sec} + PV(S - C)) - \tau \text{ Book Equity}}{A}$ 

# Losses: Bank's View vs Actuals vs Model

#### • 2021 BHC 10K

- + market value change for +1% shift in yield curve
- Despite security duration
- Actuals: 2021-23
  - Bank values fell
  - Security duration  $\uparrow$  decline
- Our model (all banks)
  - Securities  $\downarrow$  4-5%
  - Franchise value  $\downarrow$  1-1.5%



Determinants of Total Security Duration

	(1)	(2)	(3)
Fixed FV component	-0.636	-0.139	-0.141
	(-6.12)	(-1.55)	(-1.56)
Floating FV component		3.151 (15.99)	3.144 (15.95)
Log tangible assets			-0.052 (-2.74)
Intercept	2.177	1.713	2.373
	(70.23)	(51.93)	(9.64)
R <sup>2</sup>	0.01	0.09	0.09
Obs.	3772	3772	3772

# Security Holdings & Duration



- Total Securities Duration largely driven by floating spread
- Low deposit beta banks *take on* interest rate risk
- Why?
  - Deposit "bucketing"?
  - NIM hedging?

### Remaining Franchise Value Exceeds Losses

 Banks with higher security losses

... tended to have higher floating spreads (low deposit betas)

... and thus have similar remaining franchise value



Most banks remain solvent as ongoing concerns



# Conclusions

- Banks with sticky, low beta deposits hold more long-term securities, which
  - stabilizes NIM
  - improves *regulatory* interest rate risk (EVE)
  - But increases *actual* duration
- Deposit + Lending Franchise
  - Has positive duration (but << loan duration)
- In 2022-3, bank valuations fell due to
  - Securities Losses: -4.5% Assets
  - Franchise Losses: -1.5% Assets

#### . . . . . . . . .

......

••••

# Appendix

32

# Motivation 1: Deposit Runoff?

- Regulatory guidance
  - Treat non-maturing deposits based on "avg. life" assumption
  - E.g. 10-year runoff
- Floating Franchise Value:

 $\phi_1\left(\frac{r}{r+\delta}\right)$ 

where  $\delta$  is the "runoff rate"

• Floating Duration

$$Dur\left[\phi_1\left(\frac{r}{r+\delta}\right)\right] = -\frac{\delta/r}{r+\delta}$$

• E.g. 
$$r$$
 = 3%,  $\delta$  = 9%  $\Rightarrow$  -25 yrs

- With  $\phi_1 \approx 16\%$ 
  - 1% rise in rates

 $\Rightarrow$  1% increase Bank Value (Assets)

Hedge: 20% securities x 5 yr duration ... But this calculation is fundamentally incorrect (no *net* runoff)

# FDIC Guidance for EVE

#### **Decay Rate Example**

Г	Scenario	PV of Deposits at 20% Decay Rate	PV of Deposits at 50% Decay Rate	
	Up 300 bps	\$83	\$93	
	Base Case	\$89	\$96	
	Down 100 bps	\$90	\$97	

- Reflects the impact of deposit decay rates and average life assumptions on EVE results
- Illustrates a sensitivity analysis of a critical assumption
- Is the NMD deposit premium reasonable given customer behavior and deposit lives?

Notes: Book Value = \$100. Beta in Up 300 bps scenario: 25%. Beta used in Down 100 bps scenario: 75%. Dollar figures in thousands.

FEDERAL DEPOSIT INSURANCE CORPORATION

# DSS (2023), DSSW (2023)

"sticky").<sup>3</sup> Based on the FDIC study, a reasonable estimate is that they remain in the bank for T = 10 years on average. The value of the deposit franchise in this case is equal to the value calculated above minus the present discounted terminal value beyond T years:

$$DF = DF^{\infty} - \frac{DF^{\infty}}{(1+r^{p})^{T}} = D \times (1-\beta - c/r^{p}) \times \left[1 - \frac{1}{(1+r^{p})^{T}}\right].$$

# Motivation 2: Cash Flow (NIM) Hedging?

• Suppose all security holdings are floating rate

$$CF = (1-d)r^* + (s-c)$$
$$= \underbrace{(1-d+\phi_1)}_{\text{Total Exposure}}r^* + (\phi_0 - c)$$

- To hedge cash flow exposure to interest rates:
- ⇒ Swap floating-rate securities for fixed-rate securities
- With 10% equity and  $\varphi_1\approx 15\%$
- ⇒ Hedge with 25% long-term fixed-rate securities

Matches population mean (≈ 26%) ... But also *increases* bank duration risk (BPS 2015)





![](_page_37_Figure_0.jpeg)

FIGURE C.2

Securities Holdings and Floating Sensitivity  $\phi_1$ , Subsample Analysis

# THE END

![](_page_38_Picture_1.jpeg)