

# LABOR MARKET SHOCKS AND MONETARY POLICY

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*The views expressed here are those of the authors and do not necessarily reflect the views of the Federal Reserve Bank of St. Louis or Bank of Canada.*

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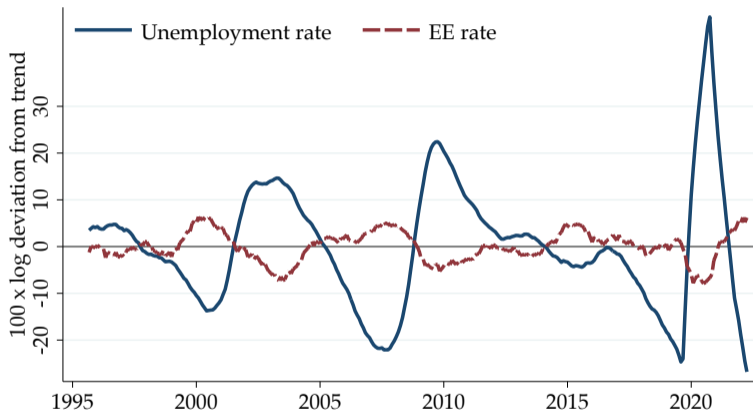
Moscarini and Postel-Vinay (2019), Faccini and Melosi (2022), Alves (2019)
- U.S. employer-to-employer (EE) transition rate is procyclical and persistent.
  - Important driver of **wage and productivity** growth.

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  - Important driver of **wage and productivity** growth.
    - Moscarini and Postel-Vinay (2017), Karahan et al. (2017), Haltiwanger et al. (2018), Faberman et al. (2022)
- Relative strength of wage vs productivity growth over the cycle can determine inflation.
  - Potential implications for monetary policy.

# COMOVEMENT OF UNEMPLOYMENT AND EE FLOWS



Weakening correlation between unemployment and EE rates between 2016–2019.

# QUESTIONS

1. **Positive:** How do fluctuations in EE flows affect inflation dynamics?
2. **Normative:** What is the optimal monetary policy accounting for EE dynamics?

## THIS PAPER

- Develop HANK model with frictional labor market and on-the-job search (OJS).
  - income risk cyclical and corr. with MPC. Acharya and Dogra (2020) and Patterson (2022)



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  - Document a significant weakening of  $\text{corr}(u, EE)$  post Great-Recession (2016–19).
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    - Labor market: direct (e.g. wage rebargaining), GE effect on tightness (e.g. labor demand).
- **Normative analysis:** Study optimal monetary policy within a class of Taylor rules.
  - Including the EE rate in the Taylor rule
    - reduces inflation and unemployment volatility.
    - provides non-monotonic welfare gains across worker productivity.

# ROADMAP

MOTIVATION

**MODEL**

SOLUTION

RESULTS

# OVERVIEW: HANK + LABOR SEARCH WITH OJS

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  - Experience **labor market transitions** over lifecycle with stochastic retirement and death.
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  - Labor service: **hire workers in a frictional labor market** and sell labor services at  $p_t^l$ . [Details](#)
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- Monetary authority controls nominal interest rate through Taylor rule. [Details](#)



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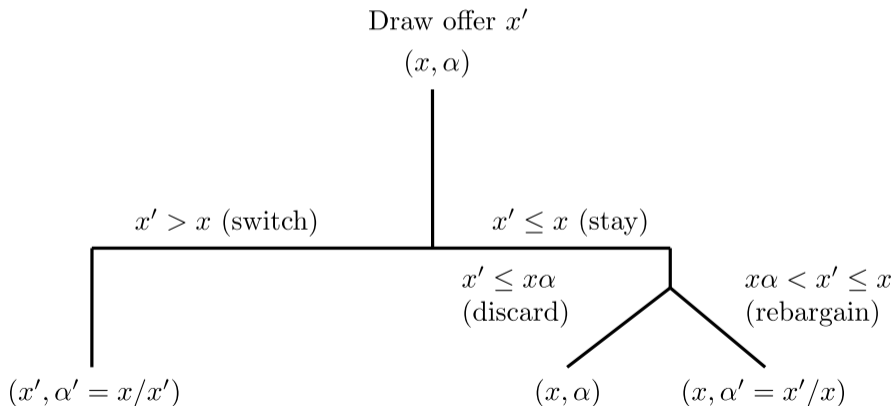
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- Wages  $w(h, x, \alpha)$ : Depend on skill  $h$ , match productivity  $x$ , and **bargained piece rate  $\alpha$** .

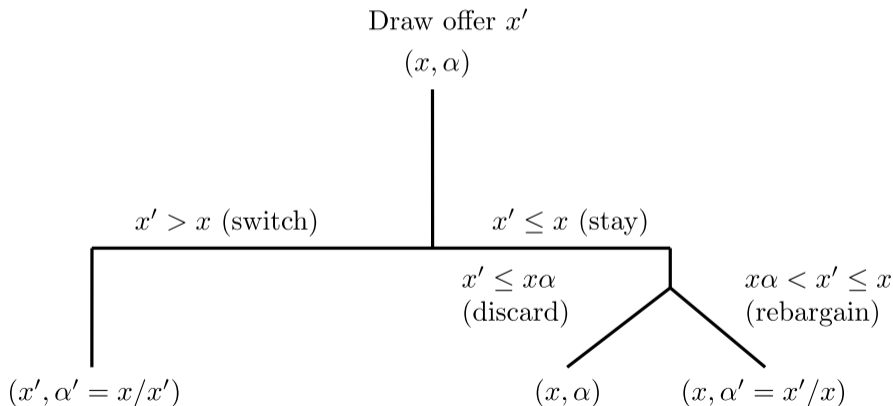
## WAGE DETERMINATION

- Wage is an **endogenous piece rate**  $\alpha$  of output  $F(h, x) = hx$ :  $w(h, x, \alpha) = \alpha\phi^E F(h, x)$ .
  - $\phi^E \in (0, 1)$ : maximum share of output a worker can receive with full piece rate  $\alpha = 1$ .
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More offers  $\Rightarrow$  More frequent EE or rebargaining  $\Rightarrow$  Price of labor services  $\Rightarrow$  Inflation



## SEARCH AND MATCHING

- Random search with worker and firm contact rates  $f(\theta)$  and  $q(\theta)$  per unit search efficiency.
  - Labor market tightness  $\theta = v/S$ : Ratio of vacancies to aggregate effective search.

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- Vacancy creation: Service firm
  - Labor service firms take into account entire distribution of workers when posting vacancies
- Worker-firm match terminates due to:
  - (exogenous) job separation shock.
  - (exogenous) retirement.
  - (endogenous) worker quitting to take another job.

# ROADMAP

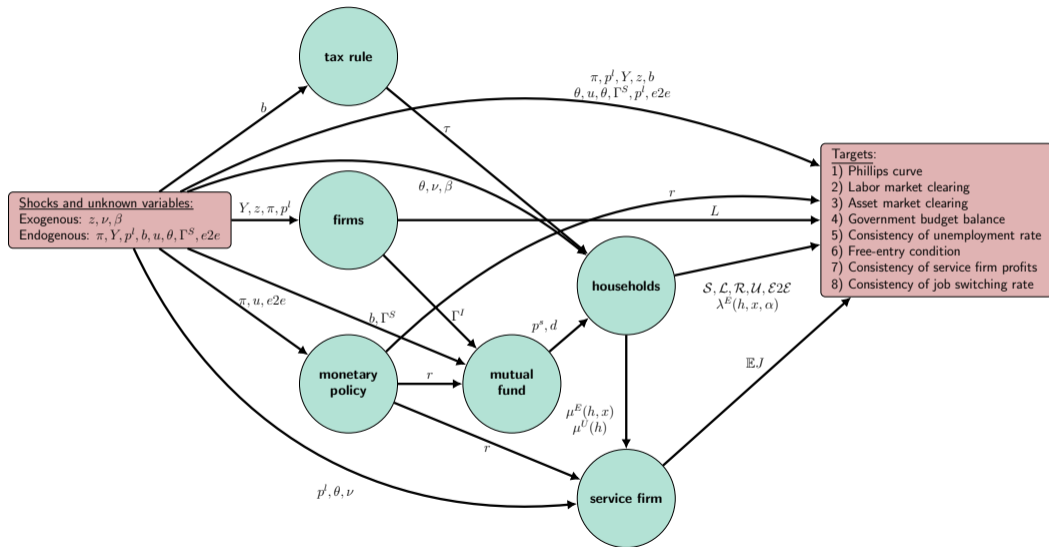
MOTIVATION

MODEL

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# DIRECTED ACYCLIC GRAPH (DAG) MODEL REPRESENTATION



**Solution:** Sequence-space Jacobian method (Auclert et al., 2021) + worker distribution

[Details](#)

# ROADMAP

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# Positive Analysis

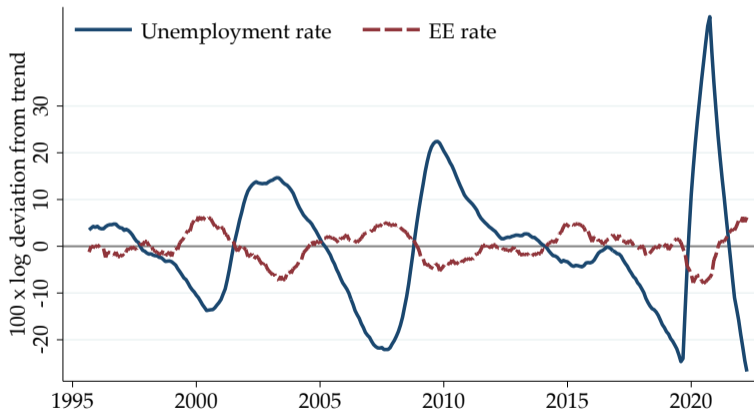
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Post-Great Recession Case Study

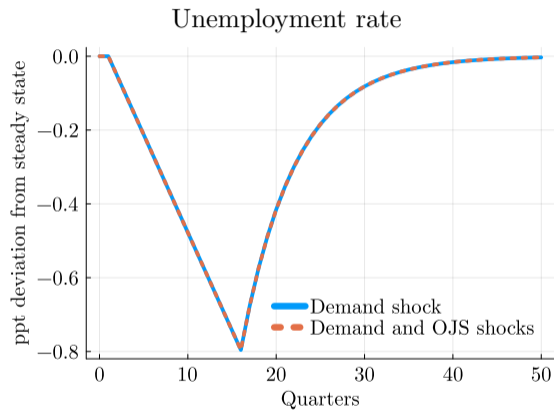


## MISSING $\text{corr}(u, EE)$ POST-GREAT RECESSION

- How do labor market dynamics affect the comovement of inflation and unemployment?
- **Case study:** Significant weakening of  $\text{corr}(u, EE)$  post-Great Recession, 2016–19.

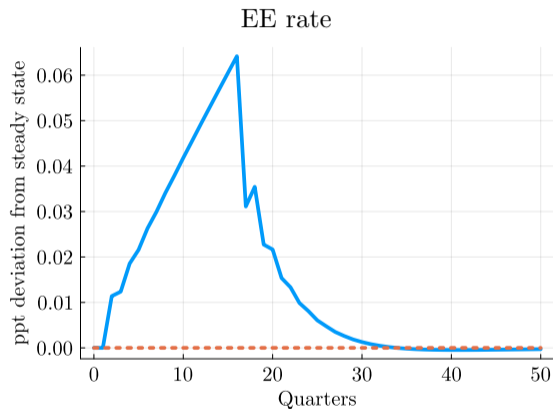
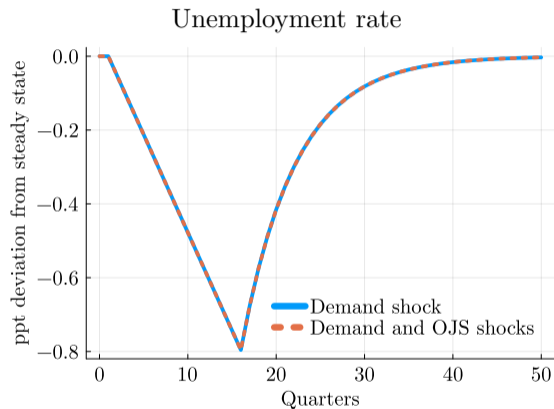


# LABOR MARKETS UNDER DEMAND AND OJS SHOCKS



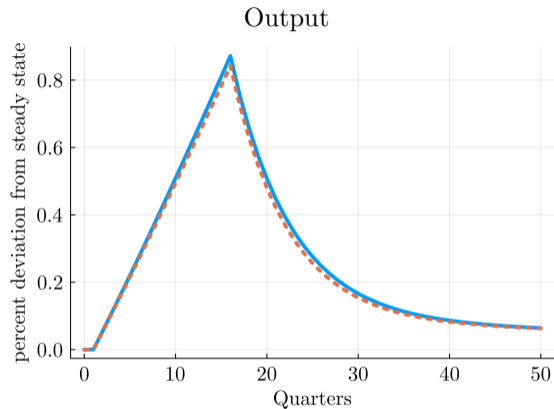
Common unemployment path,

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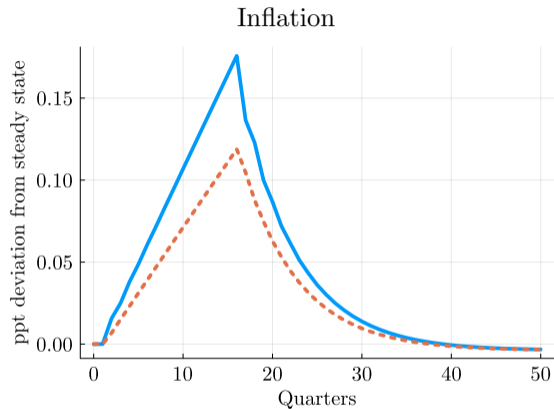
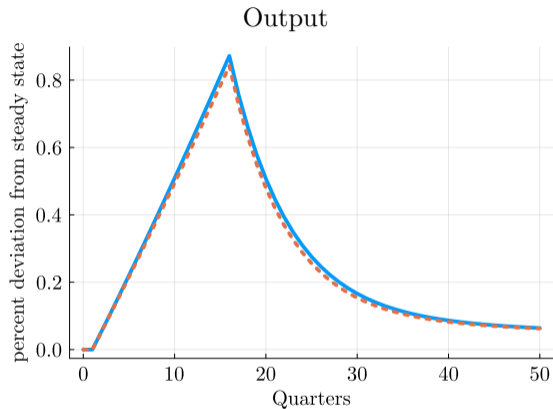
Common unemployment path, but different EE dynamics.

# INFLATION UNDER DEMAND AND OJS SHOCKS



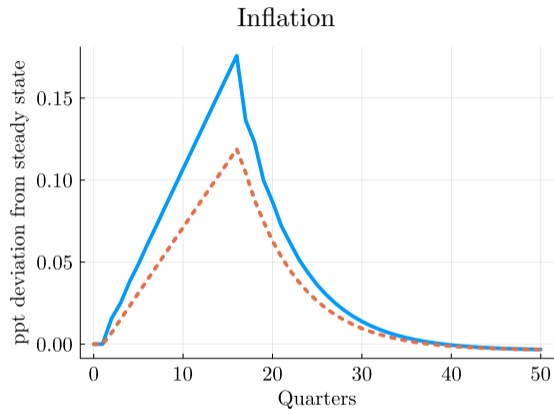
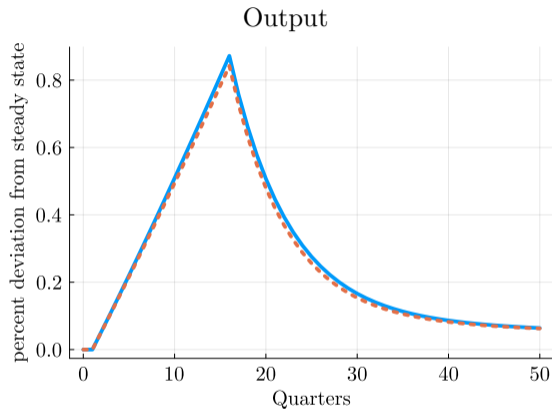
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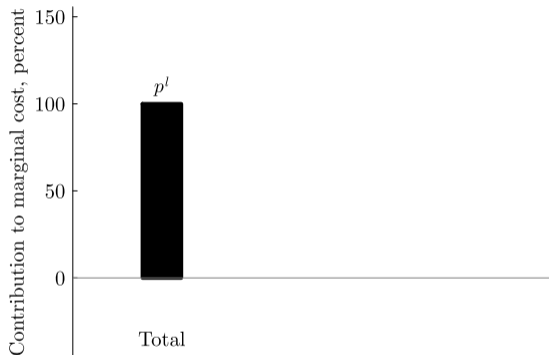
Identical unemployment and similar output dynamics, but muted inflation response.  
Annual inflation rate 0.23pp lower due to lower EE.

# Positive Analysis

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Decomposing Effects of OJS Shocks on Inflation

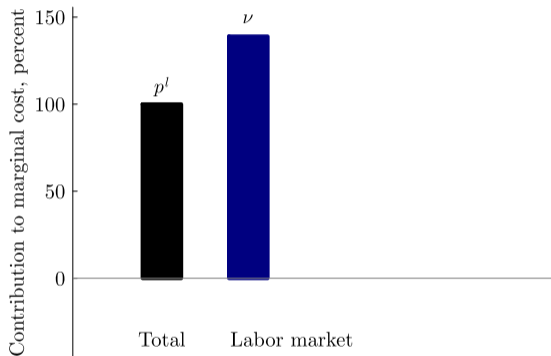
## DECOMPOSING EFFECTS OF OJS SHOCK ON INFLATION



NKPC implies that inflation  $\pi$  is driven by marginal cost  $p^l$  to a first order approximation.  
An increase in OJS efficiency  $\nu$  leads to an increase in  $p^l$ .

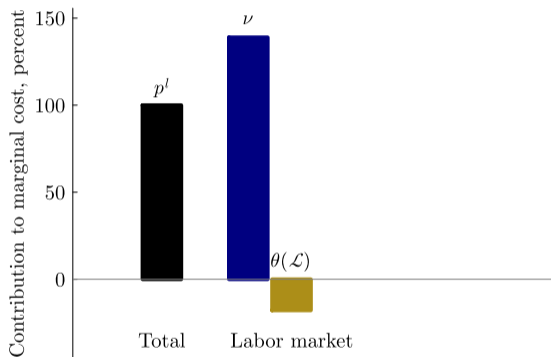


## DECOMPOSING EFFECTS OF OJS: LABOR MARKET



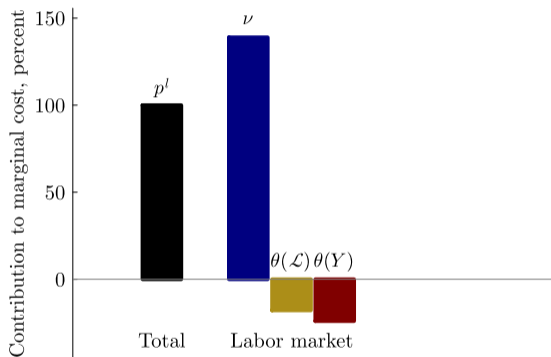
More frequent rebargaining and shorter matches lower expected match value.  
For free-entry to hold,  $p^l$  increases.

## DECOMPOSING EFFECTS OF OJS: LABOR MARKET



Improved productivity distribution raises supply of labor services.  
For labor market to clear,  $\theta$  decreases. For free-entry to hold,  $p^l$  decreases.

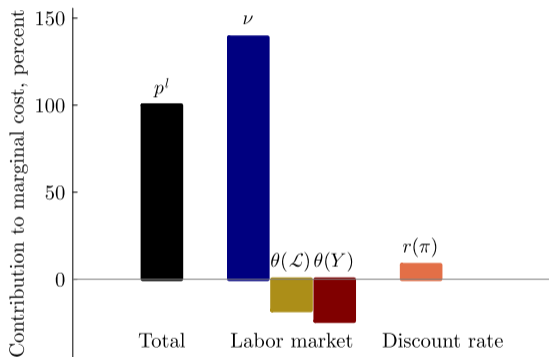
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Crowd-out increases  $u$ —reducing  $C$  and  $Y$ —and hence reduces demand for labor services.

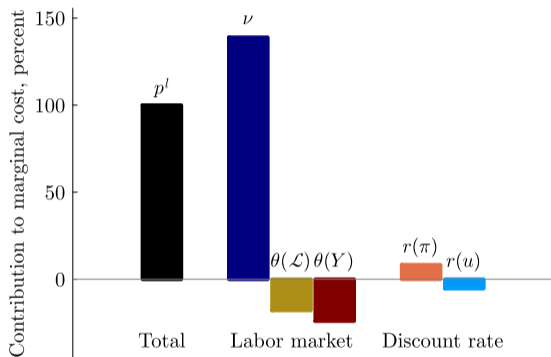
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# DECOMPOSING EFFECTS OF OJS: DISCOUNT RATE



Inflation rises in equilibrium, which increases  $r$  through MP.  
For free-entry to hold,  $p^l$  increases.

# DECOMPOSING EFFECTS OF OJS: DISCOUNT RATE



Unemployment rises in equilibrium, which reduces  $r$  through MP.  
For free-entry to hold,  $p^l$  decreases.

# HETEROGENEOUS CONSUMPTION RESPONSES TO HIGHER OJS

- PE: Results
  - positive consumption response stronger for wealth-poor among E but *wealth-rich* among U,
  - as raising current  $c$  upon shock affecting *future* income requires some wealth or income.

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  - due to lower dividends and share prices caused by an increase in real rate. Results
- **Implications for our quantitative results:** In a complete-markets model,
  - Aggregate consumption response would follow response of wealth-rich.
  - Overstatement of decline in aggregate demand leads to larger GE effect on tightness.
  - This would lead to smaller increase in marginal cost  $p^l$  and inflation.
  - Thus, we would attribute smaller role to job ladder shocks in explaining missing inflation.



# Normative Analysis

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Optimal Monetary Policy

# OPTIMAL MONETARY POLICY

- Under a central bank loss function

Yellen (2012), Debortoli et al. (2019)

$$\mathcal{W} = \text{var}(\pi_t - \pi^*) + \Psi \text{var}(Y_t - Y^*),$$

evaluate the performance of a generalized Taylor rule for  $\Phi_u$ ,  $\Phi_{EE}$  combinations:

Motivation

$$i_t = i^* + \Phi_\pi (\pi_t - \pi^*) + \Phi_u (u_t - u^*) + \Phi_{EE} (EE_t - EE^*).$$

- **Computational challenge:**

Details

- Each  $\Phi_u$ ,  $\Phi_{EE}$  combination corresponds to a new set of Jacobians.
- Costly in our model because Jacobians involve the worker distribution over many states.
- **Key:** Use *policy* shocks to compute IRFs to *structural shock* under alternative Taylor rule.

McKay and Wolf 2022

## OPTIMAL MONETARY POLICY

- Optimal MP prescribes  $\Phi_u^* = -3.18$  and  $\Phi_{EE}^* = 2.22$ . [More](#)
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  - volatilities of output, tightness, consumption, and price of labor services reduce to one-third,
  - volatilities of real interest rate and price of shares double. [Results](#)
- Ignoring job mobility dynamics, i.e.,  $\Phi_{EE} = 0$ , yields:
  - less aggressive response on unemployment gap  $\Phi_u = -2.71$
  - 12 percent higher central bank loss relative to optimal MP.

## HETEROGENEOUS WELFARE GAINS

- Non-monotonic welfare gains across match productivity distribution: Results
  - Low productivity workers gain from stable job ladder during recessions.
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  - Wealth-rich exposed to larger fluctuations in price of shares.
- Large welfare gains even among employed:
  - Employed workers benefit from improved job-ladder stability.
  - Unemployed workers, in addition, benefit from less severe downturns and faster recoveries.

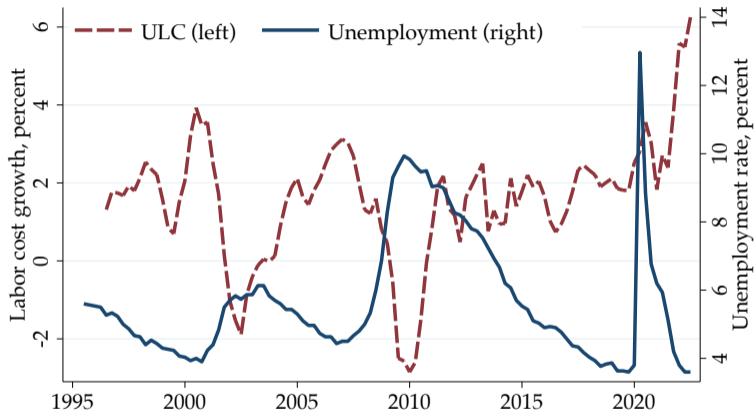


# CONCLUSION

- Develop a HANK model featuring a frictional labor market with on-the-job search.
- Analyze macro implications of an EE shock.
  - Quantify magnitude of missing inflation post-Great Recession to be 0.23pp.
  - Decompose channels through which an EE shock affects inflation.
- Evaluate monetary policy under a dual-mandate objective function.
  - Including EE rate in reaction function reduces overall inflation and unemployment volatility.
- **Future work:**
  - Heterogeneous labor market shocks.
  - Estimate model with and without labor market shocks and evaluate its performance.
  - Fiscal and monetary policy interactions accounting for rich labor market dynamics.

EXTRA SLIDES

# COMOVEMENT OF UNEMPLOYMENT AND LABOR COSTS



## RELATED LITERATURE

### 1. **Missing disinflation/inflation around Great Recession:**

Ball and Mazumder (2011), Coibon and Gorodnichenko (2015), Carvalho, Eusepi, Moench, and Preston (2017), Hazell, Herreno, Nakamura, and Steinsson (2020)

**This paper:** Quantify role of job mobility on inflation

### 2. **Effects of job mobility on inflation:**

*RANK*: Moscarini and Postel-Vinay (2019), Faccini and Melosi (2022); *HANK*: Alves (2019)

**This paper:** Rich labor market heterogeneity, decomposition, and optimal MP

### 3. **HANK with labor search:**

Ravn and Sterk (2016), Gornemann, Kuester, and Nakajima (2021)

**This paper:** Incorporate job mobility dynamics

### 4. **Computational methods:** Auclert, Bardoczy, Rognlie, and Straub (2021)

**This paper:** Incorporate discretized worker distribution into the SSJ method

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### **Final good firm:**

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- Operate linear technology using *labor services*  $l_t(j)$  to produce differentiated variety  $y_t(j)$ .
  - Production function is  $y_t(j) = z_t l_t(j)$  with aggregate productivity  $z_t$ .
  - Price of labor services  $p_t^l$  is determined in the labor market by worker flows.

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  - Price of labor services  $p_t^l$  is determined in the labor market by worker flows.
- Pricing subject to quadratic costs  $\Rightarrow$  New Keynesian Phillips Curve: Rotemberg (1982)

$$\frac{\log(1 + \pi_t - \pi^*)(1 + \pi_t)}{1 + \pi_t - \pi^*} = \vartheta \left( \frac{p_t^l}{z_t} - \frac{\eta - 1}{\eta} \right) + \frac{1}{1 + r_{t+1}} \frac{\log(1 + \pi_{t+1} - \pi^*)(1 + \pi_{t+1})}{1 + \pi_{t+1} - \pi^*} \frac{Y_{t+1}}{Y_t}.$$

# MONETARY AND FISCAL AUTHORITY

The central bank controls the short-term nominal interest rate following a Taylor rule:

$$i_t = i^* + \Phi_\pi (\pi_t - \pi^*) + \Phi_u (u_t - u^*).$$



# MONETARY AND FISCAL AUTHORITY

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$$i_t = i^* + \Phi_\pi (\pi_t - \pi^*) + \Phi_u (u_t - u^*).$$

The fiscal authority: Taxes

- Consumption tax  $\tau_c$ , income tax  $(\tau_t, \Upsilon)$ ,  $UI$ , pensions  $\phi^R$ , and exogenous spending  $G_t$ .
- Finances deficits by issuing nominal debt  $B_t$ . Budget Constraint

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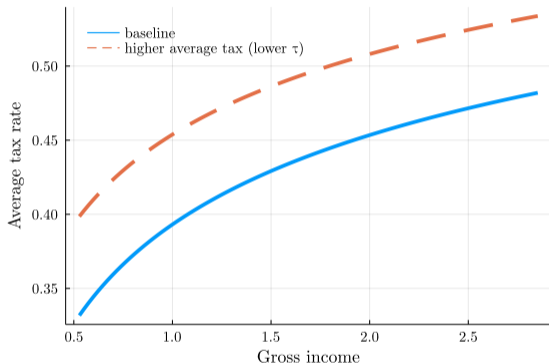
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Mutual fund: [Details](#)

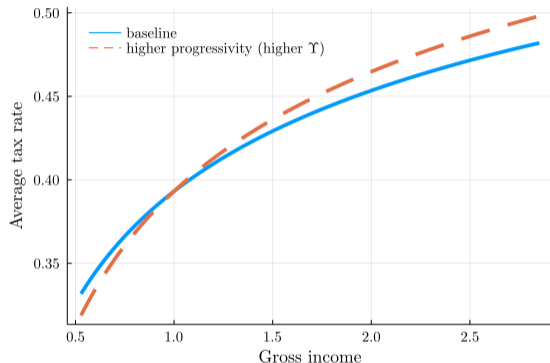
- Owns all firms and holds government debt.
- Issues shares and pays dividends.

# INCOME TAXES

## High average tax rate (low $\tau$ )



## High progressivity (high $\Upsilon$ )



$$\text{Net income} = \tau\omega^{1-\Upsilon} \Rightarrow \text{average tax rate} = 1 - \tau\omega^{-\Upsilon}$$

## GOVERNMENT BUDGET CONSTRAINT

$$\begin{aligned} B_{t-1} + G_t + P_t \int UI(h) d\lambda_t^U(s, h) + P_t \int \phi^R d\lambda_t^R(s) &= \frac{B_t}{1 + i_t} \\ &+ P_t \tau_c \int c(s, h, x, \alpha) d\lambda_t(s, h, x, \alpha) \\ &+ P_t \int (UI(h) - \tau_t UI(h)^{1-\Upsilon}) d\lambda_t^U(s, h) \\ &+ P_t \int (w(h, x, \alpha) - \tau_t w(h, x, \alpha)^{1-\Upsilon}) d\lambda_t^E(s, h, x, \alpha) \\ &+ P_t \int (\phi^R - \tau_t (\phi^R)^{1-\Upsilon}) d\lambda_t^R(s) \end{aligned}$$

- Consumption tax  $\tau_c$  and progressive income tax  $(\tau_t, \Upsilon)$ .
- Unemployment benefit  $UI(h)$ , retirement pension  $\phi^R$ , government expenditures  $G_t$ .
- Nominal debt  $B_t$ .
- $\lambda_t^X(\cdot)$  worker distribution over relevant states.
- Nominal price level  $P_t$ .

## MUTUAL FUND

- Owns intermediate and labor service firms, and all government bonds.
- Issues shares at price  $P^s$  and holds government bonds to earn a gross return of  $1 + i$ .
- No-arbitrage implies returns on stock and bonds are equalized:

$$\frac{P_{t+1}^s + D_{t+1}}{P_t^s} = 1 + i_t.$$

- Cannot retain any funds. All balances are distributed to share owners as dividends:

$$D_t = B_{t-1} - \frac{B_t}{1 + i_t} + P_t \Gamma_t^I + P_t \Gamma_t^S,$$

where  $\Gamma^I$  and  $\Gamma^S$  are per-period real profits of intermediate and service firms:

$$\Gamma_t^I = \left( 1 - \frac{p_t^l}{z_t} - \frac{\eta}{2\vartheta} \log(1 + \pi_t - \pi^*)^2 \right) Y_t$$
$$\Gamma_t^S = \int (p_t^l F(h, x) - w(h, x, \alpha)) d\lambda_t^E(s, h, x, \alpha).$$

# TIMING

1. **Aggregate shocks** are realized.
2. **Monetary authority** sets the nominal rate.
3. **Idiosyncratic shocks** are realized.
  - Life cycle and job destruction shocks.
  - Worker skills evolve.
4. **Labor search:** Service firms post vacancies, workers search, new matches are formed.
5. **Production:** Labor services, intermediate goods, and final goods are produced.
6. **Consumption:**
  - Profits are realized, wages, dividends and transfers are paid out.
  - Consumption-saving decisions are made.

## UNEMPLOYED WORKER

Value of unemployment:

$$V_t^U(s, h) = \max_{s' \geq 0, c} u(c) + \beta(1 - \psi^R) \mathbb{E}_{h'|h} [\Omega_{t+1}^U(s', h')] + \beta\psi^R V_{t+1}^R(s')$$
$$\text{s.t. } P_t c(1 + \tau_c) + P_t^s s' = P_t \tau_t UI(h)^{1-\gamma} + (P_t^s + D_t)s$$

- $\psi^R$ : Probability of retirement
- $V_t^R(s)$ : Value of retirement
- $UI(h)$ : Unemployment benefits
- $P_t$ : Price of final good
- $P_t^s$ : Price of mutual fund shares
- $D_t$ : Dividends

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Value of job search:

$$\Omega_t^U(s, h) = \zeta f(\theta_t) \mathbb{E}_x V_t^E(s, h, x, \underline{x}/x) + (1 - \zeta f(\theta_t)) V_t^U(s, h)$$

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## EMPLOYED WORKER

Value of employment:

$$\begin{aligned} V_t^E(s, h, x, \alpha) &= \max_{s' \geq 0, c} u(c) + \beta(1 - \psi^R) \mathbb{E}_{h'|h} \{ (1 - \delta) \Omega_{t+1}^E(s', h', x, \alpha) + \delta \Omega_{t+1}^U(s', h') \} \\ &\quad + \beta \psi^R V_{t+1}^R(s') \\ \text{s.t.} \quad &P_t c(1 + \tau_c) + P_t^s s' = P_t \tau_t w(h, x, \alpha)^{1-\Upsilon} + (P_t^s + D_t) s \end{aligned}$$

○  $\delta$ : Probability of match separation

○  $\nu$ : On-the-job search efficiency

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 \end{aligned}$$

Value of **on-the-job search**:

$$\begin{aligned}
 \Omega_t^E(s, h, x, \alpha) &= \overbrace{\nu f(\theta_t)}^{\text{Offer}} \mathbb{E}_{\tilde{x}} \left[ \max \left\{ \overbrace{V_t^E(s, h, \tilde{x}, x/\tilde{x})}^{\text{Switch}}, \overbrace{V_t^E(s, h, x, \max\{\alpha, \tilde{x}/x\})}^{\text{Stay-Discard offer or rebargain}} \right\} \right] \\
 &\quad + \underbrace{(1 - \nu f(\theta_t))}_{\text{No offer}} V_t^E(s, h, x, \alpha)
 \end{aligned}$$

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## RETIRED WORKER

Value of retirement:

$$V_t^R(s) = \max_{s' \geq 0, c} u(c) + \beta(1 - \psi^D)V_{t+1}^R(s')$$
$$\text{s.t. } P_t c(1 + \tau_c) + P_t^s s' = P_t \tau_t (\phi^R)^{1-\Upsilon} + (P_t^s + D_t)s$$

Retired only face mortality risk.

- $\psi^D$ : Probability of death
- $\phi^R$ : Retirement pensions
- $P_t^s$ : Price of mutual fund shares
- $D_t$ : Dividends

## LABOR SERVICE FIRMS

Value of matched firm: Details

$$J_t(h, x, \alpha) = p_t^l F(h, x) - w(h, x, \alpha) + \frac{1}{1 + r_{t+1}} (1 - \psi^R) (1 - \delta) \\ \times \mathbb{E}_{h'|h} \left\{ (1 - \nu f(\theta_{t+1})) J_{t+1}(h', x, \alpha) + \nu f(\theta_{t+1}) \int_{\underline{x}}^x J(h', x, \max\{\alpha, \tilde{x}/x\}) d\Gamma^x(\tilde{x}) \right\}$$

- $p_t^l$ : Price of labor services
- $r_t$ : Real interest rate
- $\kappa$ : Cost of posting vacancy
- $F(h, x) = hx$ : Match output
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Value of posting vacancy:

$$V_t = -\kappa + q(\theta_t) \frac{1}{S_t} \left[ \zeta \int_{s,h} \int_{\tilde{x}} J_t(h, \tilde{x}, \underline{x}/\tilde{x}) d\Gamma^x(\tilde{x}) d\mu_t^U(s, h) \right. \\ \left. + \nu \int_{s,h,x,\alpha} \int_x^{\bar{x}} J_t(h, \tilde{x}, x/\tilde{x}) d\Gamma^x(\tilde{x}) d\mu_t^E(s, h, x, \alpha) \right]$$

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Free-entry implies  $V_t = 0$ .

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# LABOR SERVICE FIRMS

- Post vacancies  $v$  at cost  $\kappa$  to hire workers in a frictional labor market.
  - Labor market tightness  $\theta = v/S$ , where  $S = \int \zeta d\mu^U(s, h) + \int \nu d\mu^E(s, h, x, \alpha)$ .
  - CRS matching function  $M(v, S)$  determines number of new worker-firm contacts.
  - Worker and firm contact rates,  $f(\theta) = \frac{M(v, S)}{S}$  and  $q(\theta) = \frac{M(v, S)}{v}$ , pinned down by  $\theta$ .
- Produce  $F(h, x) = hx$  labor services using one unit of labor.
- Sell labor services to intermediate firms in a competitive market at nominal price  $P^l$ .

## SOLUTION OF MODEL WITH AGGREGATE SHOCKS

Follow Auclert, Bardoczy, Rognlie, Straub (2021) to compute IRFs and model simulation.

1. Cast the model in sequence space for  $t \in \{0, \dots, T\}$  as a directed acyclic graph (DAG).
  - + simple blocks
  - + heterogeneous-agent (HA) block
2. For each block, compute partial Jacobians of each output with respect to each input.
  - o Automatic differentiation for simple blocks.
  - o Numerical differentiation for HA block (fake-news algorithm).
3. Forward accumulate partials along topological sort of DAG to get total derivatives.
4. Use implicit function theorem to get the GE response of endogenous variables to shocks.
5. The GE Jacobian is sufficient to compute IRFs to aggregate shocks.
6. Simulate the model subject to aggregate shocks (IRF  $\equiv$  MA).



# EXTERNALLY CALIBRATED PARAMETERS

Parameter	Explanation	Value	Reason
$\sigma$	Curvature in utility function	2	Standard
$\psi^R$	Retirement probability	0.00625	40 years of work stage
$\psi^D$	Death probability	0.0125	20 years of retirement stage
$\Delta h$	Skill appreciation/depreciation amount	0.275	Set
$\pi^E$	Skill appreciation probability	0.018	Wage growth for job stayers
$\xi$	Matching function elasticity	1.6	Set
$\zeta$	Search efficiency of the unemployed	1	Normalization
$\eta$	Elasticity of substitution	6	20 percent markup
$\vartheta$	Price adjustment cost parameter	0.021	Slope of Phillips curve, Gali and Gertler (1999)
$x_G$	Government spending/GDP ratio	0.19	Total net federal outlay/ GDP
$x_B$	Debt/GDP ratio	2.43	Total public debt/GDP
$\tau_c$	Consumption tax rate	0.0312	Sales tax receipt/consumption exp.
$\Upsilon$	Progressivity of income tax	0.151	Heathcote et al. (2014)
$\rho_\tau$	Responsiveness of income tax to debt level	0.10	Auclert et al. (2020)
$\pi^*$	Steady-state inflation rate	0.00496	2% annual inflation rate
$\Phi_\pi$	Responsiveness of interest rate to inflation	1.5	Taylor (1993) and Gali (2015)
$\Phi_u$	Responsiveness of interest rate to unemployment	-0.25	Taylor (1993) and Gali (2015)

# INTERNALLY CALIBRATED PARAMETERS

Parameter	Explanation	Value	Target	Data	Model
$\beta$	Discount factor	0.981	Fraction with non-positive liquid wealth	0.16	0.11
$\kappa$	Vacancy creation cost	0.670	Unemployment rate	0.051	0.052
$\delta$	Job separation probability	0.091	EU rate	0.038	0.033
$\nu$	Search efficiency of employed	0.108	EE rate (w/o non-employment spell)	0.02	0.02
$\pi^U$	Skill depreciation probability	0.022	Earnings drop upon job loss	-0.35	-0.36
$\sigma_x$	Standard deviation of match productivity	0.063	Wage growth of job switchers	0.09	0.09
$\phi^E$	Maximum share of output as wages	0.823	Labor share	0.67	0.74
$\phi^U$	UI replacement rate	0.385	UI replacement rate	0.40	0.44
$\phi^R$	Retirement benefit amount	0.473	Retirement income/labor income	0.34	0.41

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## ESTIMATION OF SHOCKS

- Estimate AR(1) processes for discount factor  $\beta$ , productivity  $z$ , OJS efficiency  $\nu$ .
- Target autocorrelations and standard deviations of  $Y$ ,  $u$  and  $EE$ .

	Data			Model		
	Std. Dev	Autocorr.	Corr. w/ $Y$	Std. Dev	Autocorr.	Corr. w/ $Y$
$Y$	0.024	0.963	1	0.005	0.924	1
$u$	0.148	0.953	-0.882	0.092	0.859	-0.882
$EE$	0.090	0.907	0.147	0.068	0.765	0.145
$\theta$	0.275	0.930	0.809	0.062	0.105	0.626
$\pi$	0.245	0.388	0.538	0.270	0.825	0.543

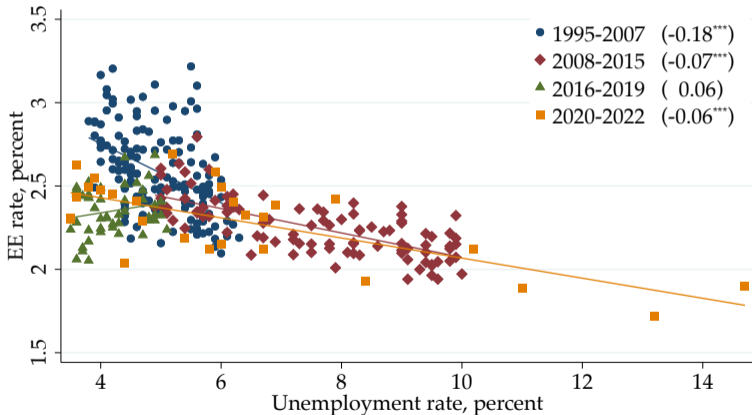
# VARIANCE DECOMPOSITION

	Share of variance explained by		
	$z$	$\nu$	$\beta$
$Y$	0.008	0.031	0.961
$u$	0.111	0.077	0.812
$EE$	0.070	0.787	0.143
$\theta$	0.337	0.046	0.618
$\pi$	0.049	0.431	0.520

Shock	$\rho$	$\sigma$
$z$	0.332	0.002
$\nu$	0.936	0.003
$\beta$	0.909	0.001

## MISSING $\text{corr}(u, EE)$ POST-GREAT RECESSION

- How do labor market dynamics affect the comovement of inflation and unemployment?
- **Case study:** Significant weakening of  $\text{corr}(u, EE)$  post-Great Recession, 2016–19.





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Goal: Quantify magnitude of “missing inflation” due to weakening  $\text{corr}(u, EE)$  in 2016–2019.

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**Economy 1:** *Counterfactual economy* — EE moves with unemployment

- Shocks to discount factor to match decline in unemployment post-Great Recession

$$\beta_t = (1 - \rho_\beta)\beta^* + \rho_\beta\beta_{t-1} + \varepsilon_{\beta,t}.$$

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**Economy 2:** *Post-Great Recession* — flat EE rate

- Shocks to discount factor to match decline in unemployment post-Great Recession

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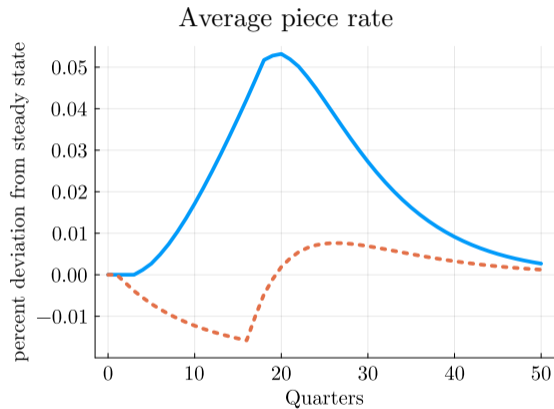
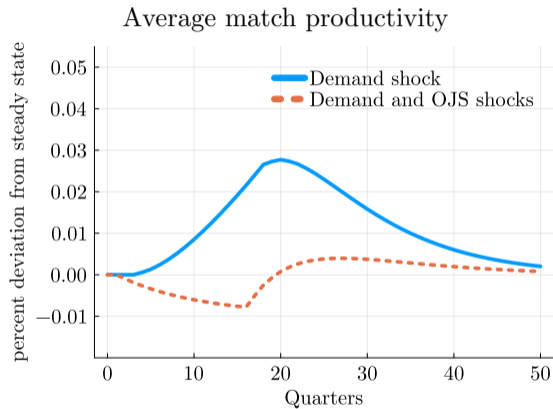
- Shocks to OJS efficiency to match path of EE rate

$$\nu_t = (1 - \rho_\nu)\nu^* + \rho_\nu\nu_{t-1} + \varepsilon_{\nu,t}.$$

## DETAILS ON MODEL SIMULATION

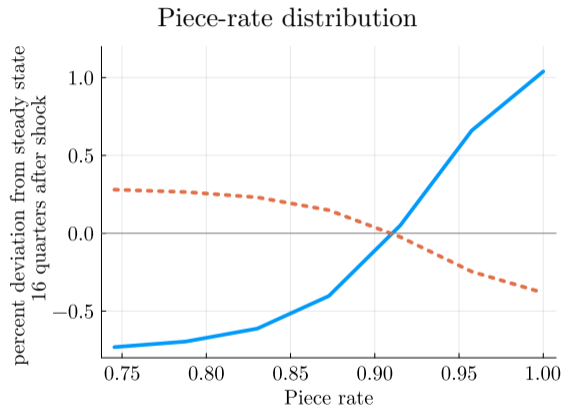
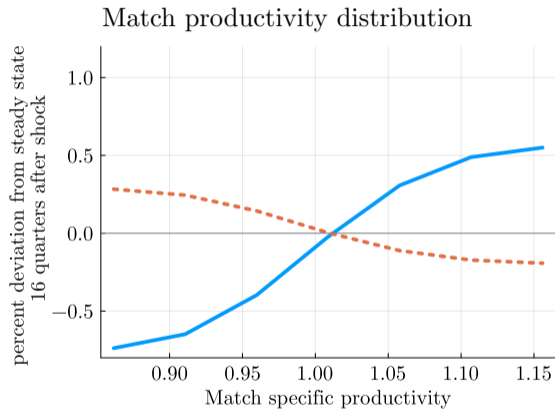
- Targets over transition horizon  $t \in \{0, \dots, T\}$ :
  1. Path of unemployment rate during post-Great Recession:
    - 15% decline by  $\bar{T} = 16$  quarters and revert back to steady state with
$$u_t = (1 - \rho_u)u^* + \rho_u u_{t-1}, \quad \text{where } \rho_u = 0.85.$$
  2. Path of EE rate during post-Great Recession:
    - Remain at steady state level of EE rate despite declining unemployment rate.
- Two economies:
  1. Economy 1: positive demand shocks
    - Shocks modeled as innovations to discount factor  $\beta$ .
    - Assume at each  $t = 0, \dots, T$ , shock  $\varepsilon_\beta < 0$  hits economy.
  2. Economy 2: positive demand and negative OJS shocks
    - Shocks modeled as innovations to discount factor  $\beta$  and OJS efficiency  $\nu$ .
    - Assume at each  $t = 0, \dots, T$ , shocks  $\varepsilon_\beta < 0$  and  $\varepsilon_\nu < 0$  hit economy.

# AVERAGE MATCH PRODUCTIVITY AND PIECE RATE



Negative OJS efficiency shocks limit the rise in average  $x$  and  $\alpha$ .

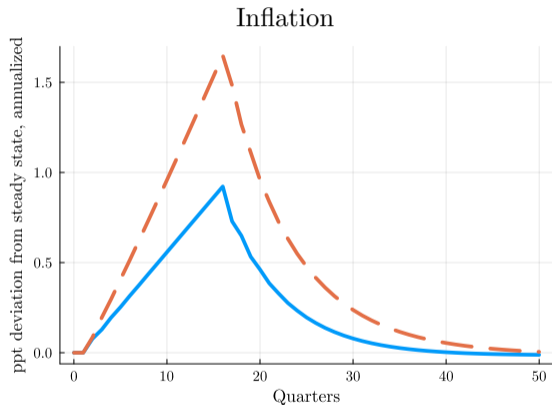
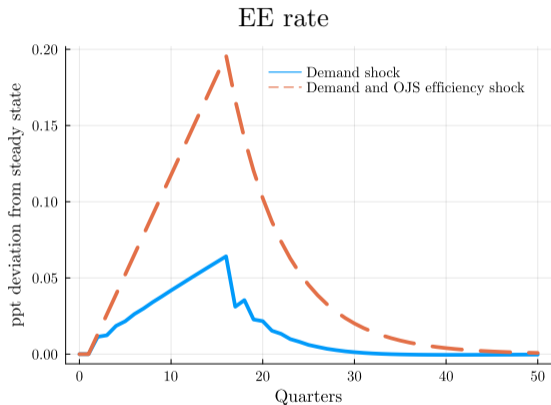
# DISTRIBUTION OF MATCH PRODUCTIVITY AND PIECE RATE



Negative OJS efficiency shocks leads to leftward shifts in distributions of  $x$  and  $\alpha$ .

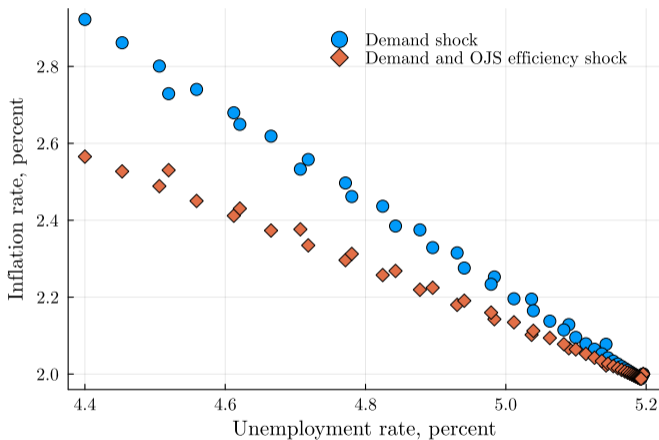


# COVID RECOVERY: “THE GREAT REALLOCATION”



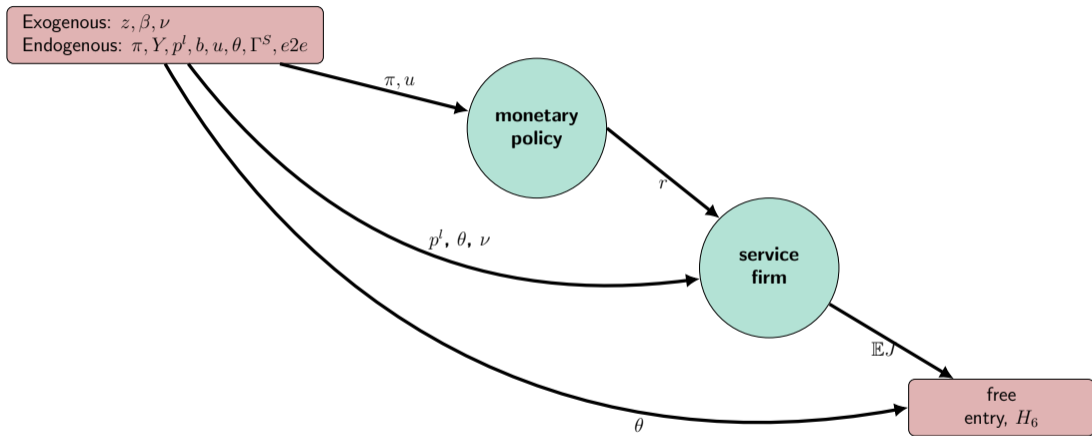
Higher EE and higher inflation.

# PHILLIPS CURVE UNDER DEMAND AND OJS SHOCKS

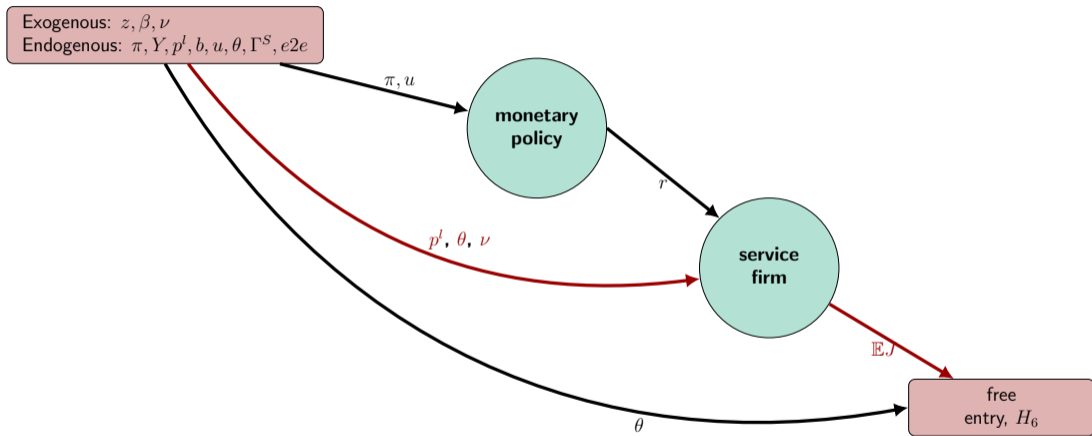


Flatter Phillips curve under negative OJS efficiency shocks.

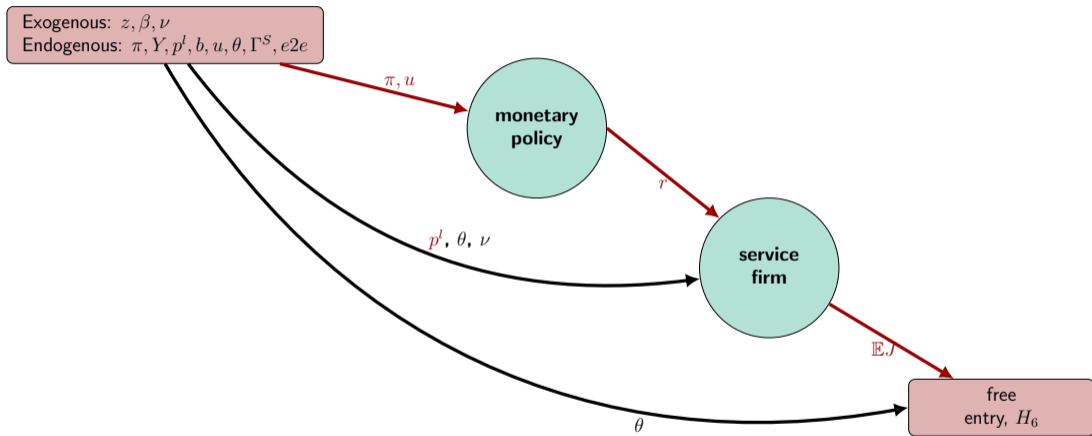
# DECOMPOSING EFFECTS OF OJS SHOCK ON INFLATION



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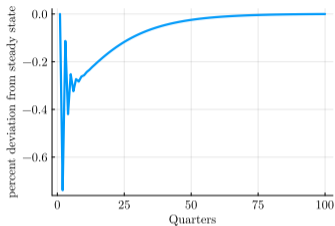


## DETAILS FOR INFLATION DECOMPOSITION

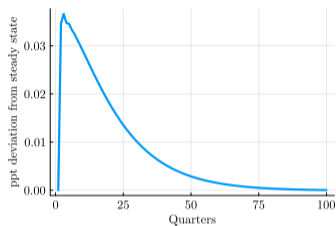
1. Start from total Jacobians of a block of interest, e.g., H6 (free-entry condition).
2. Apply IFT to H6 to get the derivative of  $p^l$  w.r.t. endogenous and exogenous variables.
3. Multiply the total derivative of  $p^l$  with GE IRFs of variables w.r.t  $\nu$ .
4. This gives the response of  $p^l$  components  $\nu$ ,  $\theta$ ,  $\pi$ ,  $u$  w.r.t  $\nu$  (direct and indirect).
5. Can further decompose these components, e.g.,  $\theta$  using other related blocks, e.g., H2.

# GE EFFECTS OF $\nu$ ON MODEL OUTCOMES

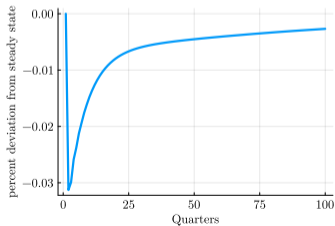
## Tightness



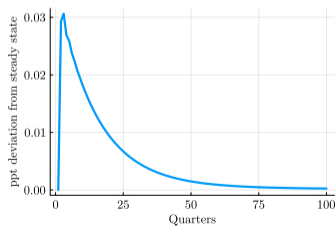
## Unemployment



## Output



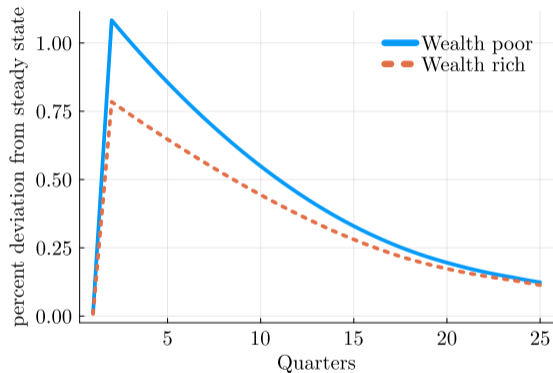
## Inflation



Impulse responses to a unit increase in  $\nu$ .

# HETEROGENEOUS CONSUMPTION RESPONSES

Consumption of employed: PE

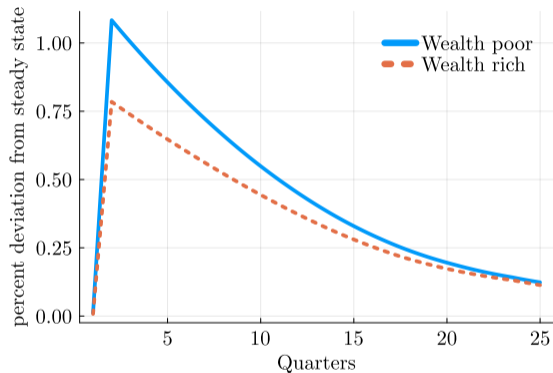


Higher future income raises consumption,

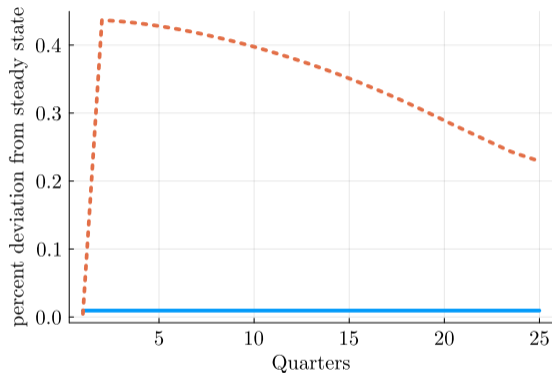


# HETEROGENEOUS CONSUMPTION RESPONSES

Consumption of employed: PE



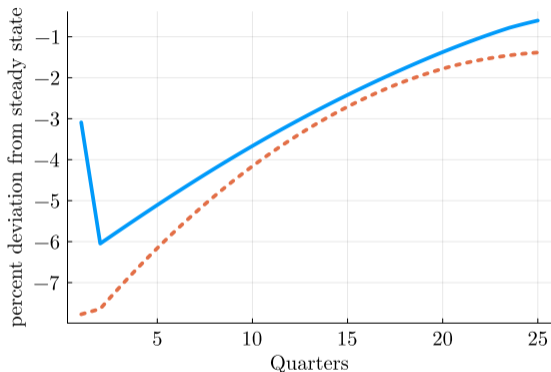
Consumption of unemployed: PE



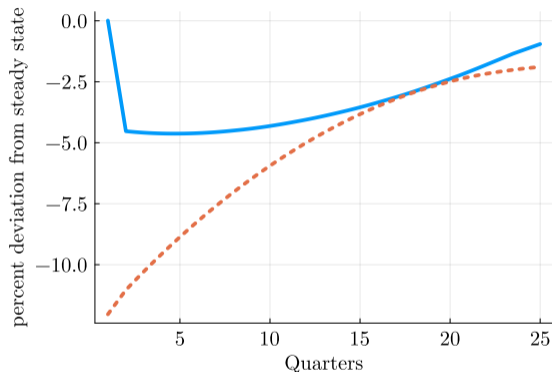
Higher future income raises consumption, except for wealth-poor unemployed

# HETEROGENEOUS CONSUMPTION RESPONSES

Consumption of employed: GE



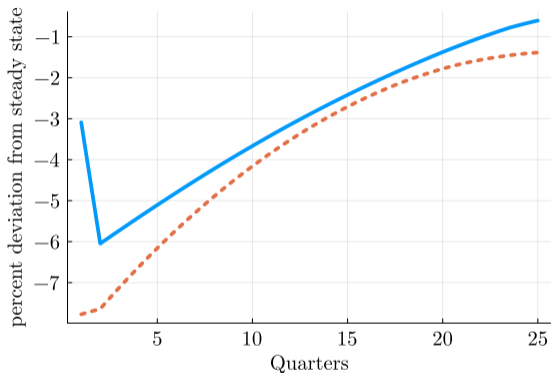
Consumption of unemployed: GE



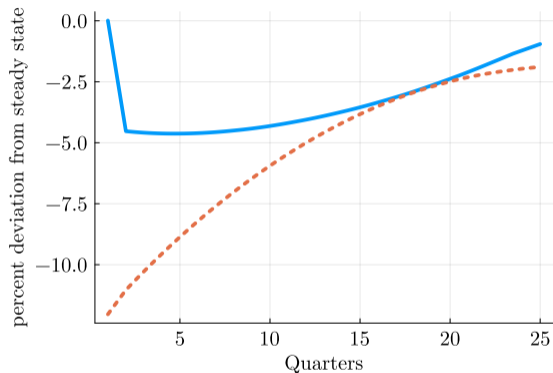
In GE, consumption declines due to real rates.  
Decline more prominent for wealth-rich due to lower dividends and share prices.

# HETEROGENEOUS CONSUMPTION RESPONSES

Consumption of employed: GE



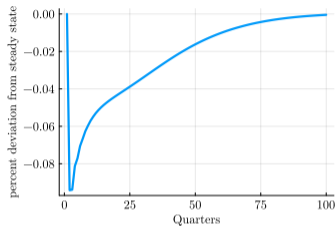
Consumption of unemployed: GE



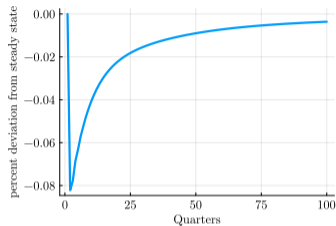
Complete markets would overstate aggregate demand decline.

# GE EFFECTS OF $\nu$ ON MODEL OUTCOMES

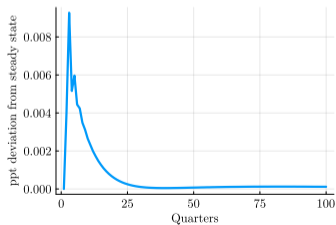
## Real dividends



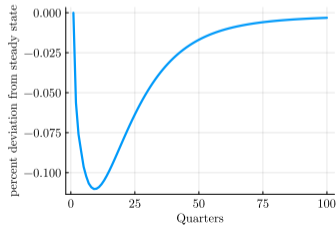
## Real share price



## Real interest rate



## Real total firm profits



Impulse responses to a unit increase in  $\nu$ .

# MONETARY POLICY

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- **Our claim:**
  - Unemployment rate is not a sufficient statistic to gauge the health of the labor market.
  - Including EE rate in the reaction function improves inflation and unemployment stability.
- **Agenda:** Study monetary policy under a dual-mandate central bank objective function.



## EVALUATING ALTERNATIVE TAYLOR RULES

- Use *policy* shocks to compute IRFs to *non-policy shocks* under alternative Taylor rules.
  - **Key:** Firms and households do not care about the systematic component of monetary policy, but care about the current and future path of interest rates. McKay and Wolf (2022)
  - No need to recompute Jacobians. Derivatives under the baseline policy are enough.
- Solving the system for policy news shocks  $\boldsymbol{\mu} = \{\mu_t\}_{t=1}^T$  given non-policy shock  $\varepsilon$

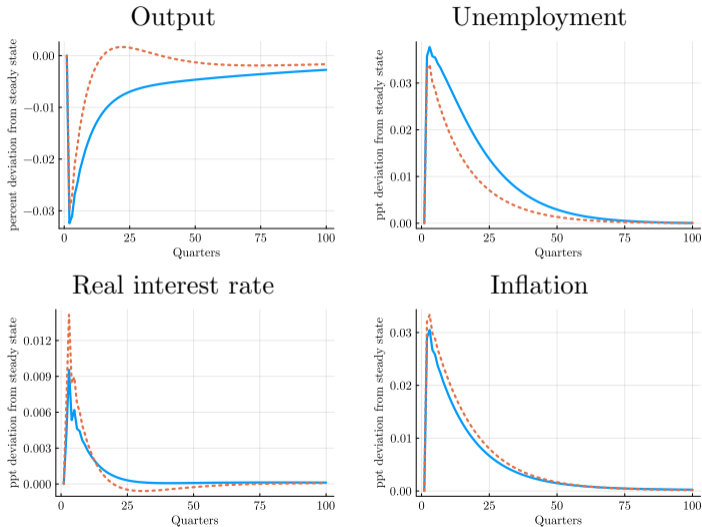
$$\underbrace{\mathbf{i}_{\Phi_\pi, \Phi_u}(\varepsilon) + \Theta_{\Phi_\pi, \Phi_u}^{i, \mu} \boldsymbol{\mu}}_{\text{IRF of } i \text{ under baseline}} = \underbrace{\tilde{\Phi}_\pi \left( \boldsymbol{\pi}_{\Phi_\pi, \Phi_u}(\varepsilon) + \Theta_{\Phi_\pi, \Phi_u}^{\pi, \mu} \boldsymbol{\mu} \right)}_{\text{IRF of } \pi \text{ under baseline}} + \underbrace{\tilde{\Phi}_u \left( \mathbf{u}_{\Phi_\pi, \Phi_u}(\varepsilon) + \Theta_{\Phi_\pi, \Phi_u}^{u, \mu} \boldsymbol{\mu} \right)}_{\text{IRF of } u \text{ under baseline}}$$

$$+ \underbrace{\tilde{\Phi}_{EE} \left( \mathbf{EE}_{\Phi_\pi, \Phi_u}(\varepsilon) + \Theta_{\Phi_\pi, \Phi_u}^{EE, \mu} \boldsymbol{\mu} \right)}_{\text{IRF of } EE \text{ under baseline}},$$

allows for computing the IRF to  $\varepsilon$  under alternative Taylor rule  $\tilde{\Phi}_\pi, \tilde{\Phi}_u, \tilde{\Phi}_{EE}$ .

- IRF to  $\varepsilon$  under alternative rule  $\equiv$  IRF to  $\varepsilon$  and  $\{\mu_t\}_{t=1}^T$  under baseline rule.

# GE EFFECTS OF $\nu$ UNDER BASELINE VS OPTIMAL POLICY



Impulse responses to a unit increase in  $\nu$  under baseline (blue) and optimal (red) MP.

## OUTCOMES UNDER OPTIMAL POLICY

- Volatilities of macroeconomic outcomes under baseline and optimal policies: Results

	$\pi$	$Y$	$r$	$\theta$	$u$	$C$	$p^l$	$p^s$
Baseline Taylor rule	0.0013	0.0059	0.0019	0.0600	0.0047	0.0059	0.0203	0.1975
Optimal Taylor rule	0.0011	0.0020	0.0033	0.0175	0.0013	0.0020	0.0081	0.3051

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- Heterogeneous welfare gains under optimal policy: Results

Match quality $x$			Share $s$			Employment $e$	
Bottom	Middle	Top	Bottom	Middle	Top	$E$	$U$
0.24	0.13	0.16	0.13	0.18	0.10	0.15	0.20