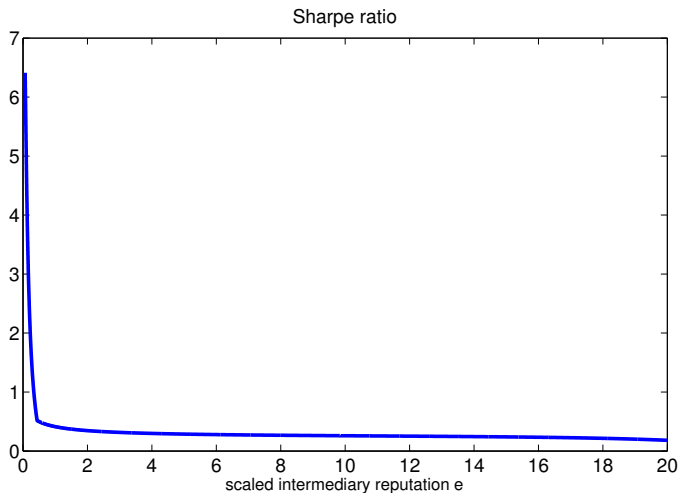


# A Macroeconomic Framework for Quantifying Systemic Risk

Zhiguo He, University of Chicago and NBER  
Arvind Krishnamurthy, Stanford University and NBER

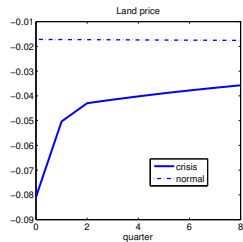
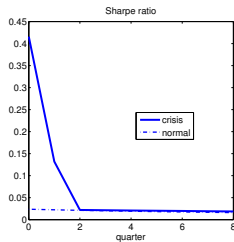
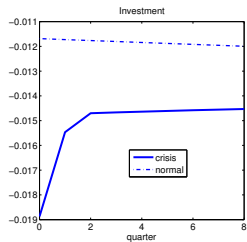
March 2015

## Financial Crisis in the Model

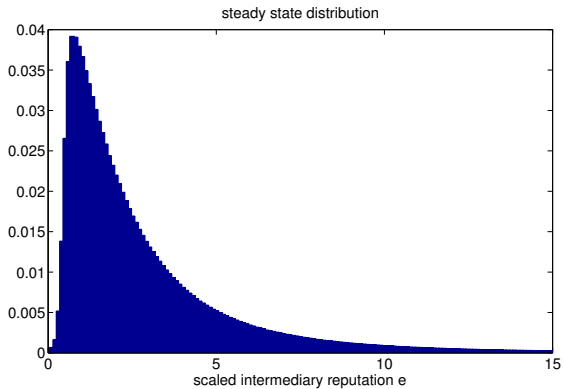


Note: Capital constraint binds for  $e < 0.435$

# Non-linearity: State-dependent Impulse Response: -1% Shock



# Global Solution: Steady State Distribution



## Model-based stress test

- Pick initial condition to match 2007Q2 asset prices
- Probability of crisis over horizon:
  - ▶ 1 year: 0.32%
  - ▶ 2 year: 3.57%
  - ▶ 5 year: 17.30 %
- Initial condition + rational forward looking agents = can't see around corners!

## Model-based stress test

- Pick initial condition to match 2007Q2 asset prices
- Probability of crisis over horizon:
  - ▶ 1 year: 0.32%
  - ▶ 2 year: 3.57%
  - ▶ 5 year: 17.30 %
- Initial condition + rational forward looking agents = can't see around corners!
- Stress test:
  - ▶ Add \$2 trillion of shadow banking liabilities, with close to 0% capital.
  - ▶ This information was not in 2007Q2 asset prices
- Probability of crisis over horizon:
  - ▶ 1 year: 6.73%
  - ▶ 2 year: 23.45%
  - ▶ 5 year: 57.95 %

- 1 Nonlinear macro model of a financial crisis
  - ▶ Recent work on financial intermediaries: He-Krishnamurthy, Brunnermeier-Sannikov, Rampini-Viswanathan, Adrian-Boyarchenko, Gertler-Kiyotaki
  - ▶ Our approach: occasionally binding constraint; global solution method (similar to Brunnermeier-Sannikov, Adrian-Boyarchenko)

# Outline of Presentation

- 1 Nonlinear macro model of a financial crisis
  - ▶ Recent work on financial intermediaries: He-Krishnamurthy, Brunnermeier-Sannikov, Rampini-Viswanathan, Adrian-Boyarchenko, Gertler-Kiyotaki
  - ▶ Our approach: occasionally binding constraint; global solution method (similar to Brunnermeier-Sannikov, Adrian-Boyarchenko)
- 2 Calibration and results
- 3 Quantify systemic risk and stress test



## Model

- Two classes of agents: households and bankers

- ▶ Households:

$$\mathbb{E} \left[ \int_0^{\infty} e^{-\rho t} \frac{1}{1-\gamma} C_t^{1-\gamma} dt \right], \quad C_t = (c_t^y)^{1-\phi} (c_t^h)^{\phi}$$

- Two types of capital: productive capital  $K_t$  and housing capital  $H$ .
  - ▶ Fixed supply of housing  $H \equiv 1$
  - ▶ Price of capital  $q_t$  and price of housing  $P_t$  determined in equilibrium

## Model

- Two classes of agents: households and bankers

- ▶ Households:

$$\mathbb{E} \left[ \int_0^{\infty} e^{-\rho t} \frac{1}{1-\gamma} C_t^{1-\gamma} dt \right], \quad C_t = (c_t^y)^{1-\phi} (c_t^h)^{\phi}$$

- Two types of capital: productive capital  $K_t$  and housing capital  $H$ .
  - ▶ Fixed supply of housing  $H \equiv 1$
  - ▶ Price of capital  $q_t$  and price of housing  $P_t$  determined in equilibrium
- Production  $Y = AK_t$ , with  $A$  being constant
- Fundamental shocks: stochastic capital quality shock  $dZ_t$ . TFP shocks

$$\frac{dK_t}{K_t} = i_t dt - \delta dt + \sigma dZ_t$$

## Model

- Two classes of agents: households and bankers

- ▶ Households:

$$\mathbb{E} \left[ \int_0^{\infty} e^{-\rho t} \frac{1}{1-\gamma} C_t^{1-\gamma} dt \right], \quad C_t = (c_t^y)^{1-\phi} (c_t^h)^{\phi}$$

- Two types of capital: productive capital  $K_t$  and housing capital  $H$ .
  - ▶ Fixed supply of housing  $H \equiv 1$
  - ▶ Price of capital  $q_t$  and price of housing  $P_t$  determined in equilibrium
- Production  $Y = AK_t$ , with  $A$  being constant
- Fundamental shocks: stochastic capital quality shock  $dZ_t$ . TFP shocks

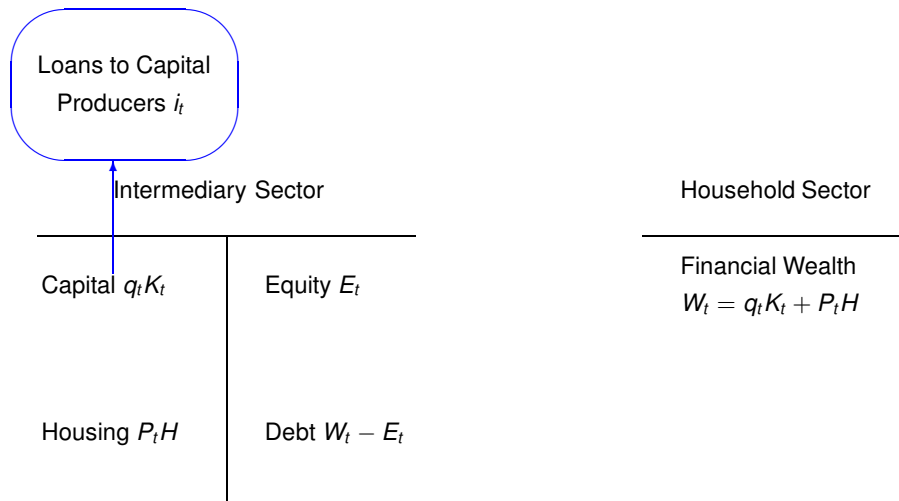
$$\frac{dK_t}{K_t} = i_t dt - \delta dt + \sigma dZ_t$$

- Investment/Capital  $i_t$ , quadratic adjustment cost

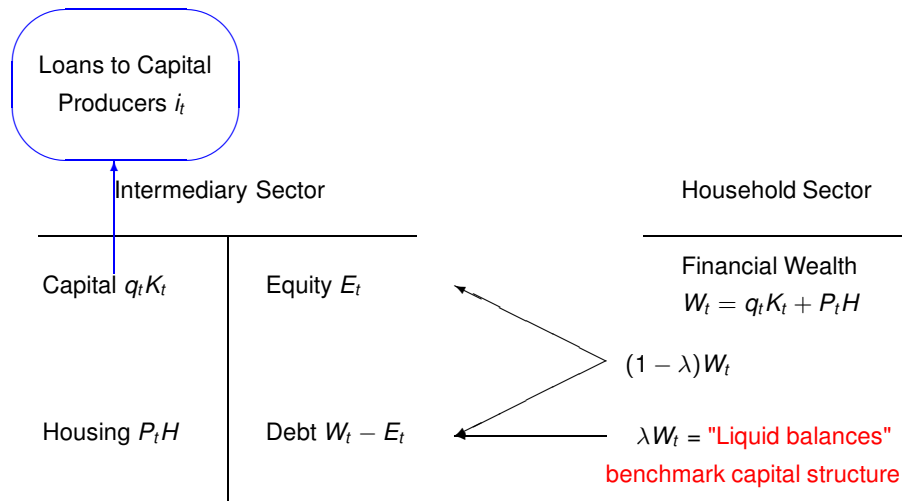
$$\Phi(i_t, K_t) = i_t K_t + \frac{\kappa}{2} (i_t - \delta)^2 K_t$$

$$\max_{i_t} q_t i_t K_t - \Phi(i_t, K_t) \Rightarrow i_t = \delta + \frac{q_t - 1}{\kappa}$$

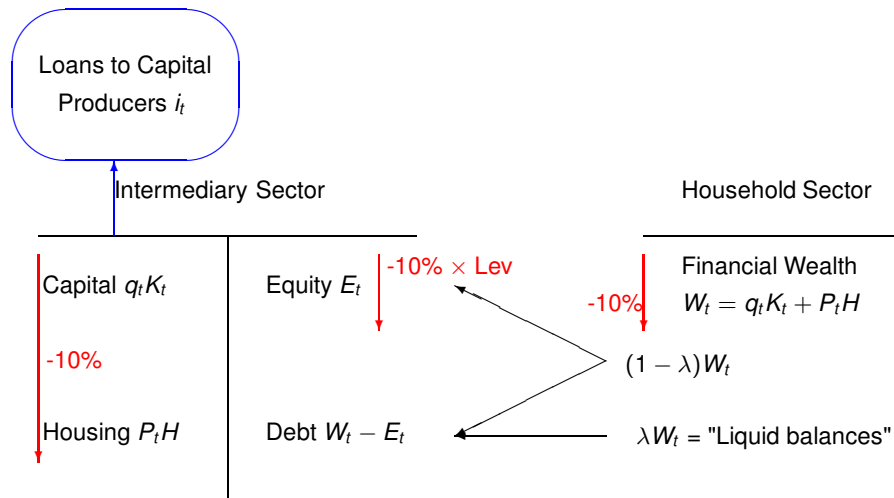
## Aggregate Balance Sheet



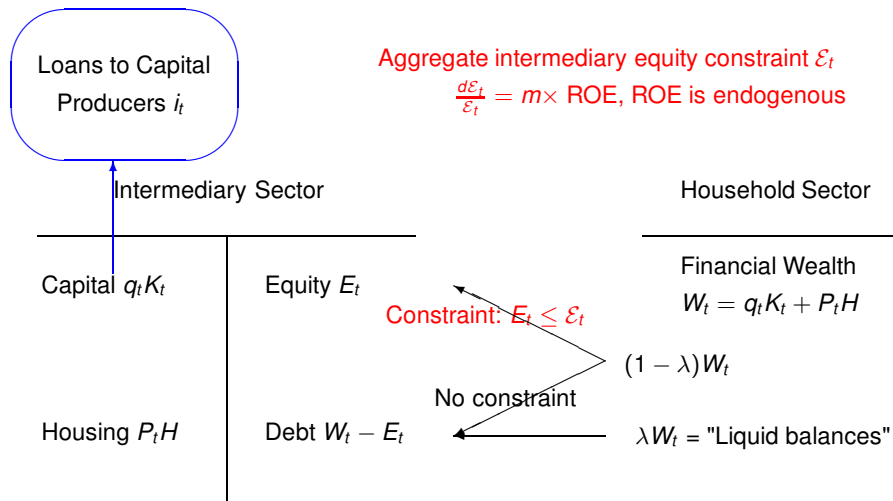
# Aggregate Balance Sheet



# Equity Dynamics in GE



# Equity Constraint



## Equity constraint: $\epsilon_t$

- Bank can raise equity upto  $\epsilon_t$  at zero cost
- Cost of raising equity more than  $\epsilon_t$  is infinite.
- $\epsilon_t$  linked to intermediary performance (constant  $m$ )

$$\frac{d\epsilon_t}{\epsilon_t} = m d\tilde{R}_t.$$



## Equity constraint: $\epsilon_t$

- Bank can raise equity upto  $\epsilon_t$  at zero cost
- Cost of raising equity more than  $\epsilon_t$  is infinite.
- $\epsilon_t$  linked to intermediary performance (constant  $m$ )

$$\frac{d\epsilon_t}{\epsilon_t} = m d\tilde{R}_t.$$

- ▶  $\epsilon_t$  as "reputation" of the banker
- ▶  $\epsilon_t$  as banker's "net worth" fluctuating with past returns

## Equity constraint: $\epsilon_t$

- Bank can raise equity upto  $\epsilon_t$  at zero cost
- Cost of raising equity more than  $\epsilon_t$  is infinite.
- $\epsilon_t$  linked to intermediary performance (constant  $m$ )

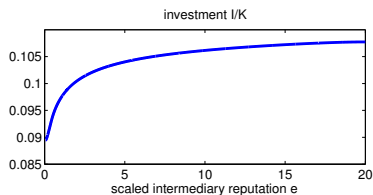
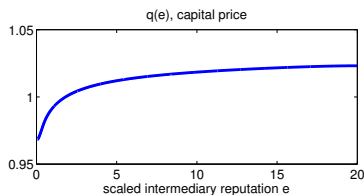
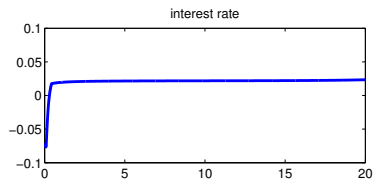
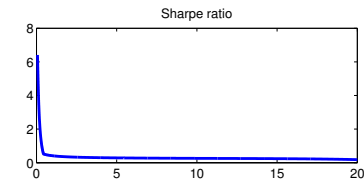
$$\frac{d\epsilon_t}{\epsilon_t} = m d\tilde{R}_t.$$

- ▶  $\epsilon_t$  as “reputation” of the banker
- ▶  $\epsilon_t$  as banker’s “net worth” fluctuating with past returns
- Aggregate dynamics of  $\mathcal{E}_t = \int \epsilon_t$

## Calibration: Baseline Parameters

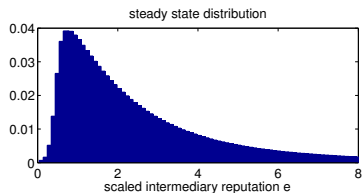
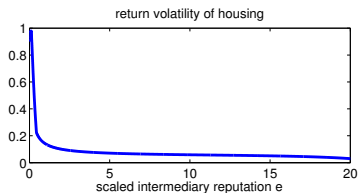
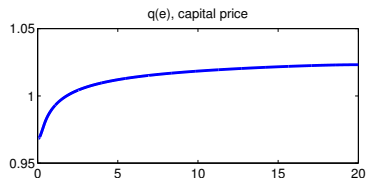
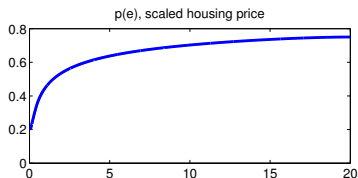
Parameter	Choice	Targets (Unconditional)	
Panel A: Intermediation			
$m$	Performance sensitivity	2	Average Sharpe ratio (model=38%)
$\lambda$	Debt ratio	0.67	Average intermediary leverage
$\eta$	Banker exit rate	13%	Prob. of crisis (model,data = 3%)
$\gamma$	Entry trigger	6.5	Highest Sharpe ratio
$\beta$	Entry cost	2.43	Average land price vol (model,data=14%)
Panel B: Technology			
$\sigma$	Capital quality shock	3%	Consumption volatility (model=1.4%) Note: Model investment vol = 4.5%
$\delta$	Depreciation rate	10%	Literature
$\kappa$	Adjustment cost	3	Literature
$A$	Productivity	0.133	Average investment-to-capital ratio
Panel C: Others			
$\rho$	Time discount rate	2%	Literature
$\xi$	1/EIS	0.15	Interest rate volatility
$\phi$	Housing share	0.5	Housing-to-wealth ratio

## Results(1): State variable is $e_t = \mathcal{E}_t/K_t$



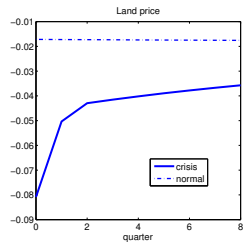
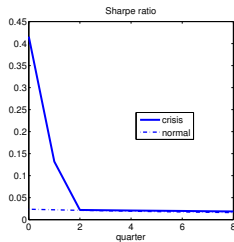
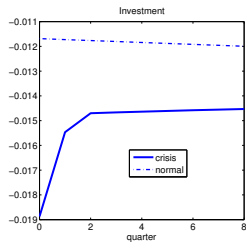
- Capital constraint binds for  $e < 0.435$

## Results(2)



- Capital constraint binds for  $e < 0.435$
- Without the possibility of the capital constraint, all of these lines would be flat. Model dynamics would be i.i.d., with vol=3%

# State-dependent Impulse Response: -1% Shock ( $= \sigma dZ_t$ ) ▶ VARdata

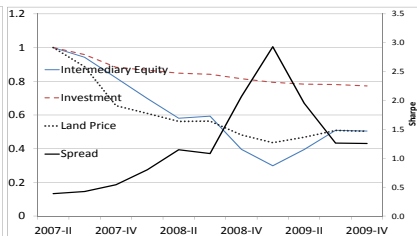
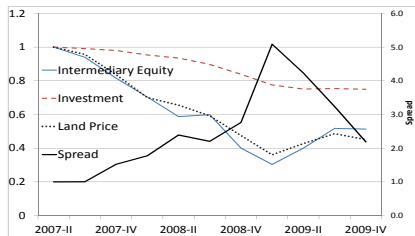


## Matching the 2007-2009 Crisis

Pick initial condition for intermediary state variable ( $e$ ) to match asset prices in 2007Q2

- Asset price = Gilchrist-Zakrajsek credit spread
- *Note: this spread (as with most spreads) was low in 2007Q2*
- Data from 1975 to 2010; compute histogram of spread variable
- Match percentile of spread in the data to the same percentile in model implied distribution for risk premium
  
- Answer: In 2007Q2,  $e = 1.27$ .

## Matching Recent Crisis: *Data(L)* and *Model(R)*



- Set initial condition of  $e = 1.27$  in 2007Q2.
- Then choose  $(Z_{t+1} - Z_t)$  shocks to match realized intermediary equity series.

07QIII	07QIV	08QI	08QII	08QIII	08QIV	09QI	09QII	09QIII	09QIV
-2.5%	-4.2	-1.1	-1.1	-0.7	-1.6	-1.8	-1.8	-0.9	-0.9

- ▶ Total -15.5%. Capital constraint binds after 07Q4—systemic risk state
- ▶ In the model (data), land price falls by 50% (55%)
- ▶ In the model (data), investment falls by 23% (25%)



## Systemic Risk: What is the probability of the 2007-2009 crisis?

- What is the likelihood of the constraint binding ("systemic crisis") assuming  $e = 1.27$  currently:
  - ▶ 0.32% in next 1 years
  - ▶ 3.57% in next 2 years
  - ▶ 17.30% in next 5 years

## Systemic Risk: What is the probability of the 2007-2009 crisis?

- What is the likelihood of the constraint binding ("systemic crisis") assuming  $e = 1.27$  currently:
  - ▶ 0.32% in next 1 years
  - ▶ 3.57% in next 2 years
  - ▶ 17.30% in next 5 years

### Lessons:

- Initial condition calibrated to asset prices + rational forward looking agents = can't see around corners!
- Even with a highly non-linear model
- Could abandon RE. Credit growth unusually high, crash likely, even though asset markets dont see it

## Stress testing: Leverage test

- Financial sector aggregate leverage fixed at 3 in model
  - ▶ We measure across commercial banks, broker/dealers, hedge funds in 2007:
    - ▶ Assets = \$15,703 billion; Liabilities = \$10,545 billion
- Suppose a stress test uncovered leverage:
  - ▶ ABCP (SIVs): \$1,189 billion; Liabilities \$1,189 billion
  - ▶ Repo (MMFs and Sec Lenders): \$1,020 billion; Liabilities \$1,000 billion (assumed 2% haircut)
- Leverage is “hidden” in sense that agents take equilibrium functions as given based on leverage=3
  - ▶ 1 year: 6.73%
  - ▶ 2 year: 23.45%
  - ▶ 5 year: 57.95 %

## Stress testing plus a model

- In current practice, work goes into estimating exposure (i.e. true leverage in example)

With a model:

- 1 Stress may trigger macro and asset price feedbacks, second round,... third round...
  - ▶ Model computes the fixed point
- 2 Model translates stress event into a probability of a systemic crisis
- 3 Model can help calibrate corrective actions (i.e. capital raising) based on target:
  - ▶ How much capital is needed to ensure probability of crisis  $< X\%$ ?
  - ▶ "Macro-VAR"

## Stress testing

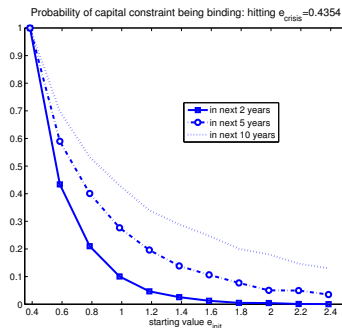
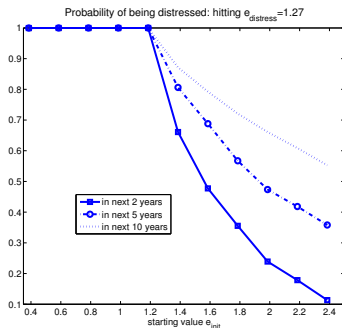
Key step: Need to map from stress scenario into underlying shock,  $dZ_t$ .

- Say stress scenario  $\Rightarrow$  -30% Return on equity
- Naive partial eqbm: leverage of 3,  $\sigma(Z_{t+0.25} - Z_t) = -30/3 = -10\%$ .
- Feed in  $-10\%$  shock into the model over one quarter.
- Result: Beginning at  $e = 1.27$  in 2007Q2, economy is immediately moved into crisis region,  $e < 0.435$
- our model helps in figuring out the right shock  $dZ_t$

In US stress tests, scenario was over 6 quarters. Feed in shocks quarter-by-quarter, over 6 quarters:

Return on Equity	6 QTR Shocks	Prob(Crisis within next 2 years)
-2%	-1.16%	5.25 %
-5	-2.53%	8.90
-10	-4.69%	22.88
-15	-6.71%	48.90
-30	-8.72%	100.00

# Stress testing

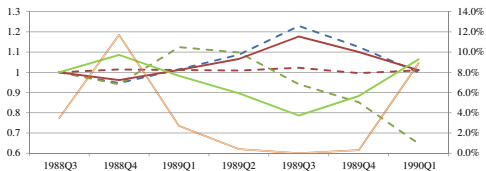


Map “stress test” into a shock to  $e$ .

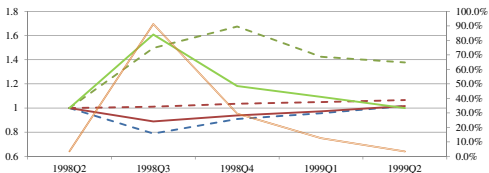
## Conclusion

- We develop a fully stochastic model of a systemic crisis, with an equity capital constraint on the intermediary sector
- Is able to replicate 2007/2008 period with only intermediary capital shocks
- The model quantitatively matches the differential comovements in distress and non-distress periods
- Offers a way of mapping macro-stress tests into probability of systemic states.

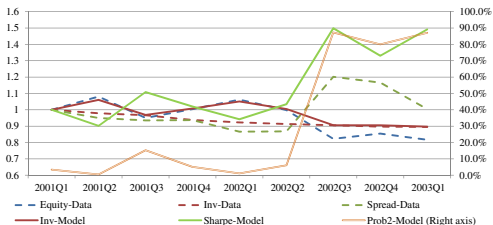
# Other crises



Panel A: Savings and Loan Crisis



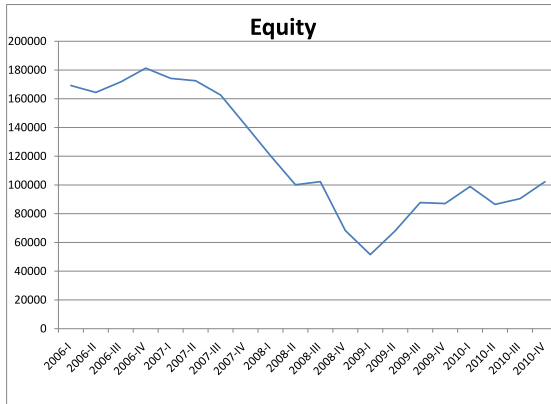
Panel B: 1998 Hedge Fund Crisis

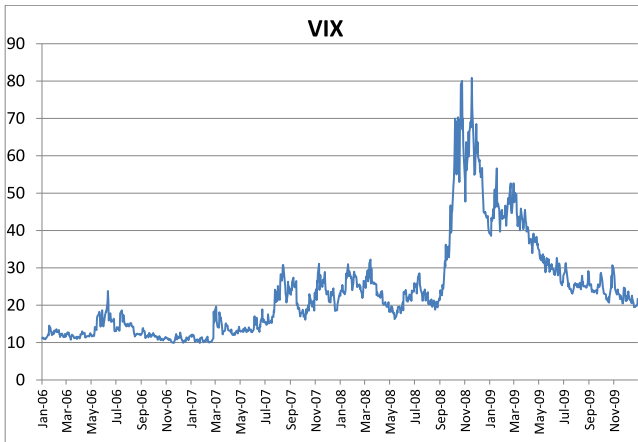


— Equity-Data     
 - - Inv-Data     
 - - Spread-Data  
— Inv-Model     
 — Sharpe-Model     
 — Prob2-Model (Right axis)

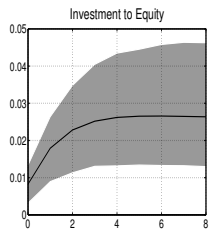
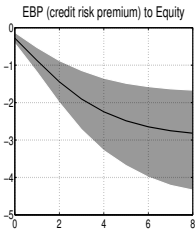
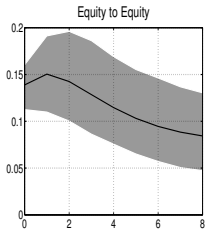


# Equity series





### Panel A: Distress Periods



### Panel B: Non Distress Periods

