

# Discussion of Doshi, Jacobs and Liu “Loss Functions for Forecasting Treasury Yields”

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November 4, 2015

## There's a Lot to Like in This Paper

- Prediction under the relevant loss function  
deserves lots of attention
- The yield curve model used for prediction  
deserves lots of attention
- Maybe even yield curve curvature  
deserves lots of attention

# Prediction Under the Relevant Loss Function

# Prediction is Key in an Evidence-Based Macro-Finance

History:  $\{y_t\}_{t=1}^T$

Realization and prediction:  $y_{T+h}, \hat{y}_{T+h,T}$

Error:  $e_{T+h,T} = y_{T+h} - \hat{y}_{T+h,T}$

Loss:  $L(e_{T+h,T})$

Accuracy comparison via expected loss:  $E(L(e_{T+h,T}))$

# What is the Relevant Loss Function, $L(e_{T+h,T})$ ?

What is the horizon,  $h$ ? Short term? Long term?

– Doshi et al. (2015)  
(this paper)

What is the loss function  $L$ ?  $L(e) = e^2$ ?  $L(e) = |e|$ ?

– Diebold and Shin (2015),  
“Assessing Point Forecast Accuracy by Stochastic Error Distance”

# Estimation Under the Relevant Loss Function: Shines in Principle

Correct specification:

- We learn the truth asymptotically
- It is best for all purposes

Incorrect specification:

- We never learn the truth, even asymptotically
- Instead we learn a “best approximation,” induced by  $L$
- MLE effectively ties our hands and picks  $L$
  - Instead, think hard about the relevant loss function
- Best approximation for one purpose generally very different from (and not implied by) best approximation for another purpose
- e.g., mis-specified  $AR(1)$ :  $\hat{\rho}^{10} \neq \widehat{\rho}^{10}$ , even as  $T \rightarrow \infty$

# Estimation Under the Relevant Multi-Step Loss Function: Flops in Practice

Of course everyone knows Weiss (1996, *J. Applied Econometrics*)

But there's a "file drawer problem"

Marcellino-Stock-Watson (2006, *Journal of Econometrics*)

is very clearly negative and not cited

("A Comparison of Direct and Iterated Multistep AR Methods for  
Forecasting Macroeconomic Time Series")

# The Yield Curve Model Used for Prediction



# Successful Time-Series Prediction Requires *Parsimony*

- Selection
- Bayesian shrinkage
- Lasso

“The Parsimony Principle”

For prediction,  
“maximally-flexible” models are not appealing

# An Appealing Predictive Model

Arbitrage-Free Nelson-Siegel (AFNS)  
(Christensen et al., 2011, *Journal of Econometrics*)

$$y_t = \Lambda f_t + \varepsilon_t$$

$$f_t = \Phi f_{t-1} + \eta_t$$

- Three (latent) factors; provably level, slope, curvature
  - Factors are latent but estimation is trivial and reliable
  - Easily accommodates the zero lower bound, non-spanning, etc.
    - *Structure placed on factor loadings ( $\Lambda$  matrix)*
- [Equivalently, structure on Duffie-Kan state-transition dynamics]  
[Equivalently, structure on maximally-flexible  $A_0(3)$ ]
- Joslin et al. (2011, *Review of Financial Studies*)  
*test the restrictions and find  $p \approx 1/2$*

# Yield Curve Curvature

???

## In Conclusion: What I'd Like to See

- 1-step vs.  $h$ -step estimation
- Squared-error vs. absolute-error loss
- AFNS  $A_0(3)$  vs. JSZ maximally-flexible  $A_0(3)$   
(and drop the latent-state maximally-flexible affine models)
- Robustness to sample start date, sample end date,  
in-sample / out-of-sample split, estimation method, etc.
- Progress in understanding curvature