

# Virtual Seminar on Climate Economics

Federal Reserve Bank of San Francisco



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# On the dependence of investor's probability of default on climate transition scenarios

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# Section 1

## Background and motivation

# Climate change: a new type of financial risk

- Central banks and financial regulators are increasingly concerned about **climate-related financial risks** (Carney 2015, FSB 2020):
  - **physical** risk: emissions concentration affects hazards and losses
  - **transition** risk: change in climate policy, regulation, technology affect firms' performance **based on energy technology**
- Financial supervisors worry about the impact of a **disorderly transition** on **financial stability** (NGFS 2019, FED 2020, etc)
  - Late/sudden introduction of climate policies whose impacts cannot be fully anticipated by investors
- Several central banks and financial regulators joined the Network for Greening the Financial System (NGFS):
  - Guidelines on **climate stress test** scenarios (NGFS 2020)
  - In action: some central banks developed climate stress tests (Dutch Central Bank 2019, Banque de France 2020).

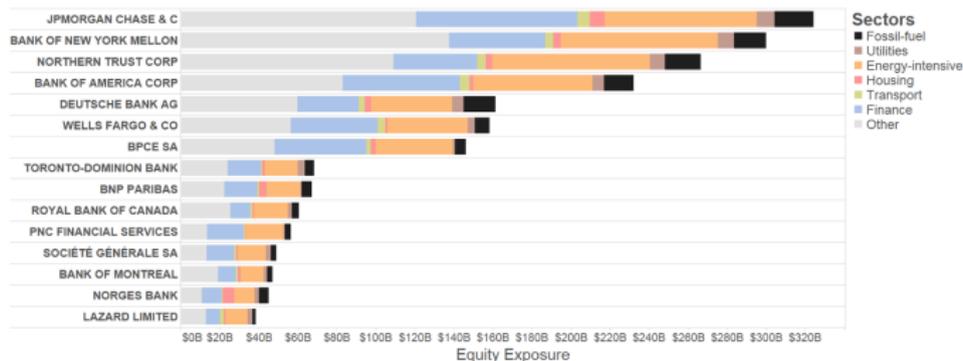
# Should financial supervisors worry? YES

Their concerns are grounded in research results:

- Dietz ea (2016): climate value at risk (VaR) of global financial assets is 1.8 percent along a business-as-usual emissions path (USD2.5 trn), much of risk in the tail
- Battiston ea (2017)'s Climate stress test: investors are exposed to activities (**Climate Policy Relevant Sectors-CPRS**) that can face losses and become stranded assets in a disorderly transition:
  - 43-45 percent of equity holdings' portfolios of pension funds and investment funds; banks most exposed to fossil and utility via loans
  - Risk can be amplified by reverberation in the network of interconnected financial actors, creating conditions for systemic risk
- *Climate risks and financial stability* research at the core of forth. Special issue on *Journal of Financial Stability* (Battiston ea 2021)

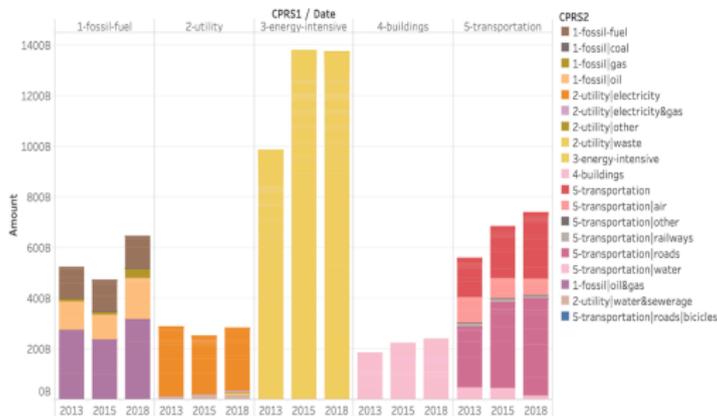
# Why risk? Investors have large exposures to CPRS

- Classification of financial assets' transition risk is provided by **Climate Policy Relevant Sectors (CPRS)**, (Battiston ea. 2017): Fossil fuel, Utility, Energy intensive, Housing, Transport, Agriculture
- CPRS overcome key limitations of approaches based only on emissions by considering firms' energy technology mix and policy sensitivity, to operationalize the notion of **stranded assets**



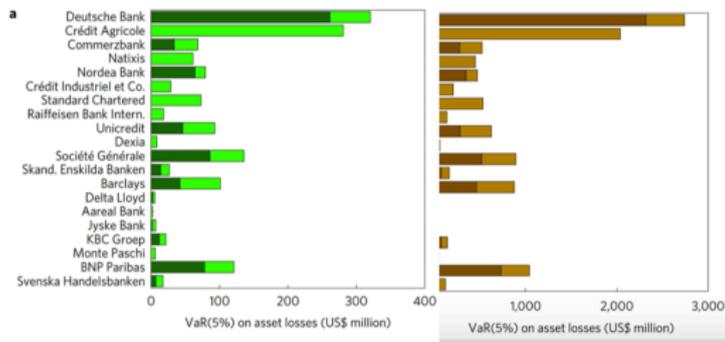
# CPRS is applied by several financial supervisors

- **European Commission JRC study of EU Taxonomy financial impact (EU equity and bonds market, this figure), 2019**
- **EIOPA Financial Stability Report 2019**
- **European Central Bank (2019)'s Climate change and financial stability (Financial Stability Review 2019)**
- **EBA Risk assessment of the EU banking system, Dec. 2020**
- **National Bank of Austria, Financial Stability Report 2020**



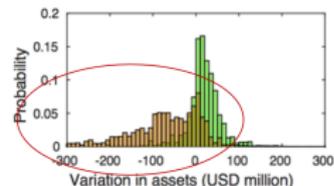
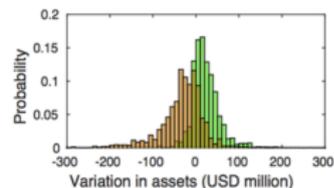
Source: Alessi et al. (2019) financial impact assessment of the EU Taxonomy

# Large direct/indirect exposures may trigger systemic risk



**Value at Risk (5% significance) on equity holdings of 20 most affected EU banks under scenario of green (brown) investment strategy. Dark/light colors: first/second round losses. Source: Battiston *et al.* (2017). A climate stress test of the financial system. *Nature Climate Change***

**1<sup>st</sup> round (top):** brown bank incurs more losses.  
**Adding 2<sup>nd</sup> round (bottom)** polarizes distribution of losses.



# Knowledge gaps for supervisory activities

- Better understanding is needed of how climate transition risk affects financial assets and investors' financial stability
- In particular, we need to understand how sensitive are investor's risk metrics (Probability of default (PD) and Expected Shortfall (ES)) to the probability of occurrence of disorderly scenarios (the risky ones)
- **This is crucial for climate financial risk supervision and risk management strategies (incl. relevant scenarios for climate stress testing). But it is still missing in the literature**

## Section 2

# Contribution of the paper

# Outline

- **Climate change** brings about a **new type** of financial risk that standard approaches to risk management are not adequate to handle
- With analytical and computational work, we study:
  - **Valuation adjustment of bonds** (corp.) based on available knowledge on climate transition scenarios (carbon pricing)
  - How PD of bonds depends on the interplay between energy technology profile of firm activities (high/low-carbon), climate transition scenarios, considering deep uncertainty on probabilities
  - Sensitivity of investor PD and ES to climate-adjusted bond PD and to the probability of occurrence of disorderly scenarios (including NGFS ones)
- We consider how PD varies across all spaces of portfolio configurations (high/low-carbon assets) that include also equilibrium portfolio

# This paper is about climate transition risk

- Many economic papers consider climate risk only in terms of GHG emissions and/or disasters (i.e. backward- looking data on temperature, emissions, losses)
- However, **climate transition risk** is relevant for finance even before climate physical risk: time horizon (5-10y)
  - Relevant variables: energy technology profile of activity, policy design
- Assessing climate transition risk is more challenging:
  - **Forward-looking**: historical info. is not a good proxy of future risks
  - Many firms issuing green bonds have multiple activities (low/high-carbon)
- Thus, we need to work with transition scenarios (e.g. those produced by Integrated Assessment Models (IAMs))

# Economic intuition

- If markets price efficiently climate risk (high carbon firms are more risky) and anticipate policy impact, transition risk not financially relevant. However, no clear signals.
- **Friction:** deep uncertainty on climate transition scenarios, their probability of occurrence and their impact, means that agents are not able/willing to internalise information on transition risk
- Issuers can vary share of investments in low/high carbon activities, investors can vary portfolio composition across issuers. However, forward-looking risk make full hedging not possible

# Main results

- The PD and ES of a leveraged investor increase non-linearly with the impact of the climate policy shock on revenues of corp. bond issuer (in low/high-carbon activities)
- The PD of a leveraged investor is sensitive to small changes in adjusted bond PD, to the probability of occurrence of disorderly climate transition scenarios
- Thus, assumptions on the sets of climate transition scenarios and their probability of occurrence play a main role for investors' risk management

# Do they matter for climate risk supervision? YES

- Take home messages for financial supervisors involved in climate financial risk management (**NGFS, ECB's Climate Change center, NY FED's Supervision Climate Committee**):
  - 1 Investors' PD can be highly sensitive to choice and probability of occurrence of climate transition scenarios.
  - 2 Thus, in order to limit the underestimation of losses due to climate transition risk, **climate stress test** exercises should allow for wide enough sets of scenarios
  - 3 Our model provides **an operative framework** to assess the dependence of investors' PD on the choice of climate scenarios, applicable with several types of climate economic and macroeconomic models

# Section 3

## The model

# Scenarios

## Definitions

- ① Set of Climate Policy Scenarios  $P$  corresponding to GHG emission reduction targets (e.g. 2degC) across regions ( $B = \text{Base}$ , no policy):

$$\text{ClimPolScen} = \{B, P_1, \dots, P_l, \dots, P_{n_{\text{Scen}}}\}$$

- ② Set of economic output trajectories for each sector  $S$ , country  $C$ , scenario  $P$ , estimated with given climate economic model  $M$ :

$$\text{EconScen} = \{Y_{1,1,1,1}, \dots, Y_{C,S,P,M}, \dots\}$$

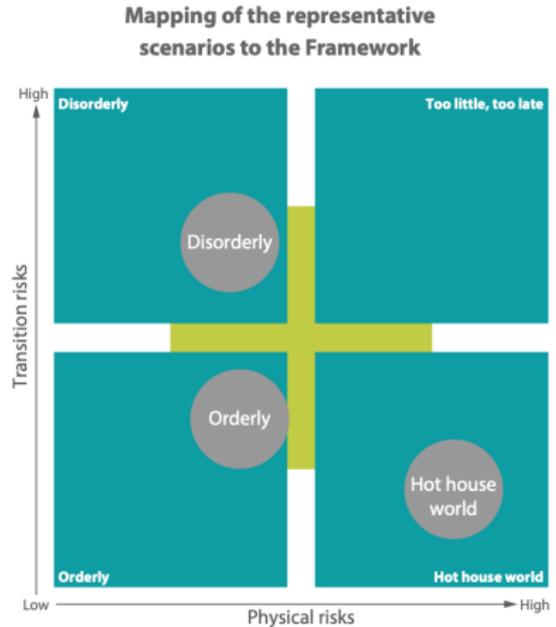
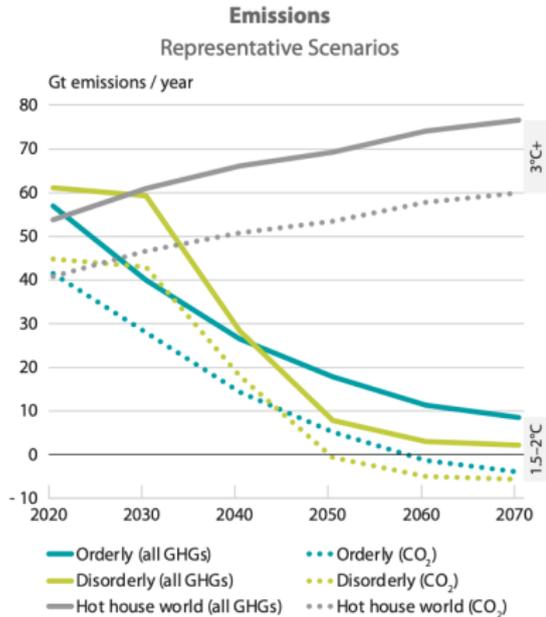
- ③ Set of **forward-looking** (disorderly) Transition Scenarios:

$$\text{TranScen} = \{BP_1, \dots, BP, \dots, BP_{n_{\text{Scen}}}\}$$

- ④ Set of Climate Policy Shocks: differences on economic output for  $S$ ,  $C$ , from  $B$  to  $P$ , estimated with model  $M$

$$\text{PolShock} = \left\{ \dots, \frac{Y_{C,S,P,M} - Y_{C,S,B,M}}{Y_{C,S,B,M}}, \dots \right\}$$

# Example of orderly and disorderly scenarios



Source: IIASA NGFS Climate Scenarios Database, using marker models.

# Impact of a disorderly transition on firm's revenues

- Decompose net shock on revenues of issuer  $j$  (with  $u_{j,S}$ : relative shock on  $S$ ;  $w_{j,S}$ : share of  $j$ 's revenues from  $S$ ):

$$\begin{aligned}
 u_j(BP) &= \frac{\text{rev}_j(P) - \text{rev}_j(B)}{\text{rev}_j(B)} = \sum_S \left( \frac{\text{rev}_{j,S}(P) - \text{rev}_{j,S}(B)}{\text{rev}_{j,S}(B)} \frac{\text{rev}_{j,S}(B)}{\text{rev}_j(B)} \right) \\
 &= \sum_S (u_{j,S}(BP) w_{j,S}(B)), \tag{1}
 \end{aligned}$$

- Focus on CPRS: Primary Energy Fossil (**PrFos**), Electricity Fossil (**EIFos**), Renewable (**EIRen**):

$$\begin{aligned}
 u_j(BP) &= u_{j,\text{PrFos}}(BP) w_{j,\text{PrFos}}(B) + \\
 &\quad u_{j,\text{EIFos}}(BP) w_{j,\text{EIFos}}(B) + u_{j,\text{EIRen}}(BP) w_{j,\text{EIRen}}(B). \tag{2}
 \end{aligned}$$

- Impact of Transition Scenario  $BP$  on revenues  $u_j$ , result in shock  $\xi_j(BP)$  on  $j$ 's assets ( $\chi_j^0$  denotes elasticity):

$$\xi_j(BP) = \chi_j^0 u_j(BP) \tag{3}$$

# Impact of a disorderly transition on firm's revenues

## Remarks

- Firm is considered as a portfolio of (low/high carbon) activities
- In a disorderly transition, high-carbon (low-carbon) activities will incur losses (gains) from carbon-stranded assets
- Shock on  $j$ 's revenues,  $u_{j,S}(BP)$ , can be approximated as a shock on output of the corresponding economic activities  $S$  (e.g. EIFos) in the economy provided by climate economic models (e.g. IAM)
- Which transition scenarios will occur is uncertain and endogenous because it depends on governments' climate policies and investors' expectations and reactions (climate sentiments, Dunz et al., 2020)

# Securities: corporate bonds

## Basic facts for zero-coupon defaultable bonds

- Risky (defaultable) bond of issuer  $j$ , issued at  $t=0$  with maturity  $T$
- Bond value at  $T$ , with  $R$  bond *Recovery Rate* (i.e. % of notional recovered upon default); *LGD Loss-Given-Default* (i.e. % loss)

$$v_j(T) = \begin{cases} R_j = (1 - \text{LGD}_j) & \text{if } j \text{ defaults (with prob. } q_j) \\ 1 & \text{else (with prob. } 1 - q_j) \end{cases}$$

- Expected value of bond's payoff is given by:

$$\mathbb{E}[v_j] = (1 - q_j) + q_j R_j = 1 - q_j(1 - R_j) = 1 - q_j \text{LGD}_j$$

- Bond price  $v_j^*$ : bond discounted expected value, with  $y_f$  risk-free rate. Price defines implicitly bond yield  $y_j$  (risk neutral measure) as:

$$v_j^* = e^{-y_f T} \mathbb{E}[v_j] = e^{-y_f T} (1 - q_j \text{LGD}_j) = e^{-y_j T}$$

- Bond spread defined as:  $s_j = y_j - y_f$ , with  $e^{-s_j T} = 1 - q_j \text{LGD}_j$
- Useful fact: for small  $s_j$ , spread = expected loss

$$s_j \approx \frac{1}{T} q_j(1 - R_j) = \frac{1}{T} q_j \text{LGD}_j$$

# Corporate default

## Shocks and default condition

- Issuer  $j$  balance sheet:  $A_j(t_0)$ ,  $A_j(T)$  **asset**,  $t_0 = 0$  issue time,  $T$  maturity;  $L_j(T)$  liability.

- Default condition: structural model, discrete time (Merton 1974)

$$A_j(T) = A_j(t_0)(1 + \eta_j(T)) < L_j(T)$$

- $\eta_j(T) \in \mathbb{R}$ : **idiosyncratic shock** (e.g. firm  $j$  productivity),  
 $\phi(\eta_1, \dots, \eta_j, \eta_n)$  **joint probability distribution of issuers** (defaults possibly correlated)
- We add climate policy shock  $\xi_j(BP)$  on  $j$ 's assets ("jump" up/down)
- New default condition reads:

$$A_j(T) = A_j(0)(1 + \eta_j(T) + \xi_j(BP)) < L_j(T)$$

$$\iff \eta_j(T) \leq \theta_j(BP) = L_j(T)/A_j(0) - 1 - \xi_j(T, BP)$$

- $\theta_j(BP)$  default threshold under scenario  $BP$
- $\xi_j(BP)$  positive/negative:  $\xi_j(BP) > -1$ , correlated across  $j$

# Section 4

## Results

# Adjustment of bond spread due climate transition

## Definition and Proposition

- Climate Spread  $\Delta s_j$  is change in spread  $s_j$ , conditional to transition scenario  $BP$ :

$$\Delta s_j = s_j(q_j(P) - s_j(q_j(B))).$$

- Conditional to transition scenario:

- (i) Climate spread reads:

$$\begin{aligned} \Delta s_j(BP) = & s_j(BP) - s_j(B) = \\ & - (1/T) (\log(v_j^*(BP)) - \log(v_j^*(B)) - (y_f(BP) - y_f(B))) \end{aligned}$$

- (ii)  $\Delta s_j(BP)$  increases (decreases) with magnitude of policy shock on revenues  $|u_j(BP)|$ , if  $u_j(BP) < 0$  ( $u_j(BP) > 0$ );
- (iv) For small shock  $u_j(BP) \ll 1$ :

$$\Delta s_j(BP) \approx - \frac{1}{T} \chi_j (u_{j,PrFos} w_{j,PrFos} + u_{j,EIFos} w_{j,EIFos} + u_{j,EIRen} w_{j,EIRen})$$

# Investor

## Investor and Portfolio Value-at-Risk

- Leveraged investor: ( $\Lambda = A/E$ )
- Investor  $i$ 's portfolio value  $z_i$  and portfolio rate of return  $\pi_i$  at  $T$ , with  $W_{ij}$  amount (numeraire) of  $j$ 's bond purchased by  $i$ :

$$z_i(T) = \sum_j W_{ij} v_j(T), \quad \pi_i = \frac{z_i(T) - z_i(t_0)}{z_i(t_0)}$$

- **Climate VaR** is the Value-at-Risk of the portfolio of investor  $i$ , conditional to Transition Scenario  $BP$  with:  $\pi$  portfolio return,  $\psi_P(\pi)$  distribution of returns conditional to the Climate Policy Shock, and  $\alpha$  is the confidence level:

$$\int_{-1}^{\text{ClimateVaR}_\alpha(BP)} \psi_{BP}(\pi) d\pi = \alpha \quad (4)$$

- **Climate ES** is the average of the losses above the Climate VaR:

$$\text{ES}(BP) = \frac{-1}{\alpha} \int_0^\alpha \text{ClimateVaR}_{\alpha'}(BP) d\alpha' \quad (5)$$

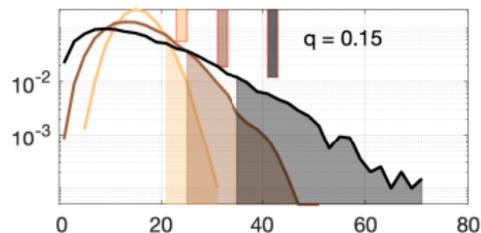
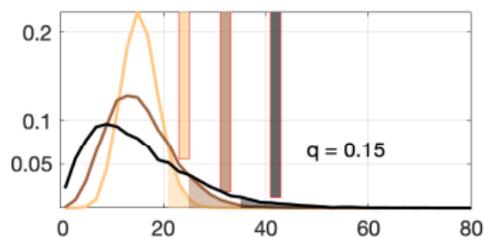
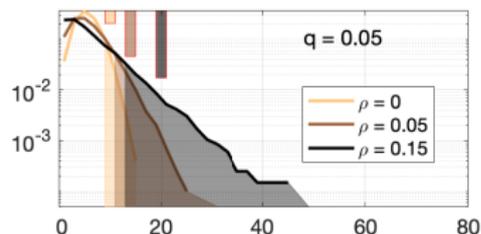
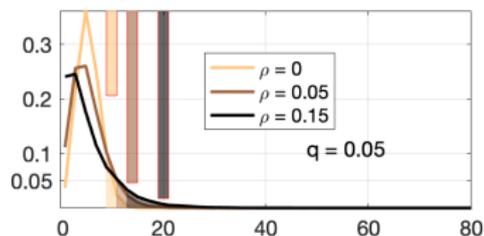
# Adjustment in investor's ES and PD

## Propositions

We prove several propositions on how investor's ES and PD are adjusted conditional to a transition scenario (Appendix). In short:

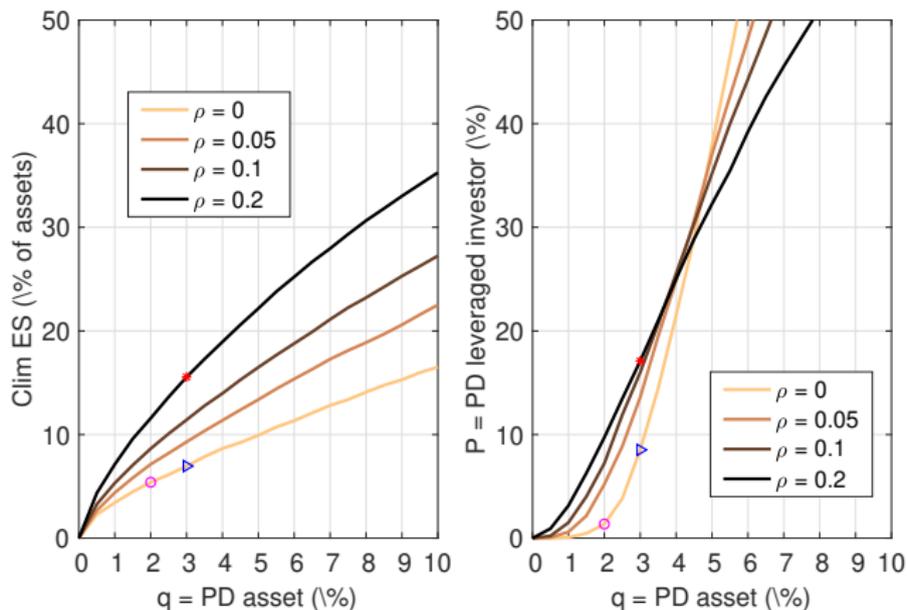
- ES(BP) increases with adjustment on bond default probability  $q(\text{BP})$
- Adjustment of PD of a leveraged investor can be derived analytically (numerically) in absence (presence) of correlation among bonds
- Under some assumptions of homogeneity, ES and PD decrease with share of climate-aligned revenues (i.e. renewable energy activities)

# How losses on bond portfolio depend on $q$ and $\rho$



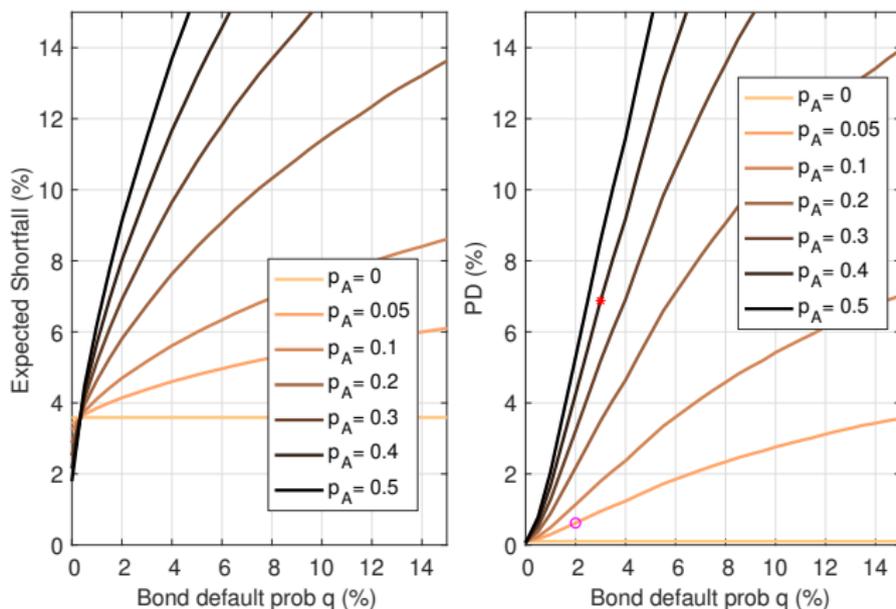
- Probability distribution (y-axis) of losses (x-axis, in %) on example portfolio of 100 bonds, equally weighted
- Climate ES (vertical bars) move right both with bond default probability  $q$  and with default correlation  $\rho$

# Climate ES and PD: sensitive to climate scenarios



- Consider a possible discrepancy between estimated  $(q, \rho)$  (magenta) and actual (blue, red)
- Large difference in Climate ES; even larger in PD

# Considering adverse scenario mitigate impact of uncertainty on ES and PD



- Adverse scenario occurs with prob.  $p_A$ . Effect of discrepancy between estimated  $(q, p_A)$  (magenta) and actual (red) is smaller if investor consider multiple scenarios, but still large

# Conclusion

- We develop a model to compute:
  - the valuation adjustment of a corporate bond, depending both on climate transition risk scenarios and on companies' shares of revenues across low/high-carbon activities, and
  - the corresponding adjustments in an investor's PD and ES
- Implications for climate financial risk management: **climate stress tests** should allow for a wide enough set of scenarios to limit the underestimation of losses
- The model provides an **operative framework** applicable with several types of climate and macroeconomic models
- Ongoing follow-up work: i) model calibration, ii) application to compound pandemic and **climate physical risk**.

**Comments, suggestions, critiques:  
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# Section 5

## Appendix

# A note on transition scenarios

- Climate economic models provide scenarios of emissions concentration to achieve 1.5/2 C world
- NGFS uses process-based IAM with granular representation of energy technologies (fossil, renewables)
- **Challenge:** IAM mitigation scenarios do not account for the role of finance in achieving the same scenarios, nor for financial complexity
- This has major implications on the design of **disorderly** scenarios:
  - Investments assumed to be available without frictions (no credit constraints)
  - Trajectories don't reflect the impact of mitigation scenarios on financial investment decisions
- Thus, considering more adverse scenarios on the IAM's range is important to avoid underestimate **financial risk associated** (Battiston ea. 2020)

# Issuer's default probability: definition

## Definition

- **Default probability**  $q_j$  of issuer  $j$  under Transition Scenario  $BP$ , with  $\phi_{BP}(\eta_j)$  probability distribution of idiosyncratic shock  $\eta_j$ ,  $\eta_{\text{inf}}$  lower bound of distribution support:

$$q_j(BP) = \mathcal{P}(\eta_j < \theta_j(BP)) = \int_{\eta_{\text{inf}}}^{\theta_j(BP)} \phi_{BP}(\eta_j) d\eta_j$$

## Definition. Default prob. adjustment $\Delta(BP)$

- Intuition. Frequent small productivity shocks across time and firms occur in a similar way with/without climate policy shock. Then, the policy shock shifts the probability distribution of productivity shocks and thus  $j$  default probability.
- Idiosyncratic shocks are **independent** from policy shock
- Result. Default probability **adjustment** under transition scenario:

$$\Delta q_j(BP) = q_j(P) - q_j(B) = \int_{\theta_j(B)}^{\theta_j(P)} \phi(\eta_j) d\eta_j, \text{ with}$$

$$\theta_j(P) = \theta_j(B) - \xi_j(P)$$

# Issuer's default probability: proposition

## Proposition. Default prob. adjustment $\Delta q_j(BP)$

- Assuming
  - idiosyncratic shocks are **independent** from policy shock
  - policy shock on asset proportional to shock on revenues via elasticity  $\xi_j = \chi_j^0 u_j(BP)$
- Then, the **adjustment** in default probability  $\Delta q_j(BP)$ 
  - increases with shock magnitude  $|u_j(BP)|$  if  $u_j^{BP} < 0$ , and decreases viceversa
  - Under approximation of small policy shock,  $\Delta q_j(BP)$  can be linearized to be proportional to shock on CPRS revenues:

$$\Delta q_j(BP) \approx -\chi_j (u_{j,PrFos(BP)} w_{j,PrFos} + u_{j,EiFos(BP)} w_{j,EiFos} + u_{j,EiRen(BP)} w_{j,EiRen}).$$

# Adjustment in bond value

## Definition and Proposition

- The adjustment in the value of the issuer's bond conditional to the Transition Scenario BP,  $\Delta v_j^*(BP)$ , is defined as the change in the discounted expected value of the bond, resulting from the Transition Scenario BP on issuer j's revenues  $u_j(BP)$ :

$$\Delta v_j^*(BP) = v_j^*(BP) - v_j^*(B) \quad (6)$$

- The following properties hold:
  - The expression of the adjustment of the value of the bond  $\Delta v_j^*$ , conditional to BP reads:

$$\Delta v_j^*(BP) = v_j^*(q_j(BP)) - v_j^*(q_j(B)) = -e^{-y_f T} \Delta q_j(BP) \text{LGD}_j \quad (7)$$

# Adjustment in investor's PD

## Proposition

- Consider a leveraged investor with an equally weighted portfolio, of zero-coupon bonds, with issuers having independent defaults occurring with the same probability  $q$  and with the loss-given-default LGD. The following properties hold:
  - The investor's PD,  $P(m, \Lambda, q)$  can be expressed in terms of the binomial distribution  $\mathcal{B}(m_-^*, m, q)$  :

$$P(m, \Lambda, q) = \mathcal{P}(X \geq m_-^*) = 1 - \mathcal{B}(m_-^*, m, q) \quad (8)$$

- The investor's PD is non decreasing in: a) the investor's leverage  $\Lambda$ ; b) the loss-given-default LGD; c) the bond default probability  $q$ .

# Adjustment in investor's PD

## Proposition: Example effect of climate-aligned investment

Consider:

- an equally weighted portfolio of zero-coupon bonds with the same PD,  $q$ , and the same loss-given-default  $LGD$
- all issuers  $j$  have the same shares of revenues across the three sectors Primary Energy Fossil, Electricity Fossil, Electricity Renewable,  $w_{j,PrFos}(B)$ ,  $w_{j,EIFos}(B)$ ,  $w_{j,EIRen}(B)$
- transition scenario BP such that  $u_{j,PrFos}(BP) < 0$ ,  $u_{j,EIFos}(BP) < 0$ ,  $u_{j,EIRen}(BP) > 0$  and the net shock on revenues  $u_j(BP) < 0$  for all  $j$

Then,

- (i) Then,  $ES(BP)$  decreases with the share of revenues  $w_{j,EIRen}(B)$
- (ii) Then,  $PD(BP)$  decreases with the share of revenues  $w_{j,EIRen}(B)$