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Market-Based Measures of Monetary Policy Expectations

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Abstract

A number of recent papers have used different financial market instruments to measure near-term expectations of the federal funds rate and the high-frequency changes in these instruments around FOMC announcements to measure monetary policy shocks. This paper evaluates the empirical success of a variety of financial market instruments in predicting the future path of monetary policy. All of the instruments we consider provide forecasts that are clearly superior to those of standard time series models at all of the horizons considered. Among financial market instruments, we find that federal funds futures dominate all the other securities in forecasting monetary policy at horizons out to six months. For longer horizons, the predictive power of many of the instruments we consider is very similar. In addition, we present evidence that monetary policy shocks computed using the current-month federal funds futures contract are influenced by changes in the timing of policy actions that do not influence the expected course of policy beyond a horizon of about six weeks. We propose an alternative shock measure that captures changes in market expectations of policy over slightly longer horizons.

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1. Introduction

Measures of monetary policy expectations are an important element of many empirical papers in the macroeconomics and finance literatures. Lately, a strand of literature has focused on measuring policy expectations from asset prices. In this context, market interest rates have often been used to parse out the unexpected component of policy decisions—often referred to as monetary policy shocks. Krueger and Kuttner (1996), Rudebusch (1998), and Brunner (2000) were among the first to explore this approach, and many others have subsequently followed their lead.

An important issue in this approach is the choice of the asset to be used in measuring expectations. The abundance of short-term interest rates that potentially measure federal funds rate expectations has led to a proliferation of asset-price-based monetary policy expectation measures, many times with an assertion that a particular measure is better than others with little evidence offered in support. Kuttner (2001) and Faust, Swanson, and Wright (2004) use the current-month federal funds futures contract, Bomfim (2003) and Poole and Rasche (2000) the month-ahead federal funds futures contract, Cochrane and Piazzessi (2002) the one-month eurodollar deposit rate, Ellingsen and Soderstrom (2004) the three-month Treasury bill rate, and Rigobon and Sack (2002) the three-month eurodollar futures rate.

This paper evaluates the ability of these and other financial market instruments to capture expectations of the future course of monetary policy and, correspondingly, to measure monetary policy shocks. Each of the financial market instruments we consider—term federal funds loans, federal funds futures, term eurodollar deposits, eurodollar futures, Treasury bills, and commercial paper—differ with respect to their risk and liquidity characteristics, so that it is not clear *a priori* which should provide the best forecast of the future course of monetary policy. For example, U.S. Treasury bills are regarded by market participants as being the safest and among the most liquid of the instruments in our study. Nonetheless, they may not be the best measure of monetary policy expectations because the price that investors are willing to pay for safety and liquidity may vary over time. The same kinds of problems arise with our other securities, which

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tend to be riskier and less liquid than Treasury bills. In this paper, we perform a comprehensive set of empirical tests to determine which financial market instrument—or combination of instruments—forecasts the federal funds rate the best at various horizons. Those instruments that have the highest predictive power for the federal funds rate are taken to be the best measures of monetary policy expectations.

We find that all of the financial market instruments in our study provide forecasts that are clearly superior to those of standard time series models.[1] Among our financial market securities, we find that federal funds futures dominate all of the others for predicting changes in the federal funds rate at horizons out to six months. For longer forecast horizons, we find that, perhaps surprisingly, the predictive power of many of the instruments we consider is very similar. Even at these longer horizons, though, the predictive power of these financial market instruments is substantial, with R^2 of about 40 percent for federal funds rate changes.

The superior forecasting performance of federal funds futures at horizons of one to six months may in part reflect that they are explicitly linked to the federal funds rate. However, an explicit link does not necessarily imply that these instruments will provide better forecasts. For example, to the extent that federal funds futures are less liquid than other securities, then the forecasts they provide might be expected to perform more poorly, due to the wedges introduced by larger transaction costs (bid-ask spreads, "slippage" of price against large orders) and the greater risks associated with being unable to adjust or unwind a position quickly in response to incoming news. This was arguably the case both for CPI futures in the 1980s and for Treasury inflation-indexed securities (TIPS) in the first few years after their introduction in 1997: Despite being explicitly linked to CPI inflation, both securities were generally regarded as providing poor measures of inflation expectations due in part to their low level of liquidity.[2] Moreover, even though the other instruments we consider are not explicitly linked to the federal funds rate, they

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[1] Piazzesi and Swanson (2004) also find that federal funds futures dramatically outperform random walk and AR(1) forecasts. Evans (1998) shows that federal funds futures dominate forecasts from an estimated Taylor-type rule.
[2] See Sack and Elsasser (2004) for data and a discussion regarding the liquidity of the TIPS market in its early years and the effects of liquidity on the prices of those instruments. CPI futures were introduced on the Coffee, Sugar, and Cocoa Exchange in June 1985 but were delisted in April 1987 due to extremely low trading volumes and open interest. However CPI futures were reintroduced on the Chicago Mercantile Exchange in February 2004, as the liquidity and demand for TIPS has ballooned.

are extremely close substitutes, so that the linkage to federal funds rate expectations should be very tight. This makes them prime candidates for improving or even dominating forecasts based on federal funds futures alone.

Our results have important implications for market-based measures of monetary policy shocks, or the surprise component of monetary policy announcements. In many of the papers using market-based measures of policy expectations, policy shocks are measured by revisions to near-term expectations of the federal funds rate at the time of policy decisions. Based on our findings, it appears that the best measure of shocks to the immediate policy setting would be based on federal funds futures rates, as in the approach described by Kuttner (2001).

One potential shortcoming of such a measure, as also discussed by Kuttner (2001), is that shocks to the immediate policy setting can be influenced by shifts in the timing of policy actions that have little consequence for the expected course of monetary policy beyond the horizon of a few weeks. Such policy surprises would presumably have limited effects on asset prices or the economy. We therefore compute an alternative measure of policy shocks based on the rates on federal funds and eurodollar futures with slightly longer horizons. This new measure captures changes to the expected near-term policy path rather than to the immediate policy setting, and hence it is less influenced by the timing of policy actions.

The remainder of the paper proceeds as follows. Section 2 provides an introduction to each of our financial market instruments and discusses its risk, liquidity, and available maturities. Section 3 derives our estimation framework and discusses the methodology. Section 4 estimates the forecasting power of each of our financial market instruments for the federal funds rate and the estimated average risk premium for each instrument. It also shows that the predictive power of the financial instruments clearly dominates that of a Bayesian VAR. Section 5 traces out the implications of these results for the measurement of monetary policy shocks and suggests an alternative shock measure that is less susceptible to surprises in the exact timing of FOMC decisions. Section 6 concludes. Two appendices provide technical details of our financial market instruments and of our benchmark Bayesian VAR estimation methodology.

2. Data

Expectations about the near-term course of monetary policy are an important determinant of most short-term market interest rates. This relationship is very explicit in some cases, such as for federal funds futures, which are contracts where the payout on the instrument is directly linked to the realized level of the federal funds rate. In other cases the relationship arises because investors can substitute between different strategies for obtaining short-term returns. In this section we review a number of market interest rates that could be used to measure monetary policy expectations. The discussion touches on characteristics of the underlying instruments that might influence their information content, including the liquidity of the instruments and the potential size of the risk premia that also influence these rates. For additional details see the Appendix to this paper and Stigum (1990).

Term Federal Funds Loans. The federal funds rate—the policy instrument of the Federal Reserve—is the rate at which banks make unsecured loans to one another on an overnight basis. But banks can also borrow and lend to one another for longer periods in the federal funds market. The rates on these longer-term loans, or term federal funds rates, should provide information about expected future levels of the overnight federal funds rate, given the ability of banks to substitute between locking in a longer-term rate for borrowing (lending) and rolling over overnight borrowing (lending) over the same horizon. Since these loans are unsecured, they are among the riskier instruments we consider—and hence they may embed a larger credit risk premium than that found in overnight federal funds loans. The market for loans with maturities of up to six months is reasonably active and liquid (though nowhere near the levels for the overnight federal funds market), but there is virtually no activity beyond that horizon.

Federal Funds Futures. In 1988, the Chicago Board of Trade (CBOT) introduced federal funds futures contracts. These contracts have a payout at maturity based on the average effective federal funds rate that is realized for the calendar month specified in the contract. Thus, the price of these securities is closely linked to financial market expectations for the average

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federal funds rate for the month in question.[3] The counterparty credit risk in these contracts is relatively small, given that the CBOT requires parties to mark contracts to market value (and thereby realize gains and losses) every day and to maintain a minimum collateral balance to cover any losses that may occur on subsequent days. Over most of our sample, federal funds futures contracts were extremely liquid at expirations out to three months and still fairly liquid out to five or six months, but liquidity dropped off sharply at horizons beyond that. However, in the past few years, liquidity and open interest in federal funds futures has soared, with significant liquidity extending out even to nine or ten months.

     Term Eurodollar Deposits. Term eurodollars are dollar-denominated time deposits held at financial institutions outside the United States, particularly London. As with term federal funds, these loans are unsecured, and thus suffer from some probability of default. Moreover, the set of participants in the eurodollar market may differ in credit quality from those in the term federal funds market, which could potentially drive an additional wedge between eurodollar rates and the corresponding term federal funds rate. Nevertheless, many large banks do actively substitute between domestic deposits and eurodollar deposits, suggesting that the linkage is fairly tight. Eurodollar deposit maturities range from overnight to several years, although volumes fall off considerably after one year—indeed, the British Bankers' Association does not provide quotes for eurodollar deposit rates (or LIBOR rates) for maturities longer than one year.

     Eurodollar Futures. Eurodollar futures have traded on the Chicago Mercantile Exchange (CME) since 1981 and for many have years have been the most actively traded futures instruments in the world. The contracts have a payout at maturity based on the three-month LIBOR rate that is quoted on the contract's expiration date. As with federal funds futures, the counterparty credit risk is relatively small, due to daily marking-to-market and collateral requirements. Contracts expiring in March, June, September and December are available out to

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[3] More specifically, the value of the contract at expiration is equal to *100-r*, where *r* is the average effective federal funds rate for the expiration month (this quoting convention makes the prices of these contracts closely match those of Treasury bills, although the linearity of the *100-r* formula removes the "convexity premium" that arises from Jensen's inequality in Treasury bills). Eurodollar futures contracts also follow the *100-r* quoting convention.

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horizons of ten years, although liquidity tends to decline at longer horizons.[4] Volume and open

interest are exceptionally high, however, for contracts expiring over the first several years. Of

course, the value of these contracts is directly tied to LIBOR rather than to the federal funds rate,

and hence the success of these contracts for predicting U.S. monetary policy depends, as with

term eurodollars, on the extent to which LIBOR tracks the federal funds rate in the markets.

     Treasury Bills. U.S. Treasury bills are among the safest and most liquid securities in the

world. At various times, the U.S. Treasury has issued bills with maturities ranging anywhere

from one month to one year, but it has only consistently offered three-month and six-month

securities over our sample period. Treasury bills are viewed as being essentially free of default

risk and have some tax advantages (they are not taxed at the state level), while the federal funds

rate is a private short-term interest rate that has some default risk and no tax advantages, which

introduces a potential shortcoming of bill rates as a predictor of future federal funds rates.

Nevertheless, substitution between these short-term rates is extensive and the linkage between

them is thought to be very tight.

     Commercial Paper. Commercial paper (CP) is unsecured debt with maturity shorter than

270 days issued by investment-grade corporations. We only consider the highest-grade (A1/P1)

class of commercial paper in our analysis below. As with term federal funds and eurodollars,

these loans are subject to some probability of default; however, the probability of default is lower

for CP because issuers are typically required to have a committed line of credit from a major

financial institution that can be used to repay lenders in an emergency. The U.S. CP market is

larger even than the Treasury bill market, but almost all of the activity lies in direct placements,

with very thin secondary market trading. CP issuance is concentrated at maturities of less than

90 days, with an average maturity of around 30 days. The linkage between CP and federal funds

arises because investors can substitute between holding CP and making federal funds loans (or

holding other short-term assets whose rates are influenced by the federal funds rate).

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[4] The CME offers futures contracts for the other months once they are within six months of expiration. However, liquidity in those contracts is well below those of the quarter-end months. In addition, the CME offers futures on one-month Libor rates with monthly expirations. However, these contracts also are less liquid. We do not consider these contracts in this paper.

3. Empirical Specification

The ability of investors to substitute between different financial market instruments suggests that the rate of return $r_{t,t+k}^m$ on a market instrument m from day t to day $t+k$ is equal to the expected rate of return from an investment strategy of rolling over overnight loans in the federal funds market from day t to day $t+k$, plus a risk premium $\rho_{t,t+k}^m$:

$$r_{t,t+k}^m = E_t\left[\prod_{j=t}^{t+k-1}(1+ff_j)-1\right]+\rho_{t,t+k}^m \ , \tag{1}$$

where ff_j is the overnight federal funds rate on day j. One may derive equation (1) directly from standard asset pricing theory—see, for example, Campbell, Lo, and MacKinlay (1997) for a general analysis and Gürkaynak, Sack, and Swanson (2002) for a specific derivation.[5]

We rearrange terms in equation (1) to arrive at the following regression equation:

$$\bar{\bar{ff}}_{t,t+k} = \alpha + \beta \, r_{t,t+k}^m + \varepsilon_t \,, \tag{2}$$

where, to simplify notation, we let $\bar{\bar{ff}}_{t,t+k} = \left[\prod_{j=t}^{t+k-1}(1+ff_j)-1\right]$ denote the (compounded) return to the strategy of rolling over federal funds loans and where the risk premium $\rho_{t,t+k}^m$ has been included in the regression residual (with its average level incorporated into the constant). Equation (2) is a standard interest rate forecasting regression that has been widely used in the literature. We will be interested in particular in the R^2 and root-mean-square forecast error (RMSE) from regression (2), as these directly measure the usefulness of our various financial market instruments for forecasting the federal funds rate.

A common assumption in the literature, referred to as the "expectations hypothesis," is that the risk premium $\rho_{t,t+k}^m$ is constant over time and thus depends only on the security m and its maturity k. We do not require this assumption for this paper, since we are interested in the

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[5] Note that the risk premium ρ, which is measured in (1) and (2) relative to the federal funds rate, can in principle be negative for some assets, a possibility which we confirm empirically for Treasury bills below. This can happen when an asset's covariance with the stochastic pricing kernel is smaller in magnitude than the federal funds rate's covariance with the kernel.

forecasting performance of regression (2) rather than structural estimates of β. To the extent that

the risk premium $\rho_{t,t+k}^m$ on security m varies over time, it will deteriorate the forecasting

performance of security m in regression (2) (and tend to lead to an estimate of β that is different

from unity to the extent that $\rho_{t,t+k}^m$ is correlated with $r_{t,t+k}^m$) and cause us to favor other financial

market instruments for forecasting the federal funds rate. Thus, we will naturally be led to favor

instruments for which time-varying risk premia are less of an issue. Finally, if we impose $\beta=1$ in

regression (2), then the estimated value of α will be $-\rho$, the (negative of the) average risk

premium on the asset, which we will also report for each financial market instrument.

Two final issues arise in estimating equation (2). First, some of the instruments we

consider are term interest rates (term federal funds, eurodollar deposits, Treasury bills,

commercial paper) while others are futures rates (federal funds futures, eurodollar futures),

which forecast the federal funds rate starting at some future date $t+j$. To be able to make direct

comparisons across the various instruments we consider, we back out the implied *forward* rates

from all of our term interest rates and compare the predictive power across instruments in terms

of their forward rate predictions, as follows. Let $r_{t,t+j,t+j+k}^m$ denote the implied interest rate on

security m on date t for a loan beginning on day $t+j$ and ending on day $t+j+k$.[6] A simple

modification of the analysis above yields the regression equation:

$$\overline{\overline{ff}}_{t+j,t+j+k} = \alpha + \beta\, r_{t,t+j,t+j+k}^m + \varepsilon_t. \tag{3}$$

The second issue that arises in estimating equation (3) is that if the nominal rates of

return in the equation are integrated variables (or nearly so), the estimated coefficients will be

dominated by their long-run relationship (the cointegrating vector), regardless of their short-run

relationships. Since we are primarily interested in their short-run relationships—that is, in the

ability of market rates to predict the federal funds rate over the next several months or quarters—

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[6] See the Appendix for details regarding the construction of forward rates and the quoting conventions on each of
our financial market instruments.

we follow common practice and "stochastically detrend" (2) by subtracting off the current level of the federal funds rate from both sides of the equation:

$$\bar{\bar{ff}}_{t+j,t+j+k} - ff_t = \alpha + \beta\left(r^m_{t,t+j,t+k} - ff_t\right) + \varepsilon_t. \qquad (4)$$

Equation (4) serves as the basis for all of our empirical work, below.[7] Each regression also includes two dummy variables to capture potential systematic spikes in risk premia: a Y2K dummy variable that is nonzero for the forward rate spanning the century date change, and a year-end dummy variable that is nonzero for forward rates spanning the end of any year. The year-end dummy is included because firms sometimes attempt to make their year-end balance sheets look stronger for reporting purposes (they engage in "window dressing"); as a result, firms as a whole may be more willing to hold some assets than others over the year end, which can affect their prices.[8]

4. The Predictive Power of Financial Market Instruments

We now apply regression specification (4) to our various financial market instruments. We begin our sample in 1994, since the FOMC (the Federal Open Market Committee, which is the policymaking body of the Federal Reserve) began explicitly announcing its target for the federal funds rate at that time, and thus there is a potential structural break in financial market forecasting performance beginning with that date.[9] We consider forecast horizons for each security ranging from one month ahead to four quarters ahead, although data availability prevent us from considering some forecast horizons for some securities (as discussed in section 2). The horizons considered for each instrument are summarized in Table 1.

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[7] For federal funds futures, we replace the dependent variable in (4) (the compounded federal funds rate) with the straight arithmetic (i.e., noncompounded) average of the federal funds rate over the expiration month, because this is the basis on which federal funds futures contracts are settled.

[8] The year-end dummy variable is particularly important for commercial paper, as emphasized by Downing and Oliner (2004).

[9] Lange, Sack, and Whitesell (2003) and Swanson (2005) show that financial markets in general have become better at predicting the federal funds rate since the mid-1990s, although this improvement appears to have been gradual rather than a discrete structural break in 1994.

4.1 Results for Monthly Frequency Instruments

We perform our first set of regressions at a monthly frequency, computing one-month forward rates for horizons ranging from one to six months ahead.[10] Unfortunately, eurodollar futures have quarterly expiration dates and our Treasury bill data include only quarterly maturities, so we must exclude these two instruments in this first round.

The performance of each of our financial market instruments in forecasting the federal funds rate is reported in Table 2 and summarized in Figure 1. The figure plots the RMSE (top panel) and R^2 (bottom panel) from regression (4) as a function of the horizon considered, with each line corresponding to a different market instrument.[11] Overall, the ability of all of the securities to predict the federal funds rate is remarkable, with R^2 statistics often falling in the 60 to 75 percent range.

Our results also indicate that federal funds futures dominate all of our other financial market instruments in predicting the federal funds rate at all horizons, with the difference being the most striking at horizons of one to two months.[12] We interpret this result as suggesting that federal funds futures provide the best market-based measure of monetary policy expectations at horizons out to six months. Of the remaining three financial market instruments, term federal funds and term eurodollars have very similar forecasting performance while commercial paper forecasts better than these two at a horizon of one month, about equally at a horizon of two months, and worse at a horizon of three months.

Our findings of a high R^2 for financial market forecasts at all horizons seems at odds with Rudebusch (2002), who reported that R^2 falls to zero rapidly with the forecast horizon. There are

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[10] The observations are monthly and are taken on the next-to-last business day of each month; we avoid using the last business day to reduce any possible month-end or quarter-end effects, such as increased volatility related to end-of-quarter corporate balance sheet management.

[11] All the instruments have a higher R^2 statistic at a two-month horizon than at a one-month horizon. This is due to the fact that there is little systematic variation in the dependent variable to explain at a horizon of only one month—indeed, the next policy meeting is a full three weeks away on average. The RMSE is strictly increasing with the length of the forecast horizon for all of our instruments, as one would expect.

[12] An anonymous referee wondered whether this result was partially due to the fact that federal funds futures are for an arithmetic (uncompounded) average one-month funds rate while our other financial market-based forecasts are for a compounded one-month rate. We have verified that even if we evaluate fed funds futures-based forecasts using the compounded one-month fed funds rate (which, strictly speaking, is an apples-to-oranges comparison), the effect of compounding over a one-month period is small, so that it changes our results only by a tenth of a basis point or less at all horizons, and thus does not change our overall findings.

two reasons for this discrepancy: First, our sample period (1994-2004) is one in which the federal funds rate was generally easier to forecast (Lange et al., 2000, Swanson, 2005) than the late 1980s and early 1990s, which make up a large part of Rudebusch's sample. Second, Rudebusch forecasts forward monthly changes in the federal funds rate (that is, from month $t+n-1$ to $t+n$) and reports R^2 values for those changes, while we report R^2 values for the cumulative change in the funds rate from month t to $t+n$, as in equation (4). This latter measure corresponds as closely as possible to the markets' ability to forecast the funds rate itself in n months' time.

As a benchmark for comparison, the bottom rows of Table 2 report analogous results for a set of Bayesian VAR forecasts of the federal funds rate. The BVAR is based on 12 monthly lags of the funds rate, nonfarm payrolls, and the core CPI, with a prior taken from Robertson and Tallman (2001) and Sims and Zha (1998) that shrinks the coefficients toward independent random walks, toward unit roots more generally, and toward cointegration. As discussed by Sims (1992) and Sims and Zha (1998), Bayesian VARs of this type typically provide superior forecasts of macroeconomic time series relative to standard VARs due to problems of overparameterization and overfitting associated with the latter.[13] To make the time series forecasts as comparable to our financial market forecasts as possible, we use real-time vintage data and real-time (i.e., recursive) estimation of the BVAR at each date t. Additional details of the data, estimation, and forecasting methodology for our BVAR are provided in Appendix B.

As can be seen in Table 2, all of the financial market-based forecasts clearly outperform BVAR-based forecasts of the federal funds rate at all horizons. The *RMSE* statistics range from 25 to 50 percent lower, and the R^2 values are typically three times higher, for the financial market-based forecasts relative to the BVAR forecasts.[14]

Of course, as discussed above, the financial instruments contain risk premia that can drive a wedge between their prices and funds rate expectations. The estimated average risk premia for each instrument are reported in Table 2 and graphed in Figure 2. Federal funds

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[13] This is true for our sample as well—the BVAR forecasts outperform those of a standard VAR (results not reported) due to overparameterization and overfitting of the VAR over our relatively small sample.

[14] The *RMSE* and R^2 reported are for 1994-2004 and R^2 values are for changes in the funds rate from time t to time $t+n$, just as for our financial market instruments; note that a random walk would have an R^2 of 0 by this measure.

futures have by far the smallest risk premia by far of all the financial market instruments we consider.[15] Of the remaining instruments, the average risk premia for commercial paper are consistently smaller than those for term federal funds, which are in turn smaller than the risk premia for term eurodollar deposits.

Note, too, that the hypothesis that $\beta = 1$, which we impose to estimate the risk premia, is generally not rejected for any of our securities, except at the one-month-ahead horizon for securities other than federal funds futures. While time-varying risk premia may be a factor in the poorer forecasting performance of term federal fund loans, term eurodollar deposits, and commercial paper relative to federal funds futures, our results suggest that this variation is not correlated enough with (or large enough relative to) the interest rate spreads on the right-hand side of (4) to drive our estimated coefficients very far from unity.[16]

In Table 3, we investigate to what extent a linear combination of our four financial market instruments might outperform federal funds futures by placing all four financial market instruments on the right-hand side of regression (4). At all horizons, only the federal funds futures rate is ever significant, suggesting that the other securities have little if any additional predictive power. In the bottom panel of the table, for each instrument we perform an "encompassing" test of the joint hypothesis that the coefficients on all the other securities are zero. As is evident from the table, we typically cannot reject the hypothesis that the federal funds futures rate encompasses all of the information contained in the other instruments, while we typically do reject the hypothesis that any of the other securities can stand on their own.[17] These results lend additional support to our conclusion that federal funds futures dominate all of our other market-based measures of monetary policy expectations (and the BVAR) at horizons out to six months.

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[15] The fact that risk premia on these contracts is the smallest on average raises the possibility that it also varies the least over time. This would also be consistent with our finding that fed funds futures have the best forecasting performance across all of our financial market instruments.

[16] Nonetheless, Piazzesi and Swanson (2004) estimate significant time-varying risk premia in federal funds futures and eurodollar futures and report a high correlation of this premium with nonfarm payrolls and credit spreads. Our results here only suggest that this time-variation is not highly correlated with the interest rate spreads on the right-hand side of our forecasting regressions.

[17] We also experimented with the methods for combining forecasts described in Clemen and Winkler (1986). We could not reject the hypothesis that federal funds futures performed as well as those measures.

4.2 Results for Quarterly Frequency Instruments

Our second set of regressions considers instruments that forecast quarterly averages of the federal funds rate at horizons extending out to one year.[18] Of course, moving from monthly to quarterly frequency decreases the number of observations in our sample, but as noted above, two of our financial market instruments (eurodollar futures and Treasury bills) cannot be used to compute forecasts of the federal funds rate over anything finer than a quarterly window.

Results are reported in Table 4 and summarized in Figure 2. Again, all of our financial market instruments clearly dominate Bayesian VAR-based forecasts of the federal funds rate, but this time the forecasting performance across our various financial instruments is more similar, with federal funds futures and term federal funds performing the best at short horizons and term federal funds, term eurodollars, and eurodollar futures all performing about equally well at horizons of three or four quarters. One might worry that this is because all of our instruments forecast poorly at long horizons, but this is not the case—indeed, all three instruments have R^2 values of about 40 percent in regression (4), which is substantial for a one-year-ahead forecast. Again, the hypothesis that $\beta = 1$ is not rejected for any of our securities at any horizon.

One interesting observation that emerges from the table is that commercial paper and Treasury bills forecast relatively poorly in the near term, despite the fact that they have among the smallest average risk premia of all our financial market instruments—indeed, the estimated average risk premium on Treasury bills is highly negative at the one-quarter horizon, reflecting the tax advantages of these securities and a willingness of investors to pay a premium for their unparalleled safety and very high liquidity. This finding highlights the fact that a smaller average risk premium and high liquidity do not necessarily correspond to better forecasting performance.

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[18] For these regressions, we sample the data on the next-to-last business day before the expiration of eurodollar futures contracts (typically about two weeks before the end of the quarter), except for federal funds futures, which we sample on the next-to-last business day of the quarter. Ideally, we would like to synchronize our federal funds futures forecasts with our eurodollar futures forecasts, but this is not possible because federal funds futures always expire at the end of the month and eurodollar futures about two weeks before the end of the quarter.

Table 5 presents results from multivariate forecasting regressions with all of our financial market instruments except federal funds futures on the right-hand side (we omit federal funds futures because we are not able to sample them on the same day with the same horizon as eurodollar futures and the other instruments). In general, no one instrument stands out as dominating or consistently encompassing the others. Although term federal funds rates fare a bit better in the encompassing tests, at the four-quarter-ahead horizon we still cannot reject the hypothesis that any of the three available instruments is a sufficient statistic for the other two. This finding may reflect a stronger tendency of financial markets to price these securities off of one another at longer maturities. Finally, the optimal linear combination of the securities varies dramatically from one column of the table to the next, suggesting that none of these estimated linear combinations will provide forecasts of the federal funds rate that are very robust. Going forward, then, one is probably best advised to use one of these instruments—or at most a simple average of two or three of them—for measuring monetary policy expectations at longer horizons.

5. Monetary Policy Shocks

The results in the previous section indicate that federal funds futures provide useful measures of monetary policy expectations. However, in many applications one is interested in *changes* in policy expectations, such as around FOMC announcements or macroeconomic data releases. Indeed, as noted in the Introduction, changes in market-based measures of monetary policy expectations around FOMC announcements have been used by a number of authors as measures of monetary policy shocks.[19] In this section, we discuss how to measure monetary policy shocks using federal funds futures, given that we found these rates provide the best measure of near-term monetary policy expectations.

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[19] Monetary policy "shocks" defined using the high-frequency financial market data are not meant to correspond exactly to the monthly or quarterly measures of monetary policy shocks one would identify from a VAR, since much goes on over the course of a month or quarter that is not captured by the one-day change around FOMC announcements. Nonetheless, the market-based monetary policy shock measures are intended to capture policy changes that, from the point of view of the private sector and financial markets, are exogenous, and thus correlated with correctly identified structural VAR shocks. See Faust, Swanson, and Wright (2005) for a detailed discussion.

A small complication that arises with federal funds futures is that these rates are based on the average federal funds rate that is realized for the calendar month specified in the contract. Thus, if an FOMC announcement is scheduled to take place on day $d1$ of month t, the implied rate from the current-month federal funds future contract, $ff1$, the day before is a weighted average of the federal funds rate that has prevailed so far in the month, r_0, and the rate that is expected to prevail for the reminder of the month, r_1, plus a risk premium:[20]

$$ff1_{t,d1-1} = \frac{d1}{D1}r_0 + \frac{D1-d1}{D1}E_{t,d1-1}\,r_1 + \rho1_{t,d1-1},$$ (8)

where $D1$ denotes the number of days in month t, $E_{t,d1-1}$ denotes the mathematical expectation conditional on information from day $d1-1$ of month t, and $\rho1$ denotes any risk premium that may be present in the contract. By leading this equation ahead one day and differencing, we can compute the surprise component of the change in the federal funds rate target—that is, $E_{t,d1}r_1 - E_{t,d1-1}r_1$. This measure, which we call $mp1$, is given by:

$$mp1_t = (ff1_{t,d1} - ff1_{t,d1-1})\frac{D1}{D1-d1},$$ (9)

which is the scaled change in the current-month federal funds futures contract around the FOMC announcement, and is the same as that used by Kuttner (2001).[21] Note that to interpret (9) as the surprise change in monetary policy expectations, we need to assume that the change in the risk premium $\rho1$ in this narrow window of time is negligible in comparison to the change in expectations itself. Piazzesi and Swanson (2004) provide some evidence that this assumption is consistent with the data.

Although the policy shocks $mp1$ likely provide the best measure of unexpected changes to the immediate policy setting, they might be affected by shifts in the *timing* of policy actions. For example, financial markets might view a federal funds rate tightening in the near future as

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[20] The federal funds rate expected to prevail over the remainder of the month is typically very close to the target rate expected to prevail. Nevertheless, the market will price in expected deviations between the effective federal funds rate and its target. However, this has no impact on the surprise measures due to the differencing involved, as long as the expected deviations do not change on the day of the FOMC meeting.

[21] For FOMC meetings that occur very late in the month (i.e., in the last seven days of the month), we use the unscaled change in the *next*-month federal funds futures contract to avoid multiplying by a very large scale factor in (8), which could unduly magnify changes in bid-ask spreads or other factors.

very likely, but be unsure as to whether the FOMC will act at the current meeting, or the meeting after. An alternative measure of monetary policy shocks that is less affected by these timing issues can be constructed by applying a similar procedure to measure changes in expectations about r_2, the federal funds rate target that will prevail after the *second* FOMC meeting from now.[22] Let $ff2$ denote the federal funds futures rate for the month containing the second FOMC meeting (typically the three-month-ahead contract). Then

$$ff2_{t,d1-1} = \frac{d2}{D2} E_{t,d1-1} r_1 + \frac{D2-d2}{D2} E_{t,d1-1} r_2 + \rho2_{t,d1-1}. \tag{10}$$

where $d2$ and $D2$ are the day of that second FOMC meeting and the number of days in the month containing that FOMC meeting, respectively, and $\rho2$ denotes any risk premium in the contract. By leading this equation ahead one day and differencing, the change in expectations for the second FOMC meeting, which we call $mp2$, is given by:

$$mp2_t = \left[\left(ff2_{t,d1} - ff2_{t,d1-1} \right) - \frac{d2}{D2} mp1_t \right] \frac{D2}{D2-d2}. \tag{11}$$

Figure 3 compares the two shock measures $mp1$ and $mp2$ in a scatter plot. As is clear in the figure, the two measures are generally very highly correlated with each other, lying along the 45-degree line. However, the shocks differ considerably on a handful of dates, which we interpret as dates on which the FOMC's action was largely a surprise in timing as opposed to a surprise in the level of the federal funds rate going forward.

To investigate this issue further, we perform a simple exercise that decomposes the policy shocks into two components: one that influences the general level of policy expectations (the "level" factor), and one that represents shifts in the timing of policy actions at the two meetings (the "timing" factor). Formally, the decomposition is as follows:

$$\begin{bmatrix} mp1_t \\ mp2_t \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ \alpha & 0 \end{bmatrix} \cdot \begin{bmatrix} level_t \\ timing_t \end{bmatrix}. \tag{12}$$

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[22] Gürkaynak (2005) discusses measuring policy expectations and surprises at horizons farther ahead than the current meeting, and Sack (2004) discusses deriving the expected policy path over a longer horizon.

Note that increases in either factor, *level* or *timing*, push up the current FOMC policy shock $mp1_t$. An increase in *level* results in a shift to the expected level of the interest rate going forward, with the rate after the second FOMC meeting from today going up by an amount α. By contrast, an increase in *timing* has no effect on the level of the federal funds rate expected after the subsequent FOMC meeting, but only on the timing of policy actions across the two meetings.

We solve this decomposition based on the variance-covariance matrix from the observed policy shocks, under the assumption that the two factors are orthogonal. The estimated value of α is 1.11, suggesting that the *level* factor is a nearly parallel shift in the policy outlook. Both types of shocks are sizable: The standard deviation of level shocks is 7.4 basis points, compared to 6.6 basis points for timing shocks. The measure $mp1$ is strongly influenced by these timing shocks, which account for 44 percent of its variance over the sample. The measure $mp2$, by construction, is not influenced at all by the timing shocks.

Note that equation (12) can be inverted to yield *level* and *timing* in terms of the observable $mp1$ and $mp2$:

$$\begin{bmatrix} level_t \\ timng_t \end{bmatrix} = \begin{bmatrix} 0 & 1/\alpha \\ 1 & -1/\alpha \end{bmatrix} \begin{bmatrix} mp1_t \\ mp2_t \end{bmatrix}, \tag{13}$$

which, since we estimate $\alpha \approx 1$, corresponds very closely to the "rule of thumb" definition of level and timing components of monetary policy announcements used by Bernanke and Kuttner (2005).

Figure 4 plots a time series of the realized values of these two factors since 1994. One observation that stands out is that timing shocks were more sizable early in the sample, particularly in 1994 and 1995. This finding might reflect the shift in the behavior of the FOMC beginning in 1994, when it began to make policy moves predominantly at FOMC meetings. The results suggest that it might have taken market participants some time to fully recognize this shift in behavior.[23] In recent years, some of the largest timing surprises have taken place at

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[23] Because of its simple structure, the decomposition does not always capture the correct interpretation of market developments. For example, the FOMC easing in July 1995 was apparently viewed as suggesting that additional policy actions would be forthcoming. However, because α is estimated to be close to 1, the decomposition

intermeeting policy moves. Indeed, two of the three sizable timing shocks in 2001 took place on January 3 and September 17.

6. Conclusions

Three notable results emerge from this paper. First, the financial market instruments we consider all provide forecasts of the federal funds rate that clearly dominate standard time series forecasts. Root-mean-squared-errors for our financial market-based forecasts are typically about half the size of time series forecasts, and the R^2 for funds rate changes is dramatically higher.

Second, federal funds futures dominate other market-based measures of monetary policy expectations at horizons out to six months. Their predictive power for the future federal funds rate is higher, their average risk premium is lower, and we cannot reject the hypothesis that they encompass the information contained in all of our other market-based forecast measures combined.

Third, for horizons of six months to one year, term federal funds, term eurodollars, and eurodollar futures all seem to forecast about equally well. This latter finding may partly reflect the degree to which these financial markets are integrated with one another.

These findings have important implications for the computation of monetary policy shocks. For changes in the very near-term stance of policy, our results support measures based on federal funds futures. However, we presented some statistical evidence that shocks computed from the current-month federal funds futures contract may be influenced by changes in the *timing* of policy actions that do not influence the expected course of the federal funds rate beyond a horizon of about six weeks. We thus presented an alternative shock measure that captures changes in market expectations of the course of monetary policy over slightly longer horizons, which may be more useful for many purposes.

It is our hope that this paper will serve as a reference and encourage the use of market-based measures of monetary policy expectations, including in particular the use of these

interprets the market response as a large negative shift in the path factor and a large positive shift in the timing factor.

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instruments to compute monetary policy surprises around FOMC announcements and changes in market expectations for monetary policy in response to other macroeconomic data and news releases.

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Appendix A: Details on Quoting Conventions and Forward Rate Calculations

The market rates used in the analysis differ in the details of their quoting conventions, maturity, and time to settlement, as described in the following table:

Description of Market Quotes

Instrument	Quote Basis	Day Count	Maturity	Settlement
Term Federal Funds Loans	Investment	360	1-12 calendar months	t+2
Federal Funds Futures	*	*	*	*
Eurodollar Deposits	Investment	360	1-12 calendar months	t+2
Eurodollar Futures	**	**	**	**
Treasury Bills	Coupon-equivalent	365	13, 26 weeks	t+1
Commercial Paper	Discount	360	30, 60, 90 days	t
Overnight Federal Funds	Investment	360	1 day	t

* Based on the average value of the overnight federal funds rate over a month.
** Based on the value of the eurodollar deposit rate at expiration.

For example, the interest rate quoted on an *investment* basis is given by the formula

$$r^i = \frac{I}{100} \cdot \frac{360}{M} \tag{A.1}$$

where I denotes the dollar amount of interest to be paid at maturity per \$100 loaned and M is the number of days to maturity of the loan (and note that this quote is, by convention, based on a 360-day year). By contrast, the interest rate quoted on a *discount* basis is given by

$$r^d = \frac{100 - P}{100} \cdot \frac{360}{M} \tag{A.2}$$

where P is the price of the security per \$100 face value. The interest rate on a Treasury bill quoted on a *coupon-equivalent* basis is given by

$$r^{ce} = \frac{100 - P}{P} \cdot \frac{365}{M} \tag{A.3}$$

To make our financial market instruments comparable to one another, we first convert all of the quoted rates (including the overnight federal funds rate) to the equivalent interest rate expressed as a textbook 365-day rate compounded daily, i.e. $(1+r)^{M/365}$.

A second complication arises from small differences in the time to maturity of our various instruments. For example, one-month term federal funds loans and eurodollar deposits mature on the same calendar day in the subsequent month, and thus the exact horizon covered can vary from 28 to 31 days. In contrast, "one-month" commercial paper always has a maturity of 30 days. To account for this, in computing the dependent variable of the regressions, we construct the compounded overnight federal

funds rate return ($\overline{\overline{ff}}_{t,t+k} = \prod_{j=t}^{t+k-1}(1+ff_j)-1$) separately for each market instrument, in each case exactly

matching the horizon spanned by that instrument.

      The third complication that arises is differences in time to settlement—the number of days between when the agreement to make a loan is finalized and when the money is actually transferred from the lender to the borrower.[24] As shown in the table, those procedures range from same-day settlement (*t*) to two-day settlement (*t+2*). We also adjust our dependent variable to take into account these differences, although this still leaves a small discrepancy in the comparison of the instruments. For example, term federal funds loans forecast the overnight federal funds rate beginning two business days forward, while commercial paper forecasts the overnight federal funds rate beginning the same day. This gives a slight advantage to commercial paper. By design, federal funds futures forecast the overnight funds rate over a fixed calendar month. To make their horizon comparable to two-day settlement, we take our monthly quotes on the second-to-last business day of the month.

      Finally, we construct forward rates from term rates. For concreteness, consider calculating the one-month forward rate beginning two months ahead, denoted *fwd*. The forward rate is defined by the following equation:

$$\left(1+r3\right)^{d3/365} = \left(1+r2\right)^{d2/365}\left(1+fwd\right)^{(d3-d2)/365}, \tag{A.3}$$

where *r2* and *r3* are the two- and three-month term rates, respectively, and *d2* and *d3* are the number of days covered by those rates. Note that the day counts *d2* and *d3* will vary across instruments and across time, given the maturity differences discussed above.

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[24] Note that the maturity of the loan is unaffected by the time to settlement, i.e., a 91-day loan with t+2 settlement begins on day t+2 and ends on day t+93.

Appendix B: Bayesian VAR Data, Estimation, and Forecasting Methodology

To compute time series forecasts of the federal funds rate in section 4, we use a Bayesian VAR, since these have been found by Sims (1992) and others to provide better forecasts of typical macroeconomic time series than standard VARs or univariate autoregressions. In this appendix, we provide the details regarding the data, estimation, and forecasting methodology for the BVAR we employ.

Data

We base our BVAR on three variables: the federal funds rate, nonfarm payrolls, and the core CPI. We experimented with including additional variables, such as a monthly GDP series or monetary aggregates, but these never resulted in noticeable improvements in the federal funds rate forecasts over our 1994-2004 sample.

We begin our sample in January 1985. Many authors (e.g., Bernanke and Mihov, 1998) have estimated one or more structural breaks in monetary policy in the early 1980s, so to reduce the possibility of specification error we begin our estimation after the last of these estimated breakpoints and after the end of the Volcker disinflation of the early 1980s. We also experimented with extending the estimation period back to about 1960, but this never led to noticeable improvements in the federal funds rate forecasts over the 1994-2004 period.

At the end of each month t, the federal funds rate for month t is known, but the level of nonfarm payrolls and the core CPI is only known for month t-1 due to lags of a few weeks in the release of these statistics. To make the information sets underlying our BVAR forecasts as comparable as possible to those underlying our financial market forecast data, we use values of the federal funds rate through date t and of nonfarm payrolls and the core CPI through date t-1 in the BVAR. Moreover, we use the real-time vintage of these data series. Core CPI is not revised (except on rare occasion) and thus is known in real time, but we use the level of nonfarm payrolls as it was first reported, rather than the final revised value that may not have been computed by the BLS until several months or even years after the fact.

Estimation

We experimented with estimating the BVAR both in levels and in changes, and found that the latter performed much better for forecast horizons of six months or less. In particular, we used the month-to-month first-difference of the federal funds rate, the year-on-year log change in the core CPI, and the year-on-year log change in nonfarm payrolls. We used the year-on-year change for the latter two variables because the month-to-month changes in those series tend to be very noisy, which would tend to bias coefficients downward.

For monthly data, we estimated the BVAR on 12 lags using a prior taken from Sims and Zha (1998) and Robertson and Tallman (2001). In particular, we used a Normal-Flat prior with the seven hyperparameters discussed in Robertson-Tallman set as follows: μ_1 (overall scale) = 1, μ_2 (strength of independent random walks prior) = .5, μ_3 (strength of prior on intercept) = 1, μ_4 (decay rate on lags) = 5, μ_5 (strength of independent unit roots prior) = 5, and μ_6 (strength of cointegration prior) = 5.[25] We

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[25] We are indebted to Ellis Tallman for providing us with Matlab code for estimating BVARs of this type and for helpful discussions regarding reasonable hyperparameter values for our particular sample and application.

experimented with values for these hyperparameters quite a bit and found that our forecasts and results were very robust to these changes.

For quarterly data (Table 4) with a forecast horizon of 1-2 quarters, we estimated the BVAR in first-differences, as described above, using 4 lags with the seven hyperparameters of the Normal-Flat prior set as follows: $\mu_1 = 1$, $\mu_2 = 3$, $\mu_3 = 1$, $\mu_4 = 2$, $\mu_5 = 0$, and $\mu_6 = 0$. For forecast horizons of 3-4 quarters, we found that a BVAR in levels performed substantially better, so we estimated the BVAR in levels (log-levels for nonfarm payrolls and the core CPI) and set: $\mu_1 = 1$, $\mu_2 = 5$, $\mu_3 = 1$, $\mu_4 = 1$, $\mu_5 = 0$, and $\mu_6 = 0$. Note that for quarterly data, we found that the additional "unit root" and "cointegration" hyperparameters only hurt forecast performance relative to a more standard Minnesota-style specification.

At each date t from January 1994 through November 2004, we re-estimate the BVAR on data running from 1985 through t, taking account of the data availability and real-time vintage issues discussed above. Thus, our time series forecasts are based on information that mirrors as closely as possible the information underlying our financial market data.

Finally, it is worth noting that, despite our use of real-time data and recursive estimation, all of our BVAR forecasts have benefited from hindsight through our choice of specification and hyperparameter values. Thus, our BVAR forecast results should probably be regarded as something of an ideal time series-based forecast that would have been very difficult to actually achieve in real time. The fact that our financial market-based forecasts still compare so favorably to the BVAR-based forecasts is a further sign of their high quality.

Forecasting

Our forecasts are computed as one would compute forecasts from a standard VAR. At each date t, we estimate a coefficient matrix B for the BVAR and then compute our forecasts for x_{t+1}, x_{t+2}, etc. by projecting the system forward from date t, so that $\hat{x}_{t+1} = Bx_t$, $\hat{x}_{t+2} = B^2x_t$, etc. For those forecasts that were done in first-differences for the federal funds rate, we arrive back at a funds rate level forecast by cumulating the first-difference forecasts forward.

Table 1: Data Description

Instrument	Horizon Covered
Term Federal Funds Loans	1 to 12 Months
Federal Funds Futures	1 to 6 Months
Term Eurodollar Deposits	1 to 12 Months
Eurodollar Futures	1 to 4 Quarters
Treasury Bills	1 to 2 Quarters
Commercial Paper	1 to 3 Months

Notes: Data for federal funds futures are from CBOT, eurodollar futures from CME, term federal funds from Bloomberg, term eurodollar deposits from the British Bankers Association, constant-maturity Treasury Bills from the U.S. Treasury Dept., and commercial paper from the Federal Reserve's H.15 data release. Before 1997, the commercial paper data is based on a survey of dealers. See text and Appendix A for details.

Table 2: Monthly Regressions

$$\overline{ff}_{t+j,t+j+k} - ff_t = \alpha + \beta \left(r^m_{t,t+j,t+j+k} - ff_t \right) + \varepsilon_t$$

	α	β	RMSE (bp)	R^2	p-value, $H_0: \beta=1$	average risk premium (bp), $\beta=1$ imposed
Term Federal Funds:						
One-month	-.019 (-0.74)	0.69 (8.16)	13.1	.52	.00	10.2 (9.03)
Two-month	-.141 (-3.29)	0.93 (10.04)	19.3	.65	.43	16.9 (7.21)
Three-month	-.242 (-3.30)	1.00 (8.01)	25.7	.69	.97	24.0 (6.75)
Four-month	-.315 (-2.89)	1.12 (6.29)	36.2	.64	.49	25.0 (4.47)
Five-month	-.390 (-2.61)	1.12 (5.84)	46.1	.60	.54	31.2 (4.08)
Six-month	-.432 (-2.00)	1.04 (4.00)	59.2	.51	.87	40.1 (3.37)
Federal Funds Futures:						
One-month	-.016 (-1.38)	0.94 (17.86)	9.1	.73	.24	2.6 (3.13)
Two-month	-.077 (-2.51)	1.06 (12.05)	15.6	.75	.51	6.1 (3.23)
Three-month	-.124 (-2.20)	1.11 (8.75)	24.2	.71	.40	8.6 (2.47)
Four-month	-.177 (-2.02)	1.14 (6.79)	34.5	.66	.41	12.1 (2.23)
Five-month	-.240 (-1.86)	1.14 (5.58)	45.0	.60	.50	17.2 (2.15)
Six-month	-.305 (-1.68)	1.12 (4.52)	56.6	.54	.64	23.7 (2.15)
Eurodollar Deposits:						
One-month	-.065 (-2.15)	0.77 (8.27)	13.0	.54	.01	13.3 (12.10)
Two-month	-.195 (-4.06)	0.97 (9.86)	18.9	.66	.73	20.9 (9.14)
Three-month	-.307 (-3.83)	1.07 (8.00)	25.8	.69	.61	27.1 (7.63)
Four-month	-.367 (-3.08)	1.14 (6.32)	36.0	.64	.45	28.6 (5.26)
Five-month	-.436 (-2.74)	1.14 (5.77)	46.1	.60	.47	33.5 (4.49)
Six-month	-.460 (-2.14)	1.07 (4.17)	58.4	.52	.78	40.9 (3.59)
Commercial Paper:						
One-month	.013 (0.74)	0.72 (11.35)	10.6	.63	.00	5.3 (5.94)
Two-month	-.065 (-1.81)	0.90 (9.63)	18.5	.65	.28	9.7 (4.68)
Three-month	-.145 (-1.94)	0.95 (6.47)	28.4	.61	.73	16.6 (3.92)
Bayesian VAR:						
One-month	--	--	16.9	.18	--	--
Two-month	--	--	29.9	.20	--	--
Three-month	--	--	42.2	.21	--	--
Four-month	--	--	53.7	.21	--	--
Five-month	--	--	65.1	.20	--	--
Six-month	--	--	76.7	.17	--	--

Sample period: 1994:1-2004:12 at monthly frequency, sampled the next-to-last business day of the month; number of observations is 132-n, where n is forecast horizon in months. t-statistics are reported in parentheses and use Newey-West heteroskedasticity- and autocorrelation-consistent standard errors. The BVAR is estimated recursively from 1985:1 to each forecast date t; RMSE and R^2 for the BVAR are for 1994:1-2004:12 and R^2 is for changes from t to $t+n$, just as for the financial market-based forecasts See text for details.

Table 3: Forecasts Using Multiple Financial Market Instruments

Monthly Regressions

| | --- Horizon (months) --- | | | | | |
	1	2	3	4	5	6
Coefficients:						
Term Federal Funds	-0.27	-0.00	0.31	0.27	0.43	0.30
	(-1.08)	(-0.00)	(1.07)	(0.56)	(1.29)	(0.81)
Federal Funds Futures	1.14	1.29	0.85	0.77	0.48	0.92
	(7.13)	(6.14)	(3.04)	(2.17)	(1.42)	(1.97)
Eurodollar Deposits	0.06	-0.13	0.13	0.10	0.23	-0.10
	(0.26)	(-0.49)	(0.53)	(0.19)	(0.46)	(-0.26)
Commercial Paper	0.03	-0.09	-0.18	--	--	--
	(0.24)	(-0.51)	(-1.28)			
Encompassing Tests (p-value):						
Term Federal Funds	.000	.000	.002	.022	.014	.048
Federal Funds Futures	.176	.650	.007	.621	.237	.662
Eurodollar Deposits	.000	.000	.000	.067	.071	.000
Commercial Paper	.000	.000	.000	--	--	--

The note to Table 2 applies. Regressions include all four financial market instruments on the right-hand side. Encompassing tests are for the joint restriction that all other financial market instruments in the regression have a zero coefficient.

Table 4: Quarterly Regressions

$$\overline{ff}_{t+j,t+j+k} - ff_t = \alpha + \beta\left(r^m_{t,t+j,t+j+k} - ff_t\right) + \varepsilon_t$$

	α	β	RMSE (bp)	R^2	p-value, $H_0: \beta=1$	average risk premium (bp), $\beta=1$ imposed
Term Federal Funds:						
One-quarter	-.129 (-3.67)	1.00 (11.64)	14.9	.82	.97	12.9 (5.71)
Two-quarter	-.348 (-2.33)	1.08 (5.42)	42.8	.67	.70	30.6 (3.01)
Three-quarter	-.555 (-1.68)	1.07 (3.46)	75.4	.52	.82	49.3 (2.61)
Four-quarter	-.854 (-1.61)	1.04 (3.25)	107.3	.40	.90	79.5 (4.15)
Federal Funds Futures:						
One-quarter	-.089 (-2.33)	1.07 (8.29)	14.4	.77	.59	7.2 (3.28)
Two-quarter	-.264 (-1.88)	1.04 (4.72)	44.0	.61	.85	24.4 (2.87)
Eurodollar Deposits						
One-quarter	-.235 (-2.97)	1.14 (7.09)	19.9	.67	.40	17.2 (6.43)
Two-quarter	-.385 (-2.24)	1.08 (4.76)	46.5	.61	.74	33.8 (3.32)
Three-quarter	-.621 (-1.65)	1.11 (3.11)	77.9	.49	.76	52.2 (2.60)
Four-quarter	-.952 (-1.62)	1.09 (3.01)	107.0	.40	.80	81.0 (3.96)
Eurodollar Futures:						
One-quarter	-.231 (-2.98)	1.15 (7.19)	19.8	.69	.36	16.4 (6.46)
Two-quarter	-.385 (-2.26)	1.10 (4.55)	46.1	.62	.67	32.6 (3.20)
Three-quarter	-.588 (-1.57)	1.06 (2.95)	78.9	.48	.87	53.7 (2.53)
Four-quarter	-.897 (-1.55)	1.05 (2.92)	108.3	.39	.90	82.7 (3.88)
Commercial Paper:						
One-quarter	-.109 (-1.77)	.894 (5.09)	21.2	.58	.55	13.9 (4.16)
Treasury Bills:						
One-quarter	.240 (4.85)	0.78 (4.67)	28.2	.33	.20	-23.7 (-4.80)
Two-quarter	-.082 (-0.70)	1.02 (4.81)	45.8	.61	.93	7.7 (0.74)
Bayesian VAR:						
One-quarter	--	--	47.2	.00	--	--
Two-quarter	--	--	85.7	.00	--	--
Three-quarter	--	--	110.0	.13	--	--
Four-quarter	--	--	132.2	.19	--	--

Sample period: 1994:1-2004:4 at quarterly frequency, sampled the next-to-last business day before the expiration of eurodollar futures (about two weeks before the end of the quarter), except for federal fund futures, which are sampled the next-to-last business day of the quarter; number of observations is 44-n, where n is the forecast horizon in quarters. t-statistics are reported in parentheses and use Newey-West heteroskedasticity- and autocorrelation-consistent standard errors. The BVAR is estimated recursively from 1985:1 to each forecast date t; RMSE and R^2 for the BVAR are for 1994:1-2004:4 and R^2 is for changes from t to $t+n$, just as for the financial market-based forecasts See text for details.

Table 5: Forecasts Using Multiple Financial Market Instruments
Quarterly Regressions

	--- Horizon (quarters) ---			
	1	2	3	4
Coefficients:				
Term Federal Funds	1.17 (13.98)	1.82 (5.91)	1.41 (2.38)	0.27 (0.24)
Eurodollar Deposits	-0.76 (-0.59)	-3.82 (-3.18)	-0.52 (-0.46)	0.46 (0.23)
Eurodollar Futures	1.09 (0.88)	2.53 (2.26)	0.15 (0.19)	0.33 (0.18)
Treasury Bills	0.35 (3.18)	0.47 (0.92)	--	--
Commercial Paper	-0.73 (-2.22)	--	--	--
Encompassing Tests (p-value):				
Term Federal Funds	.002	.010	.893	.834
Eurodollar Deposits	.000	.000	.054	.943
Eurodollar Futures	.000	.000	.011	.915
Treasury Bills	.000	.000	--	--
Commercial Paper	.000	--	--	--

The note to Table 4 applies. Regressions include all four financial market instruments on the right-hand side. Encompassing tests are for the joint restriction that all other financial market instruments in the regression have a zero coefficient.
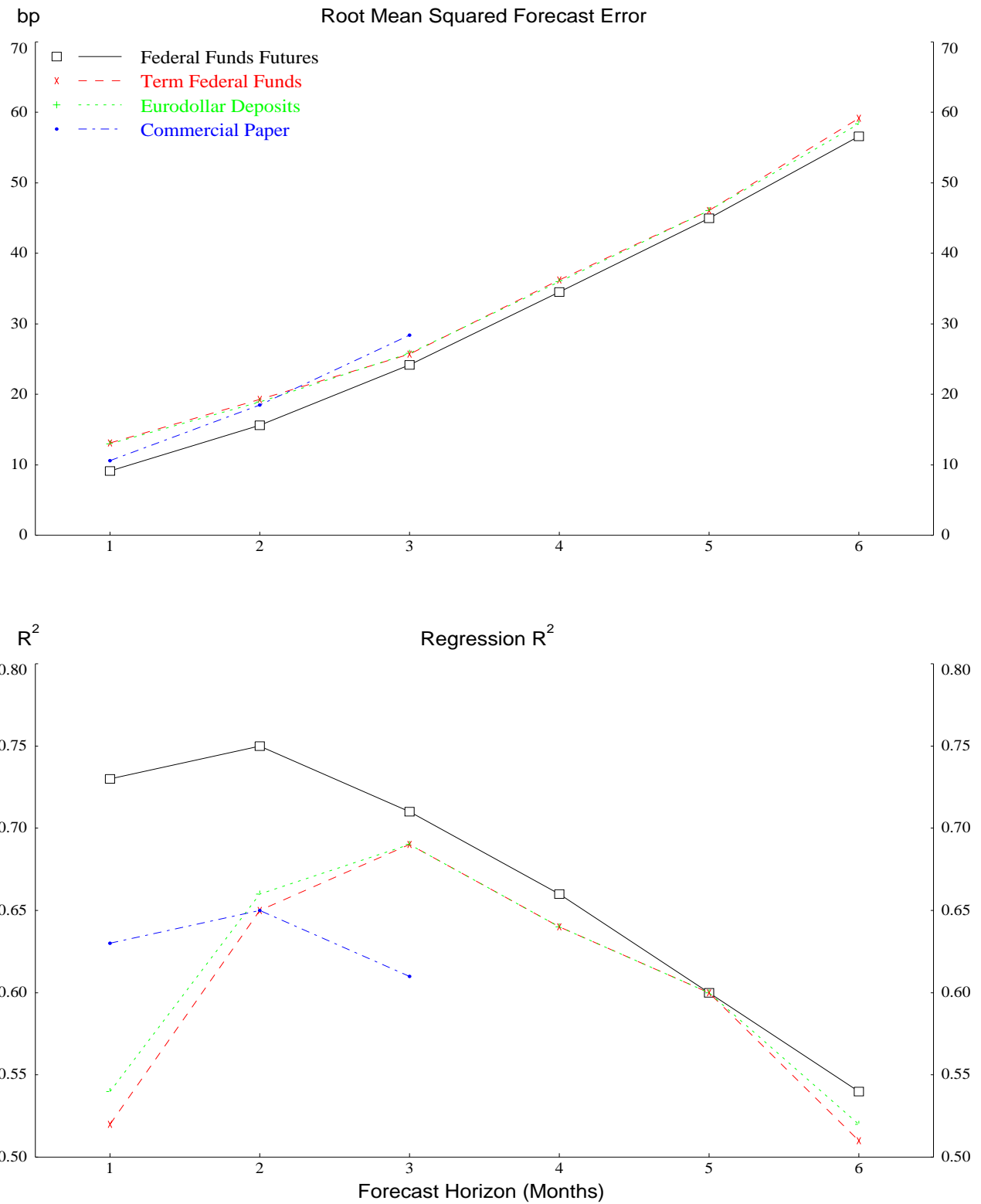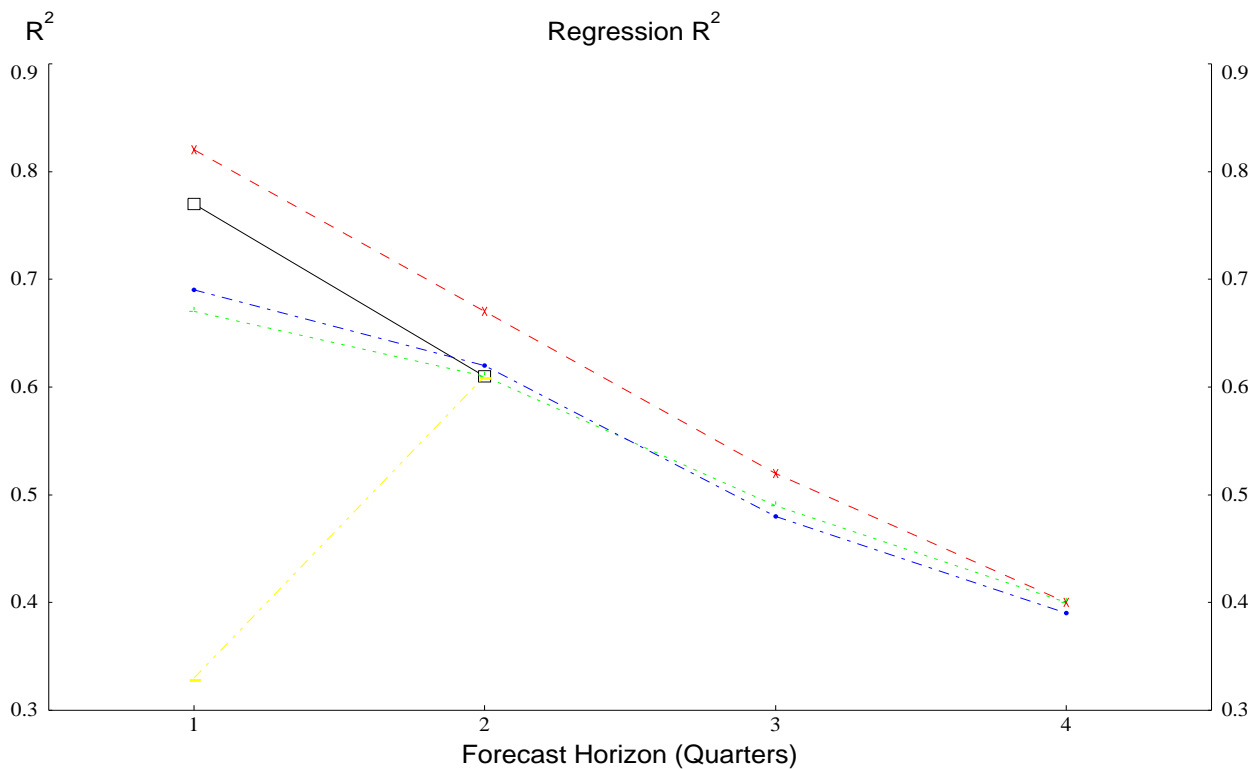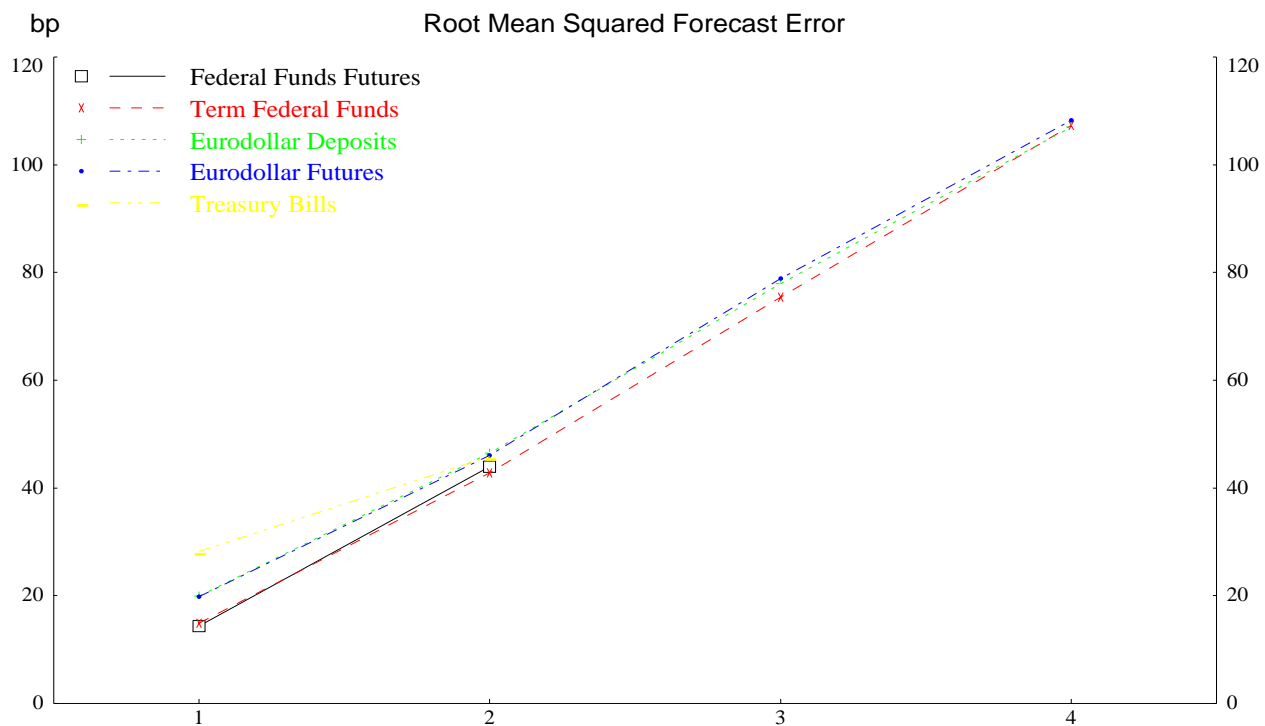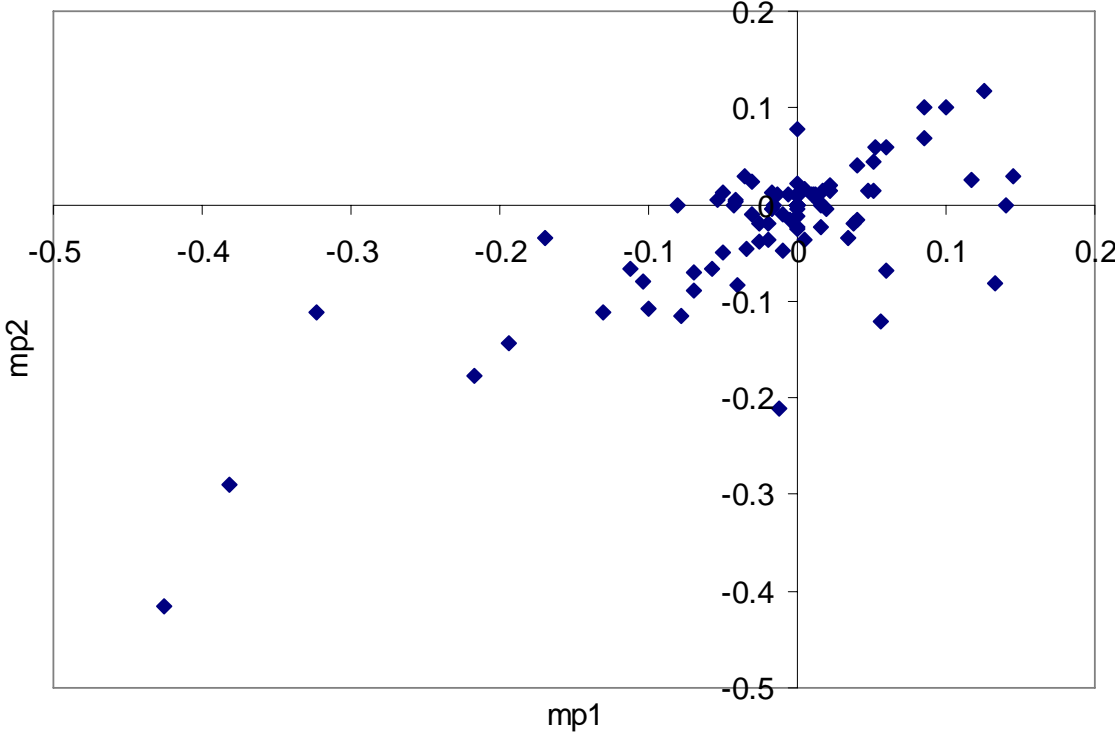
Figure 1 : Monthly Regressions

Root Mean Squared Forecast Error

Regression R^2

Forecast Horizon (Months)

Figure 2 : Quarterly Regressions

Figure 3: Comparison of Monetary Policy Shock Measures
(mp1 vs. mp2)

Figure 4: Decomposition of Monetary Policy Shocks

Feb 1994 to May 1999

June 1999 to December 2004