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Passive Quantitative Easing: Bond Supply Effects through a Halt to Debt Issuance

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Abstract

This article presents empirical evidence of a supply-induced transmission channel to long-term interest rates caused by a halt to government debt issuance. This is conceptually equivalent to a central bank-operated asset purchase program, commonly known as quantitative easing (QE). However, as it involves neither asset purchases nor associated creation of central bank reserves, we refer to it as *passive* QE. For evidence, we analyze the response of Danish government bond risk premia to a temporary halt in government debt issuance announced by the Danish National Bank. The data suggest that declines in long-term yields during its enforcement reflected both reduced term premia, consistent with supply-induced portfolio balance effects, and increased safety premia, consistent with safe assets scarcity effects.

JEL Classification: E43, E47, G12, G13

Keywords: affine arbitrage-free term structure model, safety premia, portfolio balance effects, negative interest rates

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1 Introduction

The literature on asset price effects arising from central bank large-scale asset purchases, commonly known as quantitative easing (QE), has identified two distinct portfolio balance effects tied to financial frictions. One is caused by imperfect asset substitutability derived from the reduced supply of the purchased assets; see Gagnon et al. (2011) and Krishnamurthy and Vissing-Jorgensen (2011), among many others. The other is due to the segmentation of the market for central bank reserves and works through banks' portfolio responses to associated reserves expansions; see Christensen and Krogstrup (2019, 2022). However, when a central bank operates a QE program, it is nearly impossible to distinguish between these two effects empirically as both transmission channels are operating simultaneously.

For separate identification of supply-induced portfolio balance effects—the main transmission channel emphasized in the literature—this paper argues that we need to focus on a halt to government debt issuance. This is so because such a policy is conceptually equivalent to a central bank-operated bond purchase program in that they both reduce the anticipated market supply of government bonds. However, there are two important differences that ensure the stated identification. First and most importantly, there is no creation of central bank reserves and hence no reserve-induced portfolio balance effects by definition. Second, without any active bond purchases by the central bank, there is also no change in the bargaining power between buyers and sellers in the market for government bonds and hence no reduction in bond liquidity risk premia; see Christensen and Gillan (2022). As a consequence, this unique policy is referred to as passive QE.

For empirical evidence on the financial market impact of passive QE, we focus on Denmark, where the government in January 2015 unexpectedly announced a halt to government debt issuance that lasted until October 2015 and, by our estimates, reduced the outstanding amount of Danish government bonds by 29.9 billion Danish krones (about 5 billion U.S. dollars), or about 4.5 percent. The shortfall in issuance was never made up, as the Danish government had sufficient funds in its general account with the Danish National Bank (DNB) for its operations during this period. As a result, this policy permanently lowered the trajectory for the outstanding amount of Danish government debt. This means that effects on long-term bond yields could be anticipated despite the short-lived enforcement of the policy. In addition, Denmark is a near-ideal place for examining the financial market effects of passive QE thanks to its very long-established peg to the euro. This implies that the announcement of the halt to government debt issuance was unlikely to affect investors' expectations about future monetary policy. This effectively rules out the signaling channel as a relevant mechanism behind our findings.

¹Before the launch of the euro in 1999, the Danish krone was pegged to the German mark for many years.

²For a discussion of, and evidence on, the signaling transmission channel of QE for U.S. data, see Christensen and Rudebusch (2012) and Bauer and Rudebusch (2014).

To analyze potential remaining transmission channels in a unified framework, we use the preferred dynamic term structure model of Danish government bond prices identified by Christensen and Hetland (2023, henceforth CH). In addition to providing estimates of standard term premia, this model also accounts for bond-specific safety premia as in Christensen and Mirkov (2022). The underlying mechanism assumes that, over time, an increasing proportion of the outstanding nominal amount is locked up in buy-and-hold investors' portfolios. Given the forward-looking behavior of investors, this lock-up effect means that a particular bond's sensitivity to the market-wide bond-specific risk factor will vary depending on how seasoned the bond is and how close to maturity it is. In a careful study of nominal Treasuries, Fontaine and Garcia (2012) also find a pervasive bond-specific risk factor that affects all bond prices with loadings that vary with the maturity and age of each bond. By observing a cross section of security prices over time, the bond-specific risk factor can be separately identified.

To examine the impact on Danish government bond risk premia from the announced debt halt, we use Danish bond-specific safety and general term premium estimates at monthly frequency covering the period from January 1999 to December 2021. We then regress these series on a dummy variable that is equal to one for the duration of the halt to debt issuance. Since both types of risk premia are likely to have been affected by the European Central Bank's (ECB) public sector bond purchase program (PSPP) ongoing at the time, we include two different measures of their size: one is the collateral scarcity premium of German government bonds, defined as the difference between the ECB deposit facility and the general collateral repo rate for German government bonds; the other is the ECB's holdings of government-backed securities acquired under the PSPP relative to nominal GDP in the euro area.³ Beyond these main policy variables, we control for a variety of additional confounding factors with a total of 15 variables. They serve as proxies for: financial market uncertainty and risk aversion; effects tied to the supply of Danish government bonds; the opportunity cost of holding money; bond market liquidity; variation in the amount of arbitrage capital; credit risk; and differences in the funding costs between Denmark and countries in the euro area.

The results of the regressions show that the average Danish safety premium was 16-21 basis points higher than could otherwise have been anticipated for the duration of the halt to debt issuance. At the same time, the Danish ten-year term premium was reduced 35-68 basis points. Given that the safety premium represents the extra yield investors forgo by holding the very safe Danish government bonds, a higher safety premium is equivalent to a lower absolute yield. Hence, the combined results suggest that Danish government bond yields were significantly lower than they otherwise would have been by between 51 basis points and as much as 89 basis points for the duration of the halt to debt issuance.

Based on these findings we conclude that passive QE works mainly by lowering standard

³Although the ECB also purchased other securities such as corporate bonds and asset-backed securities during this period, we focus on its holdings of government bonds as the relevant measure of substitutes for Danish government bonds.

term premia—a result consistent with standard supply-induced portfolio balance effects as conjectured—but also by lifting bond safety premia, which would be consistent with the scarcity safety premium channel highlighted by Christensen et al. (2023). Furthermore, given that the size of our estimated effects is quantitatively similar to those reported in studies of QE programs in the United States and the United Kingdom,⁴ our results suggest that passive QE may be about as effective at lowering long-term interest rate levels and easing financial market conditions as traditional active QE programs. In particular, this is likely to hold for bond markets with sizable safety premia, where bargaining power is already tilted towards sellers. In that case, the effectiveness of the policy does not depend on effects arising from the liquidity transmission channel of QE, which are likely to be minimal under those circumstances.

In light of the current elevated level of inflation around the world, it is important for policymakers and investors alike to understand the effects of both QE and quantitative tightening (QT), that is, how central bank bond purchases and sales affect bond yields through different risk premia and over the term structure. Given that QT—where it has been implemented—in many ways can be viewed as a passive reversal of previous QE programs by simply letting bonds mature with at most partial reinvestment, we feel compelled to point out the differences and similarities between the passive QE analyzed in this paper and the passive QT alluded to above.

Under passive QT, when government bonds reach maturity, the government issues new long-term bonds to obtain the funds to pay off the holders of the maturing bonds. This produces an upward push on bond yields through the supply-induced transmission mechanism identified in this paper. The central bank then receives its share of these funds and uses it to cancel a matching amount of outstanding reserves. As a result, the banking sector as a whole will see its assets and liabilities reduced by a magnitude equal to the amount of maturing bonds held by the central bank. In response to these exogenous changes to their balance sheets, banks are likely to rebalance their portfolios, which may produce additional reserve-induced portfolio balance effects, as described in Christensen and Krogstrup (2019, 2022). Moreover, if this is taking place in a government bond market like the Danish one in which the bonds can command a safety convenience premium, the added bond supply is likely to put downward pressure on the safety premium through the scarcity channel, as documented in this paper. In summary, passive QT may raise interest rates through two separate portfolio balance channels in addition to the scarcity channel. As such, it has the potential to be even stronger and more contractionary for financial conditions than passive QE.^{5,6}

⁴See Christensen and Rudebusch (2012) for an example.

⁵It is important to note that, thanks to forward-looking behavior on the part of investors, a significant share of the increase in interest rates from passive QT is likely to materialize upon announcement and not when bonds held by the central bank actually mature.

⁶During the 2022-2023 monetary policy tightening cycle in the United States and elsewhere, passive QT coincided with large and rapid increases in conventional policy rates. This concurrence makes it almost

The analysis in this paper relates to several important literatures. Most directly, it contributes to the voluminous literature on the financial market effects of central bank large-scale asset purchases. Second, our results relate to research on financial market convenience and safety premia. Finally, the paper also speaks to the nascent literature about the economic consequences of QT when central banks scale back the size of their balance sheets.

The remainder of the paper is organized as follows. Section 2 provides a detailed description of the Danish halt to debt issuance. Section 3 briefly describes the data, while Section 4 details the no-arbitrage term structure model we use and presents the empirical results. Section 5 examines the effects of the debt halt on Danish bond risk premia. Finally, Section 6 concludes.

2 The Danish Halt to Debt Issuance in 2015

In early 2015, there was extreme market pressure for the Danish krone to appreciate. During the first two months of the year the DNB increased its foreign reserves by 275 billion krones, or more than 40 billion U.S. dollars, an unprecedented amount in such a short period.⁷

The background for this immense pressure was that the Swiss National Bank had discontinued its minimum exchange rate to the euro on January 15, 2015, which resulted in an immediate and dramatic appreciation of the Swiss franc against the euro. In addition, the ECB had announced its first outright QE program on January 22, 2015. Importantly, in that type of market environment, the speculation in favor of the Danish krone could be considered almost risk-free. Either the DNB would be forced to give up the peg to the euro, which would mean that the Danish krone would most likely appreciate strongly against the euro as the Swiss franc had in mid-January, or the peg would be maintained and investors would be able to freely convert their acquired Danish krones back into euros at the existing exchange rate.

Faced with this pressure driven by monetary stimulus from abroad that would clearly not abate in the near term, the DNB unexpectedly announced on January 30, 2015, that the Danish government had decided—following advice from the DNB—to halt debt issuance for the foreseeable future.⁹ The announcement noted that the government expected to have sufficient funds for its operations at least through the end of 2015. Furthermore, it noted that Danish long-term bond yields remained high despite a significant reduction in the DNB's key overnight policy rate to -0.50 percent and outsized purchases of foreign currency. The stated expectation was that the halt would help lower long-term bond yields, which were above their German counterparts and thereby reduce the inflow of foreign currency.

impossible to isolate tightening effects on interest rates from QT during that episode.

⁷See p. 105 in Abildgren (2022).

⁸On February 15, 2015, the Swedish Riksbank introduced negative interest rates and launched its first QE program.

 $^{^9\}mathrm{See}$ https://www.nationalbanken.dk/da/viden-og-nyheder/presse/arkiv/2015/stop-for-salg-af-statsobligationer-30-01-2015

	N	ew issuance		Buybacks	No	Net issuance		
	2015	Avg. 2016-2018	2015	Avg. 2016-2018	2015	Avg. 2016-2018		
January	5,790	7,803	700	3,688	5,090	4,115		
February	_	8,755	375	$5,\!235$	-375	3,520		
March	_	6,953	200	2,928	-200	4,025		
April	_	6,663	400	5,083	-400	1,580		
May	2,000	7,317	3,550	6,153	-1,550	1,163		
June	_	7,807	4,950	4,918	-4,950	2,888		
July	2,500	4,388	3,340	4,765	-840	-377		
August	_	6,607	5,150	3,148	-5,150	3,458		
September	_	7,547	1,215	8,623	-1,215	-1,077		
October	14,180	6,548	6,420	4,637	7,760	1,912		
November	17,330	$7{,}157$	5,405	3,342	11,925	3,815		
December	2,440	3,678	4,695	2,430	-2,255	1,248		
Total, FebSep.	4,500	56,037	19,180	40,855	-14,680	15,182		

Table 1: Changes to the Outstanding Amount of Danish Government Bonds

The table reports the monthly changes to the outstanding amount of Danish government bonds caused by issuance of new bonds and buybacks of existing bonds during 2015 along with the average of the corresponding changes in 2016, 2017, and 2018. The last line reports the net changes for the period from February to September both for 2015 and averaged for the years 2016, 2017, and 2018. All numbers are measured in millions of Danish krones.

During the following spring and summer, financial market flows indeed started to normalize. As a consequence, on August 26, the DNB was able to announce that debt issuance would be resumed as of October 1, 2015.¹⁰ In practice, the halt ended with the issuance of a three-year bond on October 25, 2015.

The DNB serves as the debt manager of the Danish government. In this role, it aims to maintain liquidity in the market for government bonds through frequent reopenings and about as frequent buyback auctions of existing bond series. To get an estimate of the missing volumes of issuance and buybacks during the eight-month period the debt issuance halt was in place, we compare the change in the outstanding volume between February 1, 2015, and September 30, 2015, with the average change during the corresponding period in the years 2016, 2017, and 2018. These numbers are reported in Table 1. We note that, in the February-September period of 2016-2018, the average net issuance amount was 15.2 billion Danish krones. In 2015, the corresponding number shows a net decline in the outstanding amount of bonds equal to 14.7 billion Danish krones as buybacks continued, although at lower volumes compared with the 2016-2018 period. Although uncertain, we take these numbers to suggest that the outstanding amount of Danish government bonds is likely to have been reduced by about 29.9 billion Danish krones thanks to the debt issuance halt. Furthermore, there is no evidence that the government tried to make up for this shortfall by subsequently increasing

 $^{^{-10}\}mathrm{See\ https://www.nationalbanken.dk/da/viden-og-nyheder/presse/arkiv/2015/genoptagelse-af-statsobligationssalg-og-nedsaettelse-af-foliorammer-26-08-2015}$

Bond	4% 11/15-15	2.5% 11/15-16	4% 11/15-17	4% 11/15-19	3% 11/15-21	1.5% 11/15-23	7% 1/10-24	1.75% 11/15-25	4.5% 11/15-39
Mat. (yrs)	0.79	1.79	2.79	4.79	6.79	8.79	9.78	10.79	24.79
1/29-15	-45.1	-39.0	-29.8	-12.6	6.2	27.5	23.1	44.4	95.5
1/30-15	-57.2	-50.3	-38.1	-20.1	0.7	17.2	13.1	33.0	86.9
2/2-15	-81.1	-61.2	-53.3	-35.7	-18.1	2.6	-4.6	13.9	70.6
1-day ch.	-12.1	-11.3	-8.3	-7.5	-5.5	-10.3	-10.0	-11.4	-8.6
2-day ch.	-36.0	-22.2	-23.5	-23.1	-24.3	-24.9	-27.7	-30.5	-24.9

Table 2: Response of Government Bond Yields to Debt Halt Announcement

The table reports the one- and two-day responses of the outstanding Danish government bond yields to the announcement of the halt to debt issuance on January 30, 2015. All numbers are measured in basis points.

Bond	4% 11/15-15	2.5% 11/15-16	4% 11/15-17	4% 11/15-19	3% 11/15-21	1.5% 11/15-23	7% 1/10-24	1.75% 11/15-25	4.5% 11/15-39
Mat. (yrs)	0.22	1.22	2.22	4.22	6.22	8.22	9.21	10.22	24.22
8/25-15	-50.9	-33.7	-19.9	0.8	32.6	63.6	65.0	93.4	139.3
8/26-15	-49.3	-33.2	-19.5	-0.4	30.2	60.5	61.8	90.2	136.5
8/27-15	-48.4	-32.6	-18.9	3.3	32.3	63.8	65.4	93.8	142.7
1-day ch.	1.6	0.5	0.4	-1.2	-2.4	-3.1	-3.2	-3.2	-2.8
2-day ch.	2.5	1.1	1.0	2.5	-0.3	0.2	0.4	0.4	3.4

Table 3: Response of Government Bond Yields to Resumption of Debt Issuance The table reports the one- and two-day responses of the outstanding Danish government bond yields to the announcement of the resumption of debt issuance on August 26, 2015. All numbers are measured in basis points.

its debt issuance. As a result, this unique policy choice appears to have effectively lowered the trajectory for the outstanding amount of government debt permanently. To put the numbers into context, we note that the Danish economy is about 50 times smaller than the U.S. economy. Hence, this would roughly be equivalent to the U.S. Treasury announcing a 250 billion U.S. dollar reduction in the outstanding amount of U.S. Treasury debt.

As a final minor detail, we add that the halt was not fully enforced; there were two small reopening auctions of a single bond (1.75% maturing 11/15/2025) in May and July 2015 to improve liquidity in the government bond market. The liquidity was also maintained through the continuation of the buyback program as already mentioned.

Because the announcement of the debt halt was unexpected and involved notable volumes, it would be reasonable to expect an immediate reaction from bond investors. To explore that conjecture, we examine the one- and two-day reactions of Danish government bond yields to the announcement for the set of bonds outstanding at the time. We report these numbers in Table 2, where we note a moderate immediate reaction lower across the yield curve on January 30, 2015, which was likely tempered because it happened on a Friday. By Monday's close on February 2, 2015, though, we see the full market reaction, which reveals a forceful movement lower in the entire yield curve of about 25 basis points.

To provide a visual perspective, Figure 1(a) shows how the entire Danish government bond yield curve varied during the two-day event window. Crucially, given how low interest rates were already, the forceful immediate reaction to the announcement of the debt halt can be considered to be quite large.

Table 3 reports the one- and two-day yield responses to the announcement of the resump-

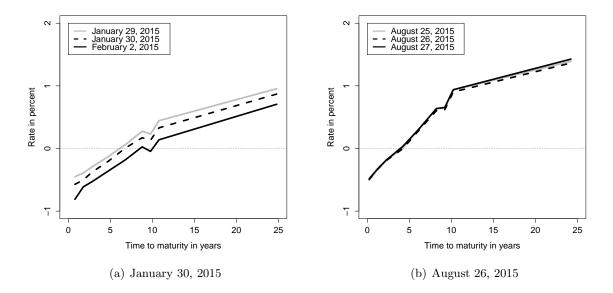


Figure 1: Yield Responses to Debt Halt Announcements

Panel (a) shows the one- and two-day responses of the outstanding Dani

Panel (a) shows the one- and two-day responses of the outstanding Danish government bond yields to the announcement of the halt to debt issuance on January 30, 2015. Panel (b) shows the one- and two-day responses of the outstanding Danish government bond yields to the announcement of the resumption of debt issuance on August 26, 2015. The data are downloaded from Bloomberg.

tion of debt issuance on August 26, 2015. The changes in the government bond yield curve are also shown in Figure 1(b), where we note a very modest, almost indifferent reaction to this announcement, even though a two-day event window still registers the anticipated *positive* uptick in the bond yields.

Figure 2 shows the exchange rate of the Danish krone to the euro since 1999. It reveals that the strong market dynamics in early 2015 in terms of volumes flowing into Danish money markets had little impact on the exchange rate. Thus, the price reaction to the debt halt announcement is entirely limited to interest rates and bond yields.

In our analysis, we are interested in going beyond the immediate market reactions documented above and examine the more persistent effects on Danish bond risk premia from this unique policy choice. In particular, we are interested in understanding whether the resulting reduction in the anticipated amount of outstanding bonds was able to produce any supply-induced portfolio balance effects on Danish term premia. Moreover, in light of the strong findings of QE scarcity effects for an international panel of bond safety premia reported in Christensen et al. (2023), we are also curious to see whether the reduction in the Danish government bond supply impacted the safety premia of Danish government bonds. The rest of the paper is devoted to exploring these questions.

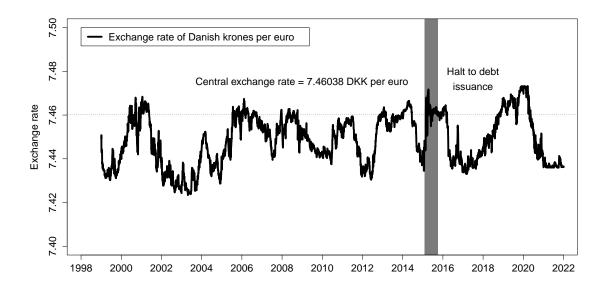


Figure 2: Exchange Rate of the Danish Krone to the Euro

3 Danish Government Bond Data

In this section, we briefly describe our sample of Danish government bond prices downloaded from Bloomberg. We use the same 40 bond prices as in CH observed monthly from January 1999 to December 2021.

Figure 3 shows the Danish government bond prices converted into yield to maturity. Several things are worth noting regarding these yield series. First, there is a trend lower in the general yield level during this period from roughly 6 percent in the early 2000s to around zero by the end of our sample. Second, there is pronounced business cycle variation in the shape of the yield curve around the lower trend. The yield curve tends to flatten ahead of recessions and steepen during the initial phase of economic recoveries. These characteristics are the practical motivation behind our choice of using a three-factor model for the frictionless part of the Danish yield curve, adopting an approach similar to what is standard for U.S. and U.K. data; see Christensen and Rudebusch (2012).

Finally, we note that shorter-term Danish yields turned negative for the first time in 2012 and were firmly in negative territory from summer 2014 when the ECB introduced negative policy rates through the end of our sample. As a consequence, we choose to focus on a model with Gaussian dynamics, which can easily handle negative interest rates.

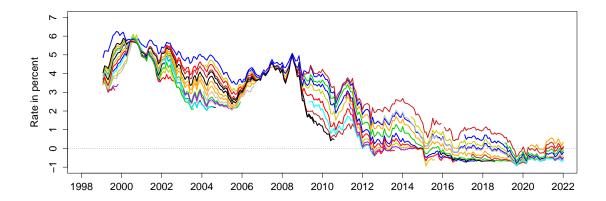


Figure 3: Yield to Maturity of Danish Government Bonds

Illustration of the yield to maturity of the Danish government bonds considered in this paper, which are subject to two sample choices: (1) sample limited to the period from January 31, 1999, to December 31, 2021; (2) censoring of a bond's price when it has less than three months to maturity.

4 Model Estimation and Results

In this section, we first detail the model that serves as the benchmark in our analysis before we describe the restrictions imposed to achieve econometric identification of the model.

4.1 The AFNS-R Model

To begin, let $X_t = (L_t, S_t, C_t, X_t^R)$ denote the state vector of the four-factor model we use. Here, L_t denotes a level factor, while S_t and C_t represent slope and curvature factors. Finally, X_t^R is the marketwide bond-specific risk factor structured as in Andreasen et al. (2021). Given that it is an augmented version of the arbitrage-free Nelson-Siegel models described in Christensen et al. (2011), we refer to it as the AFNS-R model.

The instantaneous risk-free rate is defined as

$$r_t = L_t + S_t. (1)$$

The risk-neutral Q-dynamics of the state variables used for pricing are given by

$$\begin{pmatrix} dL_t \\ dS_t \\ dC_t \\ dX_t^R \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \lambda & -\lambda & 0 \\ 0 & 0 & \lambda & 0 \\ 0 & 0 & 0 & \kappa_R^{\mathbb{Q}} \end{pmatrix} \begin{bmatrix} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ \theta_R^{\mathbb{Q}} \end{pmatrix} - \begin{pmatrix} L_t \\ S_t \\ C_t \\ X_t^R \end{pmatrix} dt + \Sigma \begin{pmatrix} dW_t^{L,\mathbb{Q}} \\ dW_t^{S,\mathbb{Q}} \\ dW_t^{C,\mathbb{Q}} \\ dW_t^{R,\mathbb{Q}} \end{pmatrix},$$

where Σ is a lower-triangular matrix.

Based on the \mathbb{Q} -dynamics above, zero-coupon bond yields preserve a Nelson and Siegel (1987) factor loading structure

$$y_t(\tau) = L_t + \left(\frac{1 - e^{-\lambda \tau}}{\lambda \tau}\right) S_t + \left(\frac{1 - e^{-\lambda \tau}}{\lambda \tau} - e^{-\lambda \tau}\right) C_t - \frac{A(\tau)}{\tau},\tag{2}$$

where $\frac{A(\tau)}{\tau}$ is a convexity term that adjusts the functional form in Nelson and Siegel (1987) to ensure absence of arbitrage (see Christensen et al. (2011)).

Importantly, due to bond-specific premia in the Danish government bond market, individual bond prices are sensitive to the variation in the bond-specific risk factor X_t^R . As a consequence, the pricing of the bonds is not performed with the standard discount function above, but rather with a discount function that accounts for the bond-specific risk:

$$\overline{r}_t^i = r_t + \beta^i (1 - e^{-\lambda^{R,i} (t - t_0^i)}) X_t^R,$$
(3)

where t_0^i denotes the date of issuance of the specific security and β^i is its sensitivity to the variation in the marketwide bond-specific risk factor. Furthermore, the decay parameter $\lambda^{R,i}$ is assumed to vary across securities as well.

As shown in Christensen and Rudebusch (2019), the net present value of one Danish krone paid by bond i at time $t + \tau$ has the following exponential-affine form

$$P_t^i(t_0^i, \tau) = E^{\mathbb{Q}} \left[e^{-\int_t^{t+\tau} \overline{\tau}^i(s, t_0^i) ds} \right]$$

$$= \exp \left(B_1^i(\tau) L_t + B_2^i(\tau) S_t + B_3^i(\tau) C_t + B_4^i(t_0^i, t, \tau) X_t^R + A^i(t_0^i, t, \tau) \right).$$

This implies that the model belongs to the class of Gaussian affine term structure models. Note also that, by fixing $\beta^i = 0$ for all i, we recover the AFNS model.

Now, consider the whole value of the bond issued at time t_0^i with maturity at $t + \tau$ that pays a coupon C annually. Its price is given by t_0^{11}

$$P_t^i(t_0^i, \tau) = C(t_1 - t)E^{\mathbb{Q}} \left[e^{-\int_t^{t_1} \overline{\tau}^i(s, t_0^i) ds} \right] + \sum_{i=2}^N CE^{\mathbb{Q}} \left[e^{-\int_t^{t_j} \overline{\tau}^i(s, t_0^i) ds} \right] + E^{\mathbb{Q}} \left[e^{-\int_t^{t+\tau} \overline{\tau}^i(s, t_0^i) ds} \right]. \tag{4}$$

So far, the description of the AFNS-R model has relied solely on the dynamics of the state variables under the Q-measure used for pricing. However, to complete the description of the model and to implement it empirically, we will need to specify the risk premia that connect these factor dynamics under the Q-measure to the dynamics under the real-world (or physical) P-measure. It is important to note that there are no restrictions on the dynamic drift components under the empirical P-measure beyond the requirement of constant volatility. To facilitate empirical implementation, we use the essentially affine risk premium specification

¹¹This is the clean price that does not account for any accrued interest and maps to our observed bond prices.

introduced in Duffee (2002). In the Gaussian framework, this specification implies that the risk premia Γ_t depend on the state variables; that is,

$$\Gamma_t = \gamma^0 + \gamma^1 X_t,$$

where $\gamma^0 \in \mathbf{R}^4$ and $\gamma^1 \in \mathbf{R}^{4 \times 4}$ contain unrestricted parameters.

Thus, the resulting unrestricted four-factor AFNS-R model has P-dynamics given by

$$dX_t = K^{\mathbb{P}}(\theta^{\mathbb{P}} - X_t) + \Sigma dW_t^{\mathbb{P}},$$

where $K^{\mathbb{P}}$ is an unrestricted 4×4 mean-reversion matrix, $\theta^{\mathbb{P}}$ is a 4×1 vector of mean levels, and Σ is a 4×4 lower triangular volatility matrix. This is the transition equation in the extended Kalman filter estimation of the AFNS-R model.

4.2 Model Estimation and Econometric Identification

Due to the nonlinear relationship between state variables and bond prices in equation (4), the model cannot be estimated with the standard Kalman filter. Instead, we use the extended Kalman filter as in Kim and Singleton (2012); see Christensen and Rudebusch (2019) for details. Furthermore, to make the fitted errors comparable across bonds of various maturities, we scale each bond price by its duration. Thus, the measurement equation for the bond prices takes the following form

$$\frac{P_t^i(t_0^i,\tau^i)}{D_t^i(t_0^i,\tau^i)} = \frac{\widehat{P}_t^i(t_0^i,\tau^i)}{D_t^i(t_0^i,\tau^i)} + \varepsilon_t^i.$$

Here, $\widehat{P}_t^i(t_0^i, \tau^i)$ is the model-implied price of bond i, $D_t^i(t_0^i, \tau^i)$ is its duration, which is calculated before estimation, and ε_t^i represents independent and Gaussian distributed measurement errors with mean zero and a common standard deviation σ_{ε} . See Andreasen et al. (2019) for evidence supporting this formulation of the measurement equation.

Furthermore, since the marketwide bond-specific risk factor is a latent factor that we do not observe, its level is not identified without additional restrictions. As a consequence, we let the first 30-year bond issued on April 6, 1994, and maturing on November 10, 2024, with 7% coupon have a unit loading on this factor, that is, $\beta^i = 1$ for this security. This choice implies that the β^i sensitivity parameters measure sensitivity to this factor relative to that of the 30-year 2024 bond. Moreover, we note that the $\lambda^{R,i}$ -parameters can be hard to identify if their values are too large or too small. As a result, we impose the restriction that they fall within the range from 0.0001 to 10, which is without practical consequences. Also, for numerical stability during model optimization, we impose the restriction that the β^i -parameters fall within the range from 0 to 250.

Finally, we follow the finance literature and assume stationarity of the state variables, which allows us to start the Kalman filter at their unconditional mean.

$K^{\mathbb{P}}$	$K^{\mathbb{P}}_{\cdot,1}$	$K^{\mathbb{P}}_{\cdot,2}$	$K^{\mathbb{P}}_{\cdot,3}$	$K^{\mathbb{P}}_{\cdot,4}$	$ heta^{\mathbb{P}}$		Σ
$K_{1,\cdot}^{\mathbb{P}}$	0.0138	0	0	0	0.0632	σ_{11}	0.0062
,	(0.0508)				(0.0462)		(0.0002)
$K_{2,\cdot}^{\mathbb{P}}$	0	0.8410	0	1.8676	-0.0297	σ_{22}	0.0116
,		(0.2428)		(0.5291)	(0.0100)		(0.0009)
$K_{3,\cdot}^{\mathbb{P}}$	0	0	0.2147	0	-0.0162	σ_{33}	0.0156
,			(0.1909)		(0.0209)		(0.0011)
$K_{4,\cdot}^{\mathbb{P}}$	0	0	0	0.4665	0.0020	σ_{44}	0.0070
				(0.2996)	(0.0051)		(0.0008)

Table 4: Estimated Dynamic Parameters of the Preferred AFNS-R Model

The table shows the estimated parameters of the $K^{\mathbb{P}}$ matrix, $\theta^{\mathbb{P}}$ vector, and diagonal Σ matrix for the preferred AFNS-R model. The estimated value of λ is 0.2921 (0.0058), while $\kappa_R^{\mathbb{Q}} = 1.9506$ (0.1103) and $\theta_R^{\mathbb{Q}} = -0.0030$ (0.0003). The maximum log likelihood value is 16,179.75. The numbers in parentheses are the estimated parameter standard deviations.

4.3 Estimation Results

For our analysis we consider the preferred specification of the AFNS-R model identified by CH. They use a general-to-specific strategy starting from an unrestricted $K^{\mathbb{P}}$. In each step, the parameter in $K^{\mathbb{P}}$ with the lowest t-statistic is eliminated. They then rely on the Bayesian information criterion (BIC) and marginal likelihood ratio tests to find the optimal stopping point as in Christensen et al. (2014). Their preferred specification has \mathbb{P} -dynamics given by

$$\begin{pmatrix} dL_t \\ dS_t \\ dC_t \\ dX_t^R \end{pmatrix} = \begin{pmatrix} \kappa_{11}^{\mathbb{P}} & 0 & 0 & 0 \\ 0 & \kappa_{22}^{\mathbb{P}} & 0 & \kappa_{24}^{\mathbb{P}} \\ 0 & 0 & \kappa_{33}^{\mathbb{P}} & 0 \\ 0 & 0 & 0 & \kappa_{44}^{\mathbb{P}} \end{pmatrix} \begin{pmatrix} \begin{pmatrix} \theta_1^{\mathbb{P}} \\ \theta_2^{\mathbb{P}} \\ \theta_3^{\mathbb{P}} \\ \theta_4^{\mathbb{P}} \end{pmatrix} - \begin{pmatrix} L_t \\ S_t \\ C_t \\ X_t^R \end{pmatrix} dt + \sum \begin{pmatrix} dW_t^{L,\mathbb{P}} \\ dW_t^{S,\mathbb{P}} \\ dW_t^{C,\mathbb{P}} \\ dW_t^{R,\mathbb{P}} \end{pmatrix},$$

where Σ is a diagonal matrix as recommended by Christensen et al. (2011).

We note that the 11 parameters eliminated in the $K^{\mathbb{P}}$ mean-reversion matrix are statistically insignificant both individually and collectively as demonstrated by CH. Hence, the data are singling out this favored specification in a very strong way. As a consequence, we feel comfortable relying on this preferred specification for our analysis of bond-specific safety and general term premia in the Danish government bond market.

The estimated parameters of the preferred specification are reported in Table 4, while results reported in CH show that the AFNS-R model provides a very tight fit to the Danish bond price data and hence not repeated here. Furthermore, the fact that $\kappa_{24}^{\mathbb{P}}$ is large and positive implies that there is a fairly strong negative correlation between the slope factor S_t and the bond-specific risk factor X_t^R , i.e., a high value of X_t^R will tend to drive S_t lower. Practically speaking, this means that when X_t^R is high and the Danish safety premia are under pressure, Danish short-term interest rates have a tendency to fall. Economically, a declining

Danish safety premium means that Danish government bond yields are being pushed up. All else being equal, this should be associated with capital inflows from abroad attracted by the higher interest rates. This will put upward pressure on the value of the Danish krone against the euro. To offset that pressure and keep the tight peg of the exchange rate to the euro, the DNB can at first intervene in the exchange rate market, but if the pressure is sustained, the ultimate remedy is to lower the Danish overnight rate, which will show up in our analysis as a decline in S_t .

4.4 The Estimated Bond Risk Premia

We first use the estimated AFNS-R model to extract the safety premium in the Danish government bond market. To compute this premium, we first use the estimated parameters and the filtered states $\left\{X_{t|t}\right\}_{t=1}^{T}$ to calculate the fitted bond prices $\left\{\hat{P}_{t}^{i}\right\}_{t=1}^{T}$ for all outstanding securities in our sample. These bond prices are then converted into yields to maturity $\left\{\hat{y}_{t}^{c,i}\right\}_{t=1}^{T}$ by solving the fixed-point problem

$$\hat{P}_{t}^{i} = C(t_{1} - t) \exp\left\{-(t_{1} - t)\hat{y}_{t}^{c,i}\right\} + \sum_{k=2}^{n} C \exp\left\{-(t_{k} - t)\hat{y}_{t}^{c,i}\right\} + \exp\left\{-(T - t)\hat{y}_{t}^{c,i}\right\},$$
(5)

for $i=1,2,...,n_t$, meaning that $\left\{\hat{y}_t^{c,i}\right\}_{t=1}^T$ is approximately the rate of return on the *i*th bond if held until maturity (see Sack and Elsasser 2004). To obtain the corresponding yields with correction for the safety premium, a new set of model-implied bond prices are computed from the estimated AFNS-R model but using only its frictionless part, i.e. with the constraints that $X_{t|t}^R=0$ for all t, $\theta_R^\mathbb{Q}=0$, and $\sigma_{44}=0$. These prices are denoted $\left\{\tilde{P}_t^i\right\}_{t=1}^T$ and converted into yields to maturity $\tilde{y}_t^{c,i}$ by solving equation (5) in the same way as above. They represent estimates of the prices that would prevail in a world without any financial frictions or convenience premia. The safety premium for the *i*th bond is then defined as

$$\Psi_t^i \equiv \tilde{y}_t^{c,i} - \hat{y}_t^{c,i}. \tag{6}$$

Second, we define the term premium in the standard way as

$$TP_t(\tau) = y_t(\tau) - \frac{1}{\tau} \int_t^{t+\tau} E_t^{\mathbb{P}}[r_s] ds.$$
 (7)

That is, the term premium is the difference in expected return between a buy-and-hold strategy for a τ -year bond and an instantaneous rollover strategy at the risk-free rate r_t . Importantly, $y_t(\tau)$ is the frictionless yield left over after the bond-specific safety premia have been accounted for. The model thus allows us to decompose bond yields into their respective term

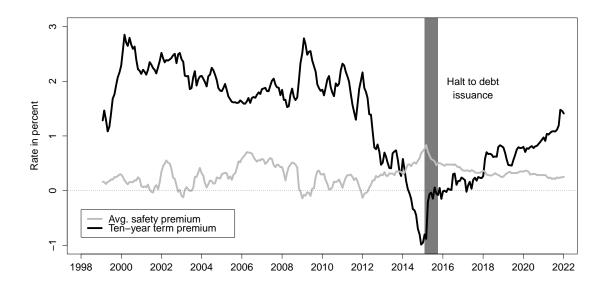


Figure 4: Average Bond Safety Premium and Ten-Year Term Premium

Illustration of the average estimated Danish government bond safety premium for each observation date implied by the AFNS-R model. The safety premia are measured as the estimated yield difference between the frictionless yield to maturity of individual bonds with the marketwide bond-specific risk factor turned off and the corresponding fitted yield to maturity. Also shown is the ten-year term premium of Danish government bonds calculated using equation (7). The data cover the period from January 31, 1999, to December 31, 2021.

premia and short-rate expectations components in addition to the safety premia described above.

Figure 4 shows the average Danish government bond safety premium $\bar{\Psi}_t$ across the outstanding bonds at a given point in time. The average estimated safety premium clearly varies notably over time: it fell to a minimum of negative 12 basis points in late 2008; it later reached a maximum of 81 basis points in January 2015, shortly after the Swiss National Bank had abandoned its minimum exchange rate to the euro and the ECB had announced its first open-ended large-scale purchases of euro-area government bonds. For the entire period, the series has an average of 29.42 basis points with a standard deviation of 18.55 basis points.

Figure 4 also shows the Danish ten-year term premium, which has changed little on net, but is characterized by fairly large persistent swings during our sample period. It averages 134.30 basis points with a standard deviation of 88.55 basis points. Thus, conventional term premia are an order of magnitude larger and more volatile than safety premia. Still, the two risk premium series have a negative correlation of -53 percent. Given that the safety premium represents the extra yield investors forgo by holding the very safe Danish government bonds, a higher safety premium is equivalent to a lower absolute yield. Hence, the negative correlation implies that both premia tend to push the observed bond yields in the same direction, but

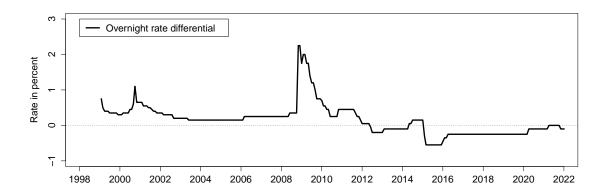


Figure 5: Overnight Rate Differential

Illustration of the difference between the Danish overnight interest rate of the certificates of deposits set by the Danish National Bank and the main overnight rate set by the European Central Bank. The data are monthly covering the period from January 31, 1999, to December 31, 2021.

the less-than-perfect correlation underscores that they represent distinct risk premia in the prices of Danish government bonds.

In terms of understanding the impact of the debt halt on Danish bond yields, we note up front that Denmark's exchange rate policy aimed at keeping the Danish krone stable against the euro is of particular importance. Accordingly, the DNB's key policy rate follows that of the ECB, with small deviations accounting for periods of extraordinary pressure on the krone in either direction as shown in Figure 5. Consequently, the expectations component of longerterm Danish government bond yields tends to mirror those of the core euro-area countries. That said, anticipated buying or selling pressures of the Danish krone vis-à-vis the euro may affect investors' near-term expectations about the spread between Danish and euro overnight rates. Indeed, this spread has assumed both positive and negative values for extended periods in the past. Hence, there may be minor deviations in the expectations component of Danish government bond yields from those embedded in core euro-area government bond yields. Overall, though, we are essentially assuming in our analysis that policy expectations in Danish and euro-area fixed-income markets are moving in tandem, and any unilateral actions by the DNB such as the halt to debt issuance analyzed here are assumed to not affect investors' policy expectations in any material way, in particular at medium- to long-term horizons. This effectively rules out any major yield effects materializing through the signaling channel.

In contrast, there are several tangible reasons why the risk premium components of Danish bond yields may not follow the same pattern as their euro-area counterparts, leading to interest rate spreads of considerable size at longer maturity horizons as described in Grønlund et al. (2022). First, because of the pegged exchange rate policy, unconventional monetary policy in the euro area is likely to have potential spillover effects on the risk premia of Danish

government bonds. The ECB's government bond purchases reduce the free float of euroarea government bonds and lower their risk premia as documented by Eser et al. (2019). In a frictionless world, this should give investors an incentive to buy Danish government bonds as a close and safe substitute. However, Danish government bonds cannot be used in euro-area general collateral repo agreements, which may make Danish government bonds comparatively less attractive to some investors, thereby dampening demand. Moreover, some investors may not be allowed to invest in Danish government bonds, say, due to restrictions on their investment mandates. Such financial frictions could adversely impact the substitution from euro-area government bonds to Danish bonds and depress the Danish safety premium, thereby limiting the pass-through of unconventional monetary policy. ¹³

5 Regression Analysis

To examine the impact on Danish government bond risk premia from the announced halt to government debt issuance, we use the average Danish safety premium and the ten-year Danish term premium estimates at monthly frequency covering the period from January 1999 to December 2021 described above. As stated earlier, we are interested in going beyond the immediate announcement effects on bond yields reported in Section 2 and measure the longer lasting impact on the Danish bond risk premia from this policy. We therefore regress these series on a dummy variable that is equal to one for the duration of the halt to debt issuance.

To control for the potential effects of the ECB's government bond purchases on the Danish bond risk premia, we consider two different measures of their size in our regression analysis. The first measure is the collateral scarcity premium of German government bonds, defined as the difference between the ECB deposit facility and general collateral repo rate for German government bonds and measured in percent; see Arrata et al. (2020).¹⁴ When the scarcity premium is positive, funds can be placed in the repo market below the ECB deposit facility rate, possibly reflecting that government bonds are scarce and in demand for repo transactions. The ECB's government bond purchases pushed the German scarcity premium into positive territory for all general collateral segments, as demonstrated by Schaffner et al. (2019). The second measure of the ECB's government bond purchases is the ECB's holdings of government-backed securities relative to annual nominal GDP in the euro area. This seems to be a reasonable proxy for the amount of truly safe assets held by the ECB, as argued

¹²Koijen et al. (2017) find that foreign investors exhibited the strongest reaction to the ECB's asset purchases under the PSPP in terms of rebalancing their portfolios toward more attractive investment opportunities elsewhere. That process could also have let them to reassess their perceptions about the relative safety of Danish safe assets.

¹³Alternatively, the ECB's asset purchases could raise the premia of all safe assets globally, although any broad-based effects from the asset purchases that lower the general interest rate level in the euro area should affect the frictionless yields within our model and not the bond-specific safety premia.

¹⁴In a Danish context, Grønlund et al. (2022) use the scarcity premium as a measure of ECB government bond purchases in their analysis of the Danish-German government bond spread.

by Christensen and Mirkov (2022). Both measures of the ECB's government bond purchases depend on the actual purchases by the ECB, and not the announcement of the purchases, reflecting that collateral scarcity occurs as bonds flow from the private market to the balance sheet of the ECB.

In addition to our main policy variables described above, we control for a variety of confounding factors as in CH. In a core set of control variables, we consider the CBOE's volatility index (VIX), the spread between Italian and German ten-year bond yields, the TED spread, and the ten-year on-the-run premium in U.S. Treasuries to proxy for investors' risk aversion, financial market uncertainty, and demand for safe-haven assets. ¹⁵ This set also contains the debt-to-GDP ratio—interpolated linearly from quarterly to monthly frequency to control for effects tied to the supply of Danish government bonds. 16 In addition, it includes the Danish overnight deposit rate as a proxy for the opportunity cost of holding money and the associated liquidity premia of Danish government bonds, as explained in Nagel (2016). Furthermore, we include the average Danish government bond age and the one-month realized volatility of the ten-year Danish government bond yield as additional proxies for bond liquidity following the work of Houwling et al. (2005).¹⁷ Inspired by the analysis of Hu et al. (2013), we also include a noise measure of Danish government bond prices to control for the variation in the amount of arbitrage capital available in this market. Finally, as a control for credit risk, we use both the yield spread between Danish and German ten-year government bonds and the difference in the debt-to-GDP ratio between Denmark and Germany, 18 and we include the EUR-DKK cross-currency basis to control for differences in funding costs. To go beyond this set of core control variables, we include a few additional potentially confounding factors in our regressions. We add the overnight federal funds rate to proxy for the U.S. safe-asset liquidity premium as in Nagel (2016), and reported earnings per share of companies in the S&P 500 stock price index to account for opportunity costs in the equity market. Finally, we also consider the MOVE volatility index to proxy for risk aversion in the bond market. Throughout, we use a sample from January 1999 to December 2021.

To test for the potential effects of the halt to debt issuance, we run linear regressions that take the following form:

$$Y_t = \alpha + \beta \cdot D_t^{halt} + \gamma \cdot QE_t + \delta \cdot X_t + \varepsilon_t, \tag{8}$$

where the dependent variable Y_t is the relevant outcome variable (the average safety premium $\bar{\Psi}_t$ or the ten-year term premium $TP_t(10)$). In terms of the explanatory variables, D_t^{halt} is the key dummy variable for the government debt issuance stop in 2015, QE_t contains either

 $^{^{15}\}mathrm{See}$ Grisse and Nitschka (2015).

¹⁶See Krishnamurthy and Vissing-Jorgensen (2012).

¹⁷The one-month realized volatility is estimated based on a standard sample estimator using daily yields.

¹⁸An alternative measure is the credit default swap rate for Danish government bonds, which unfortunately only is available from 2008 onwards.

Panel A: Average Safety Premium

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
D_t^{halt}	33.79***	33.56***	20.61***	19.48***	33.03***	19.66***	15.75**
	(6.41)	(6.89)	(6.18)	(6.90)	(6.44)	(6.77)	(7.55)
Scarcity premium		22.76^{*}	-29.36**	-39.11**			
		(16.18)	(15.43)	(17.12)			
(PSPP+PEPP)/GDP					0.13	-0.47**	-1.06***
					(0.16)	(0.23)	(0.34)
Controls	None	None	Core	All	None	Core	All
$\mathrm{Adj}\ R^2$	0.10	0.11	0.56	0.60	0.10	0.56	0.62
DW	0.15	0.15	0.32	0.38	0.15	0.30	0.36

Panel B: Ten-Year Term Premium

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
D_t^{halt}	-164.25***	-186.26***	-67.37***	-68.19***	-179.38***	-51.00**	-35.11*
	(17.84)	(27.86)	(26.14)	(26.03)	(19.09)	(26.45)	(24.83)
Scarcity premium		-503.06***	-19.34	15.84			
		(82.82)	(78.52)	(78.54)			
(PSPP+PEPP)/GDP					-4.14***	2.42^{***}	5.74***
					(1.04)	(0.91)	(1.31)
Controls	None	None	Core	All	None	Core	All
$Adj R^2$	0.11	0.35	0.75	0.77	0.28	0.77	0.81
DW	0.05	0.1	0.35	0.39	0.07	0.36	0.40

Table 5: Estimated Effects of the Halt to Debt Issuance on Danish Government Bond Risk Premia

The top panel reports the estimated coefficients of the regression in equation (8) with the average Danish safety premium as the dependent variable, while the bottom panel reports the estimated coefficients of the same regression with the Danish ten-year term premium as the dependent variable. The numbers in parentheses contain the estimated standard deviations using Newey-West standard errors with three monthly lags. The sample starts in January 1999 and ends in December 2021. Stars *, **, and *** indicate significance at the 10, 5 and 1 percent level, respectively.

the scarcity premium or the ECB's holdings of government bonds divided by the nominal euro-area GDP, and X_t contains the controlling variables. Finally, ε_t is an error term.

In the following, we run seven regressions for both measures of bond risk premia. The first includes no controls to demonstrate that our results carry through even in this naive case. For each proxy for the ECB government bond purchases, we then run three separate regressions, one with no additional controls, another with the core set of controls, and a final one with all controls included.

The results of the regressions are reported in Table 5. The empirically relevant results with controls show that the average Danish safety premium was 16-21 basis points higher than could otherwise have been anticipated for the duration of the halt to debt issuance. At the same time, the Danish ten-year term premium was reduced by 35-68 basis points.

Given that the safety premium represents the extra yield investors forgo by holding the very safe Danish government bonds, a higher safety premium is equivalent to a lower absolute yield. Moreover, given that the two bond risk premia represent separate components in the government bond prices, the estimated effects can be added together. Hence, the combined results suggest that Danish government bond yields were significantly lower than they would otherwise have been by between 51 basis points and as much as 89 basis points for the duration of the halt to debt issuance. Based on these findings we conclude that passive QE works by lowering long-term bond yields through both reduced term premia, which would be consistent with supply-induced portfolio balance effects, and increased safety premia, which would be consistent with scarcity effects of safe assets. Furthermore, given that the size of the estimated effects is quantitatively similar to those reported in studies of QE programs in the United States and the United Kingdom, the results suggest that passive QE may be about as effective at lowering interest rate levels and easing financial market conditions as traditional active QE programs. In particular, this is likely to hold for bond markets with sizable safety premia where bargaining power is already tilted towards sellers so that effects of the liquidity transmission channel of QE are likely to be minimal.

Finally, the regression results show that the ECB's bond purchases tend to lower Danish safety premia and lift Danish term premia. These observations are consistent with the findings of both CH for the Danish bond risk premia specifically and Christensen et al. (2023) based on an international panel of safety premia. The negative impact on the Danish safety premia underscores that safe asset purchases by major central banks have the ability to produce international spillover effects by altering investors' perceptions about the scarcity of safe assets in nearby foreign bond markets and hence depress the premium that safe foreign bonds can command. The positive effect on Danish term premia points to an international substitution channel whereby investors rotate out of non-targeted foreign safe assets and use the revenue to increase their exposures to the euro-area government bonds targeted by the ECB's bond purchases.

In summary, the Danish halt to debt issuance helped offset the negative effects on Danish bond yields from ECB's QE programs. In turn, this helped reduce the pressure on the Danish krone. Ultimately, this allowed the DNB to normalize the debt issuance on behalf of the Danish government. From this perspective, the temporary halt to debt issuance achieved its objectives and can be viewed as a successful policy choice in an usual and difficult situation with few other viable alternatives.

6 Conclusion

In this paper, we argue that a temporary halt to debt issuance by the government is theoretically equivalent to the central bank launching a QE program of similar size in that they both reduce the anticipated future bond supply available to private investors. Operationally,

however, this policy is unlikely to affect bond market liquidity conditions as it involves no active bond purchases by the central bank. Moreover, without the creation of any central bank reserves, it cannot produce any reserve-induced portfolio balance effects arising from banks' reaction to the dilution in the average interest rate risk of their asset portfolios.

For evidence on the effects of such a passive QE policy, we focus on Denmark, where the government unexpectedly announced a halt to debt issuance in January 2015 that ended up lasting until October 2015. An added advantage of focusing on Denmark is that its long-established and tight exchange rate peg of the Danish krone to the euro allows us to rule out any signaling effects about future monetary policy from the debt halt announcement. As a consequence, we can limit our analysis to changes in Danish bond-specific safety and general term premia, where our results suggest that the halt helped raise bond safety premia and lower term premia for the duration of its enforcement. This points to two main transmission mechanisms of passive QE to financial markets. One operates by raising bond safety premia through a scarcity channel, while the other works by lowering long-term bond yields through standard supply-induced portfolio balance effects on term premia. Based on the latter finding, we claim to be the first to provide direct evidence of the supply-induced portfolio balance channel that is the main transmission channel emphasized in the empirical literature on financial market effects of QE.

In terms of the practical relevance of passive QE, it is important to stress that a halt to government debt issuance only represents a viable alternative to launching a regular QE program in order to ease financial conditions provided the government can credibly claim to have sufficient funds to sustain its operations for the committed period. This necessary precondition should be kept in mind when it comes to pursuing this policy. However, as for the identified transmission channels, we think they would apply equally well to other safe government bond markets.

Finally, given that QT in many ways can be viewed as a passive reversal of previous QE programs as explained in the introduction, our findings suggest that this policy may be quite contractionary on financial conditions. However, we leave it for future research to examine that conjecture.

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